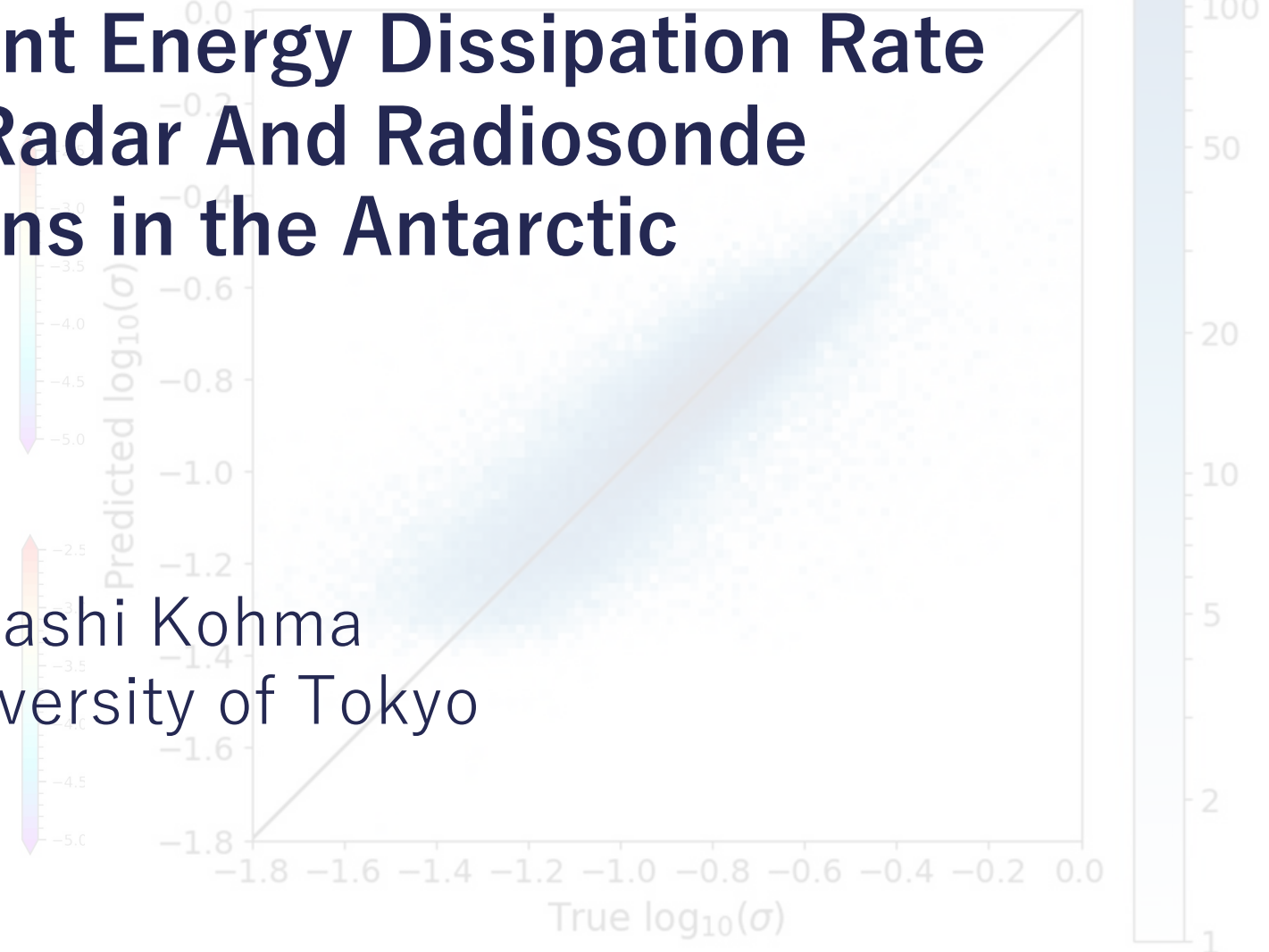
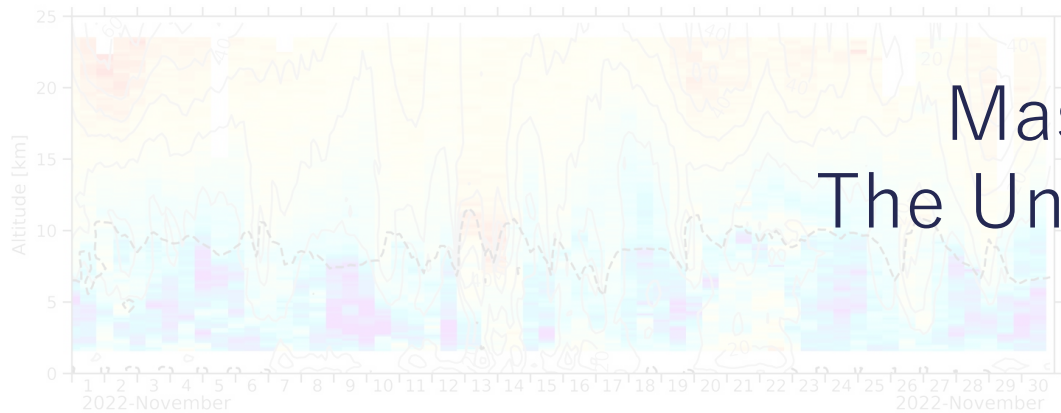
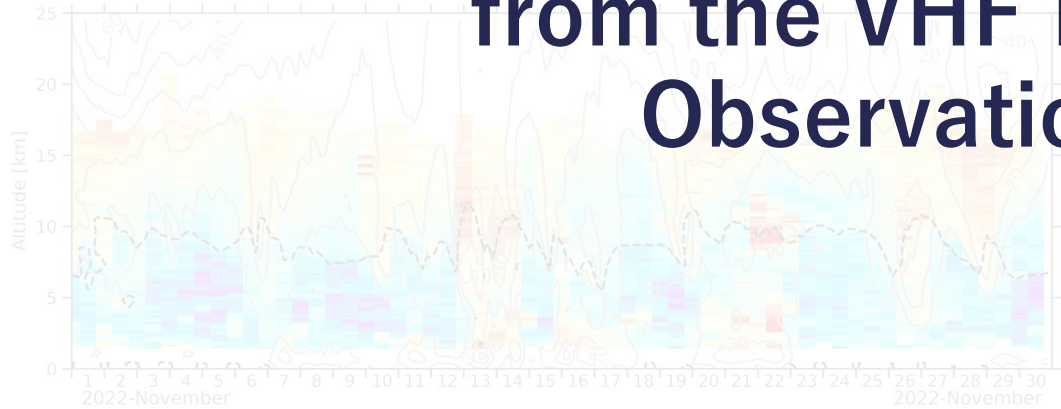


# Estimate of Turbulent Energy Dissipation Rate from the VHF Radar And Radiosonde Observations in the Antarctic



Masashi Kohma  
The University of Tokyo

This study is supported by JST FOREST program

# Outline

## 0. Introduction

- Estimation of energy dissipation rates in the free atmosphere

## 1. Turbulent Energy Dissipation Rates ( $\varepsilon$ ) Comparison:

- Used VHF radar data at Syowa Station, Antarctic
- Compared with radiosonde-based estimation via Thorpe method

(Kohma et al., 2019)

## 2. Preliminary Results of Machine Learning (ML) Approach for Estimating $\varepsilon$

- Developed a ML-based algorithm to estimate  $\varepsilon$  from the radiosonde observations.

# Introduction

- **Turbulent kinetic energy dissipation rates ( $\varepsilon$ ):**  
A variable representing loss rate of turbulent kinetic energy
- Estimation method of  $\varepsilon$  in the free atmosphere
  - VHF/UHF radar (e.g., Sato & Woodman, 1982; Hocking, 1983)
    - **Spectral width method** / Power method
  - **Radiosondes** (e.g., Clayson & Kantha, 2008; Wilson et al., 2011)
    - **Thorpe method**
  - Aircraft/UAV (e.g., Sharman et al., 2014; Luce et al., 2018; 2023)
  - Rocket (e.g., Luebken, 1997; Luebken et al., 2002)
  - etc. (e.g., Schneider et al., 2015)

# Introduction

Estimation of  $\varepsilon$  by Thorpe method (Thorpe, 1977)

Thorpe Scale  $L_T$  : Local overturning length scale

1. Sort the measured density profile (left panel) into a monotonic profile (right panel)
2. Calculate displacement distance of each sample ( $d = z_m - z_n$ )
3. Obtain  $L_T$  as the root-mean-square of  $d$

Ozmidov Scale  $L_O \equiv \left(\frac{\varepsilon}{N^3}\right)^{1/2}$  : Maximum turbulence length scale in a stratified fluid

Oceanic microstructure observations empirically indicated the proportional relation

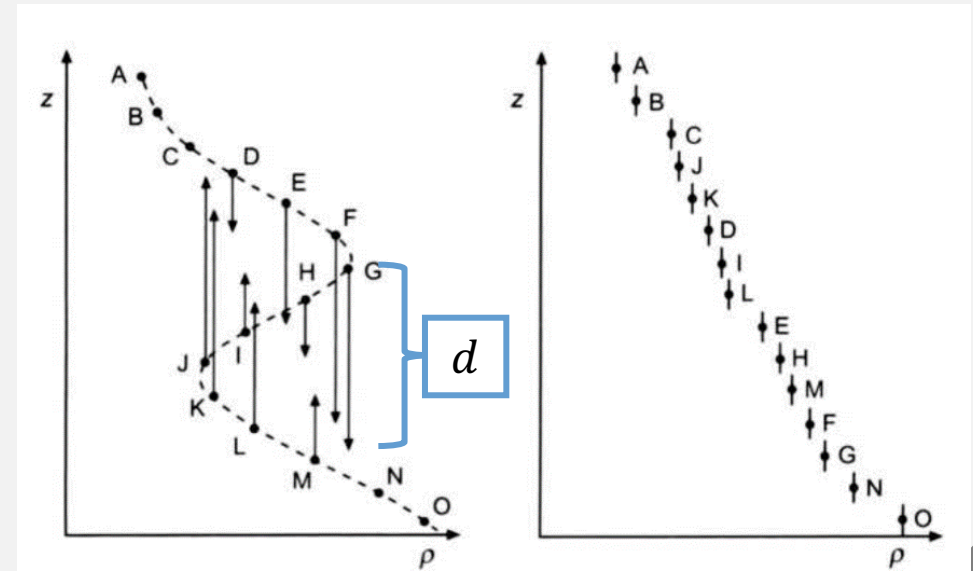
$$L_O = cL_T. (c = 0.25-4)$$

Using this relation, we obtain

$$\varepsilon = c^2 L_T^2 N^3$$

Measured density profile

Sorted density profile



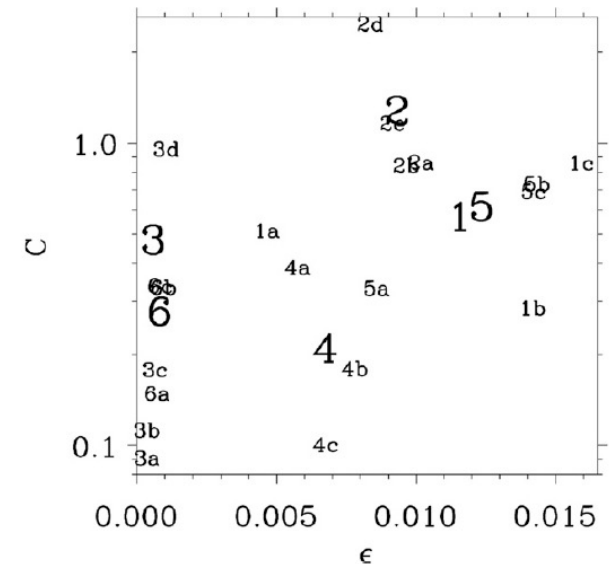
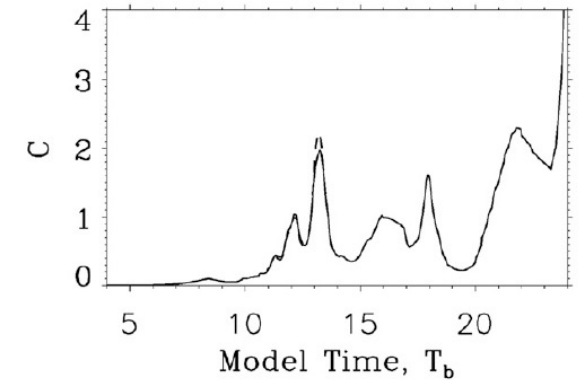
From Thorpe (1977)

# Introduction

## Uncertainty of $\varepsilon$ from Thorpe method

- The uncertainty of  $c$  (0.25-4) results in two orders of magnitude uncertainty of  $\varepsilon$  ( $\because \varepsilon \propto c^2$ )
- Fritts et al. (2016):  $c$  values can vary depending on event type (e.g., KH instability or wave breaking) and timing
- Schneider et al. (2015): The discrepancy of  $\varepsilon$  for individual layers is up to a factor of 3000.

⇒ Comparison between **radar-based** and **Thorpe-based**  $\varepsilon$  using observations at Syowa Station, Antarctic (Kohma et al., 2019)



Fritts et al. (2016)



# The program of Antarctic Syowa radar (PANSY radar)

Mesosphere-Stratosphere-Troposphere/Incoherent Scatter radar at Syowa Station (69S, 40E) in the Antarctic

System	Pulse Doppler radar. Active phased array system
Center freq.	47MHz
Antenna	Array consisting of <b>1045</b> crossed Yagi antennas <u>equivalent</u> to the circular area with a diameter of 160m ( <b>18000m<sup>2</sup></b> ), light and tough (12.6kg/antenna)
Transmitter	<b>1045</b> solid-state TR modules <b>Peak Power : 520kW</b>
Receiver	55 channel digital receiving systems Ability of imaging and interferometry obs
Power consumption	<b>66kW</b> (E-class amplifier)
Peripheral	24 antennas for E-layer FAI observation

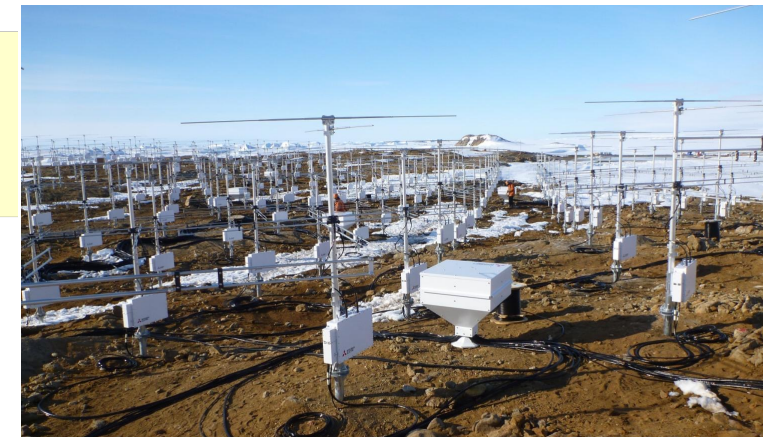
## Previous studies using the radar

- GWs in the troposphere-stratosphere: (Sato et al., 2014; Minamihara et al. 2018; 2020)
- GWs in the mesosphere: (Sato et al., 2017; Shibuya et al., 2017; Shibuya & Sato, 2019)
- Turbulent energy dissipation rates: (Kohma et al., 2019; 2020; 2021; Minamihara et al., 2023)

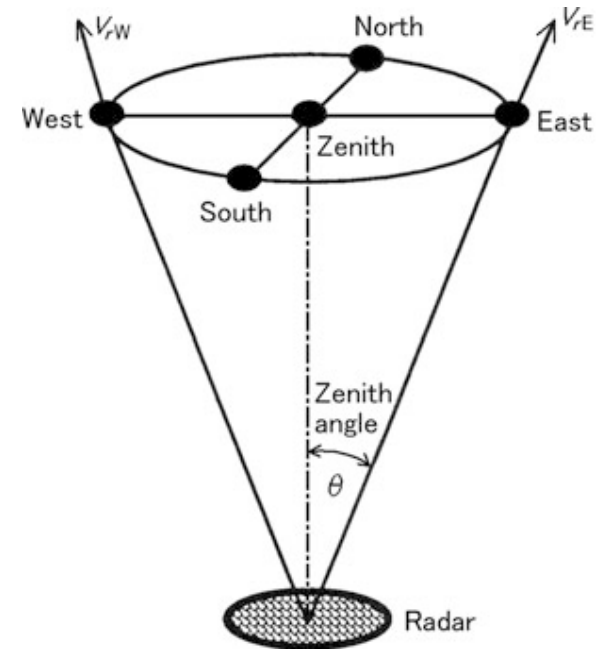
Observation of 3-d wind vectors in height regions of 1.5-20km and 60-90 km, and plasma parameters in 100-500 km with fine resolution and high accuracy

**Direct estimation of vertical flux of horizontal momentum associated with gravity waves**

The full-system observations with all antenna groups has been operated continuously since October 2015.



# Data: PANSY radar



Time interval:  $\sim 200$  s

Range resolution: 150 m (troposphere and stratosphere)

For estimation of energy dissipation rates,  
4 off-vertical beams with a zenith angle of  $10^\circ$   
are used to avoid the effect of specular reflection.

## Estimation of $\varepsilon$ from radar spectral widths

- $\sigma_{\text{obs}}^2 = \sigma_{\text{T}}^2 + \sigma_{\text{B}}^2 + \sigma_{\text{S}}^2 + \sigma_{\text{W}}^2$  ( $\sigma_{\text{T}}^2$ : Turbulence;  $\sigma_{\text{B}}^2$ : Beam broadening;  $\sigma_{\text{S}}^2$ : Shear broadening;  $\sigma_{\text{W}}^2$ : Time broadening)

Beam broadening  $\sigma_{\text{B}}^2$  is removed using an algorithm developed by Nishimura et al. (2020)

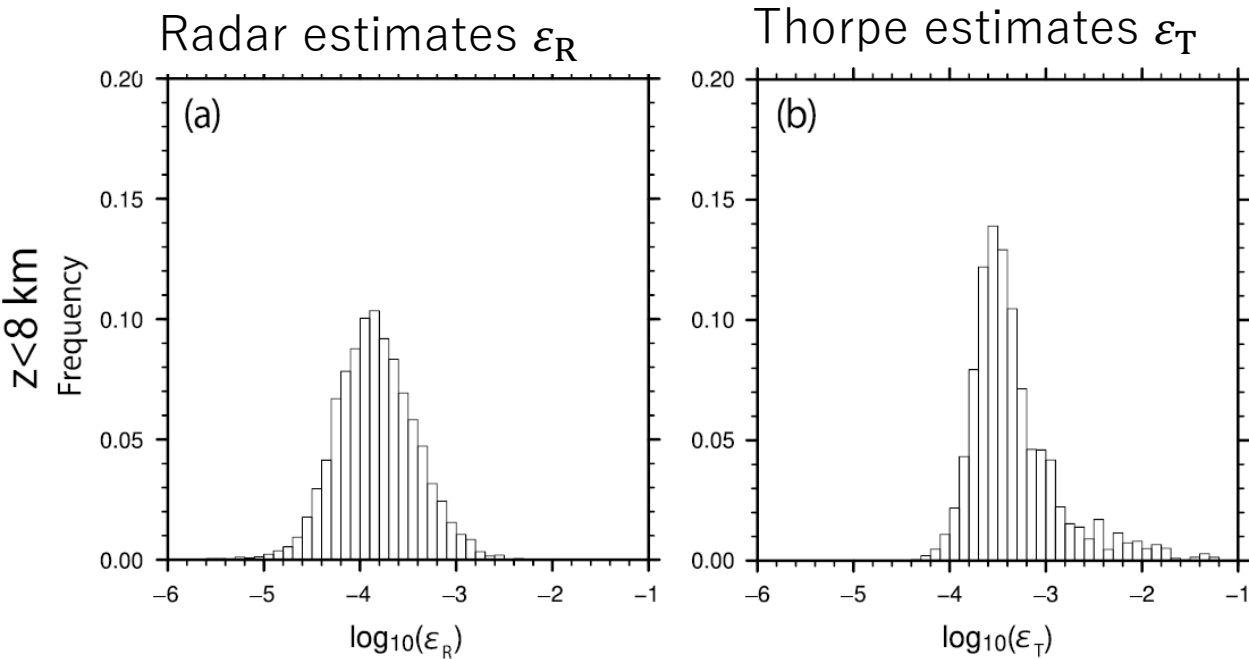
- $\varepsilon = 0.46 N w_{\text{std}}^2$  ( $w_{\text{std}}^2 = \frac{\sigma_{\text{T}}^2}{2 \ln 2}$ ) (Sato & Woodman 1982; Hocking, 1983)

where  $N$  is buoyancy frequency

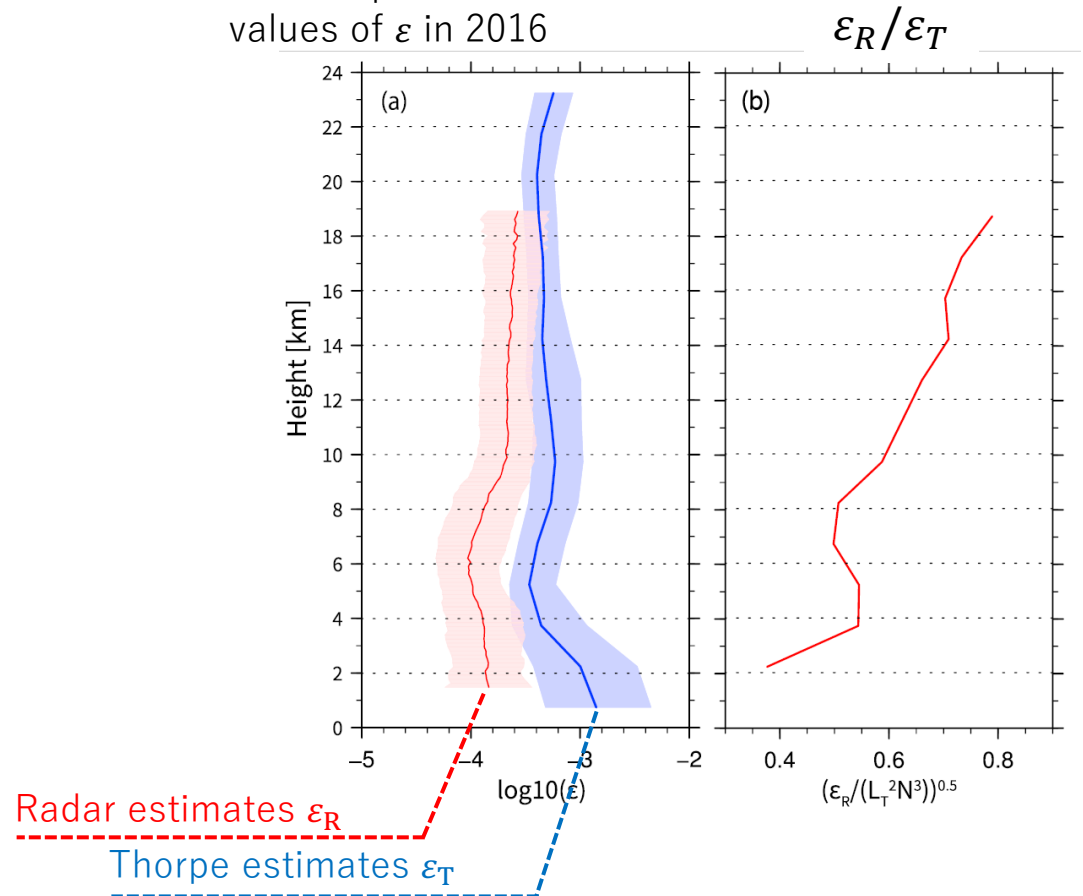
In the following,  $\varepsilon$  averaged over 4 off-vertical beams are shown.

# Comparison of $\varepsilon$ - radar estimation and Thorpe estimation

$$c(\equiv L_o/L_T) = 1$$



Vertical profiles of median  
values of  $\varepsilon$  in 2016



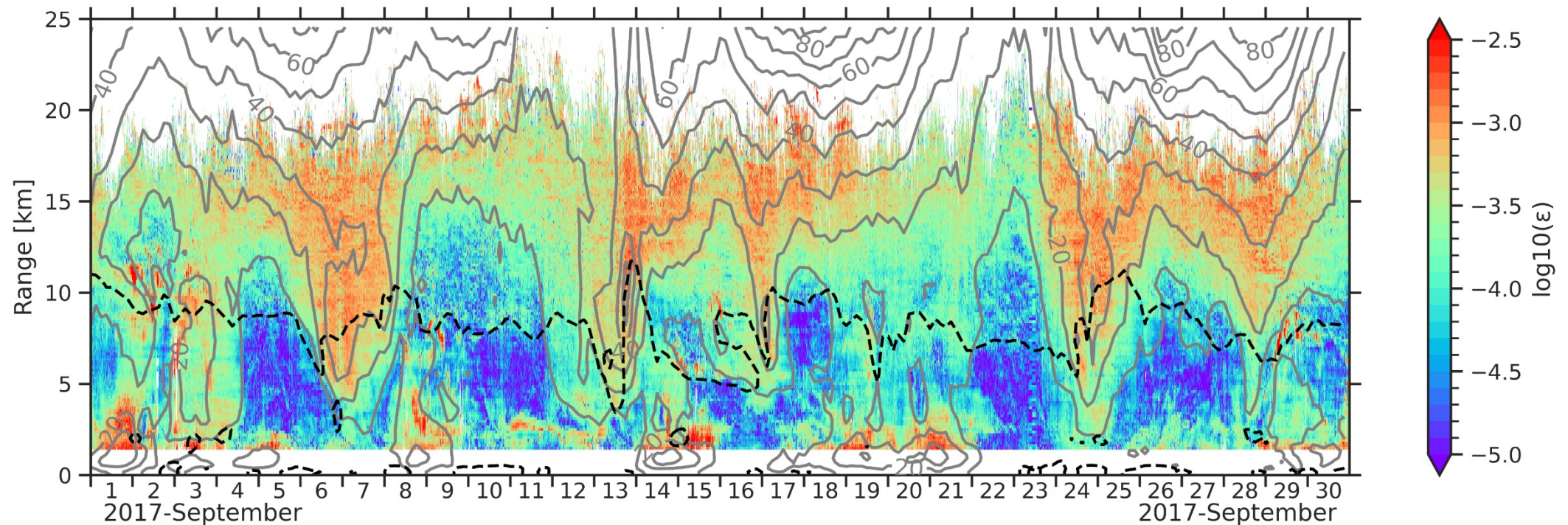
The ratio of radar-based  $\varepsilon$  to Thorpe-based  $\varepsilon$  is small in  $z=1.5-9$  km compared to over 11 km.

There are more recent studies including discussion on  $\varepsilon$  estimation based on Thorpe method.  
(e.g., Wang et al., 2019; Luce et al., 2023)



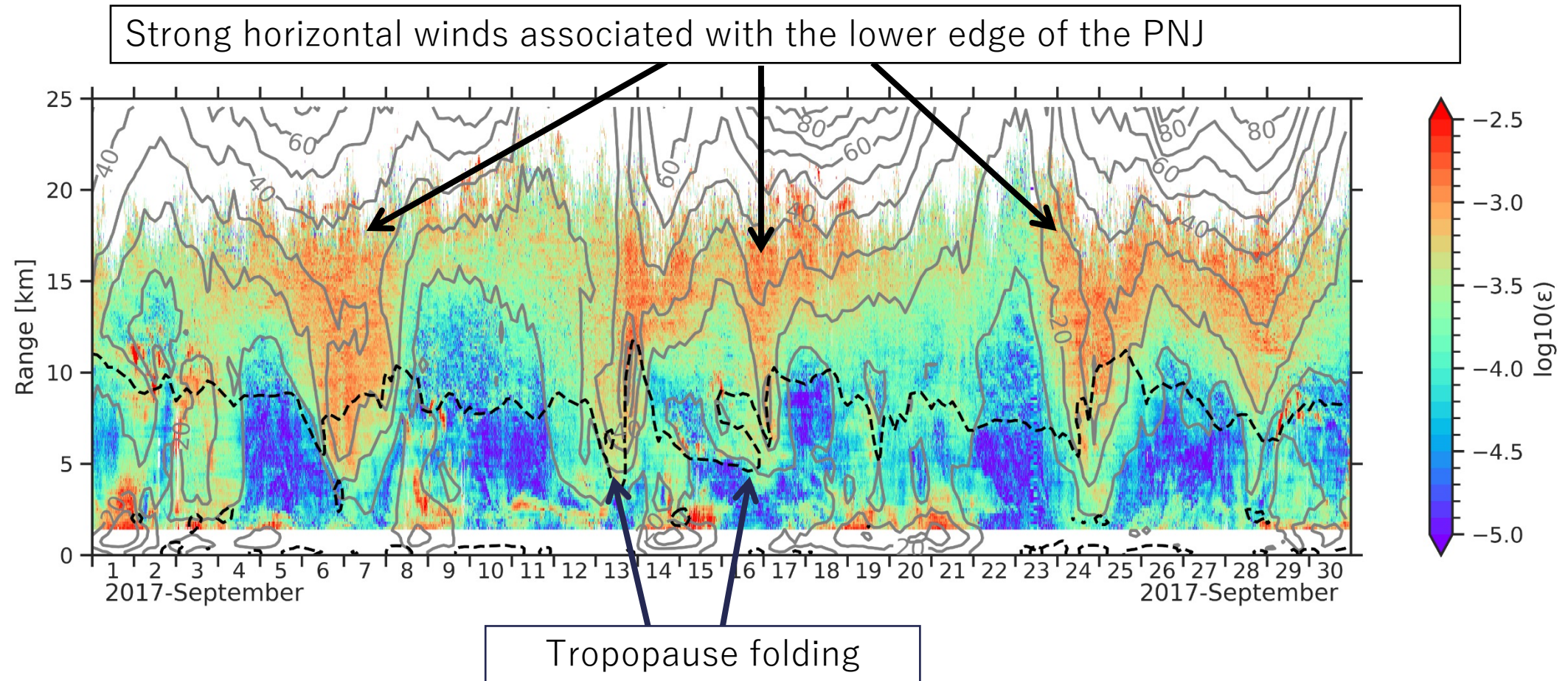
# Short-term variation of $\varepsilon$ from the radar - A time-height section (Sep. 2017)

$\log_{10}(\varepsilon)$  (color), Tropopause (PV=2PVU, black broken contour),  $\sqrt{u^2 + v^2}$  (JRA55, gray contour)



# Short-term variation of $\varepsilon$ from the radar - A time-height section (Sep. 2017)

$\log_{10}(\varepsilon)$  (color), Tropopause (PV=2PVU, black broken contour),  $\sqrt{u^2 + v^2}$  (JRA55, gray contour)

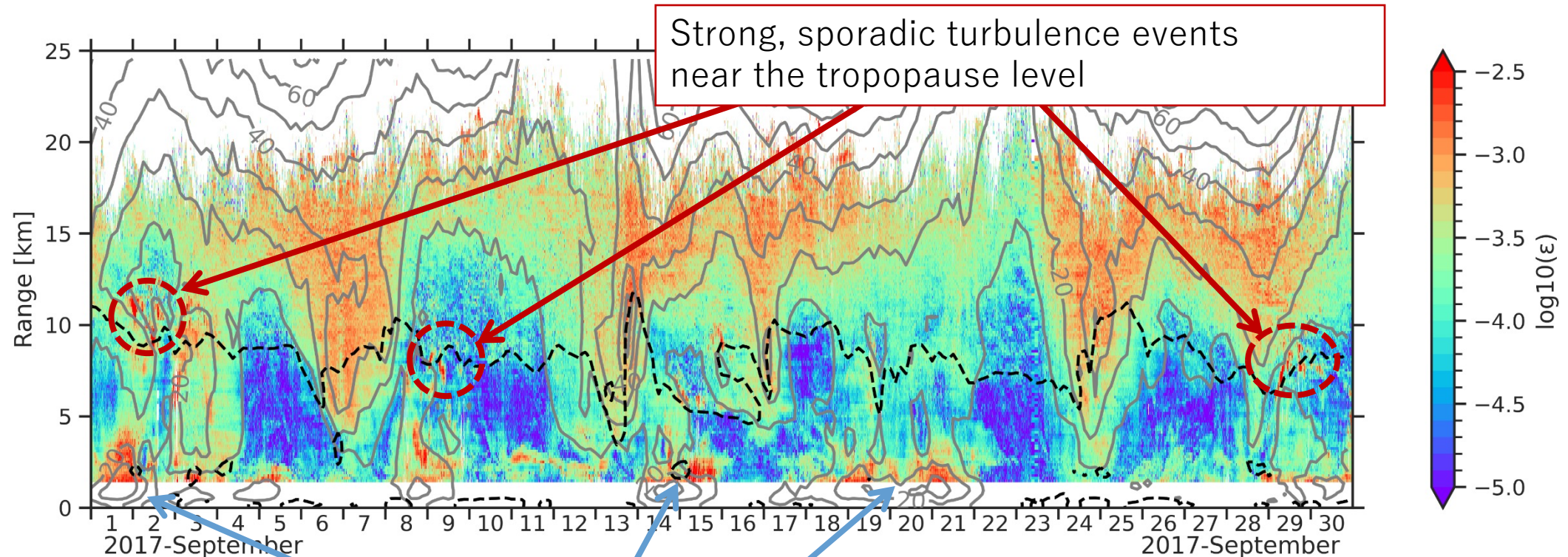


Note: Tropopause folding occur frequently along the coast of Antarctica compared to the southern mid latitudes (Kohma et al., 2022)



# Short-term variation of $\varepsilon$ from the radar - A time-height section (Sep. 2017)

$\log_{10}(\varepsilon)$  (color), Tropopause (PV=2PVU, black broken contour),  $\sqrt{u^2 + v^2}$  (JRA55, gray contour)

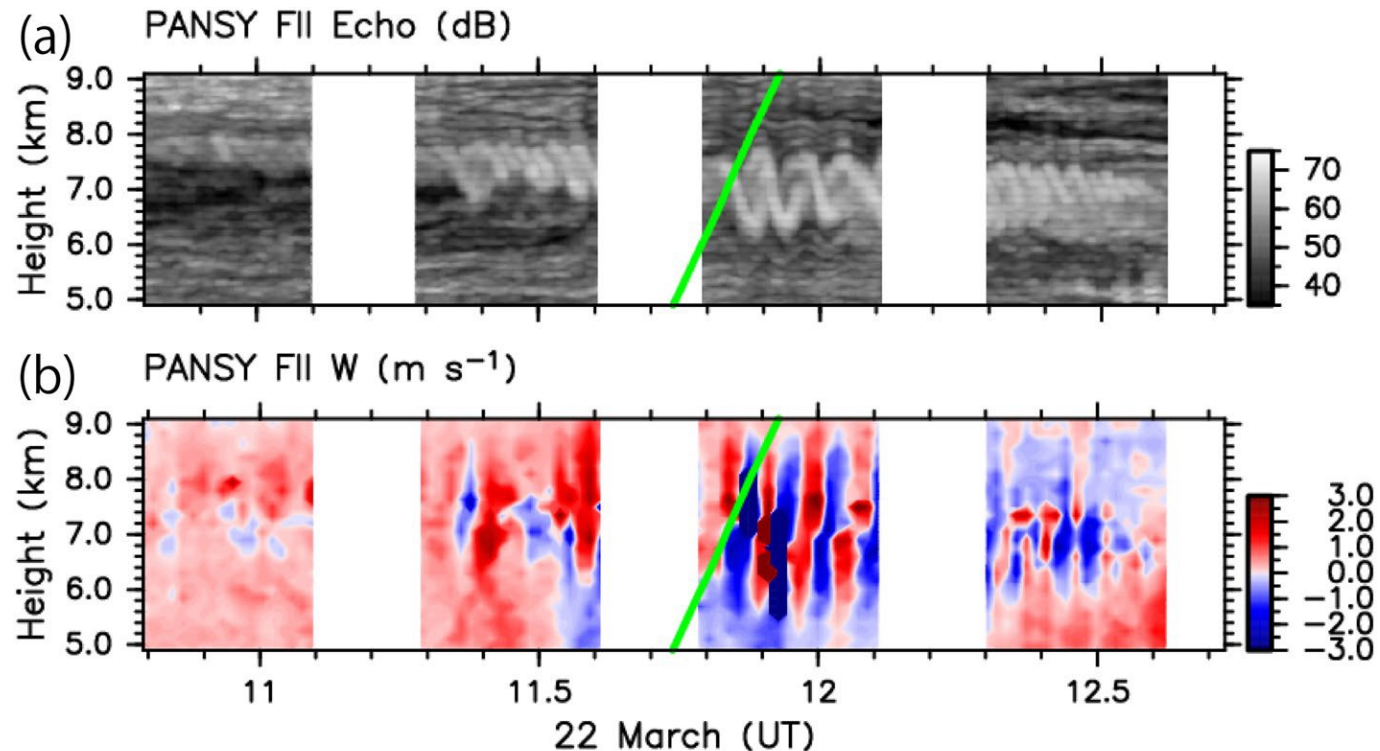


Strong, sporadic turbulence events near the tropopause level

Strong surface winds associated with synoptic-scale disturbances

# K-H billows observed by PANSY radar

- Minamihara et al. (2023)
  - Kelvin-Helmholtz (K-H) billow using Frequency-domain Interferometric Imaging (FII) techniques
    - FII mode :  $dt \sim 13$  s,  $dz \sim 9.4$  m
    - Standard mode :  $dt \sim 90$  s,  $dz \sim 150$  m
  - From 10-day observation period, about 70 K-H billows are detected



# **An approach of estimation of turbulent energy dissipation rates from radiosonde observations based on machine learning**

Preliminary results

# Motivation

## Radar-based estimates:

Traditionally used  
Fine temporal resolution

Limitation:  
Limited availability of radar  
observation sites

## Radiosonde-based estimates:

Extensive radiosonde  
observation network

Limitation:  
Uncertainty of  $\varepsilon$  estimates

## Syowa Station, Antarctic

Numerous simultaneous  
observations of a VHF radar and  
radiosondes since October 2015

## Purpose of the study:

Estimate  $f(\mathbf{x}_{\text{sonde}})$  s.t.

$f(u_{\text{sonde}}, v_{\text{sonde}}, \theta_{\text{sonde}}) = \varepsilon_{\text{radar}}$   
using **machine learning(ML) approach**  
based on a dataset of simultaneous  
observations of a radar and  
radiosondes.

In this presentation,  
the preliminary results of ML-based  
approach for estimating  $\varepsilon$  is shown.

So far, we have NOT addressed

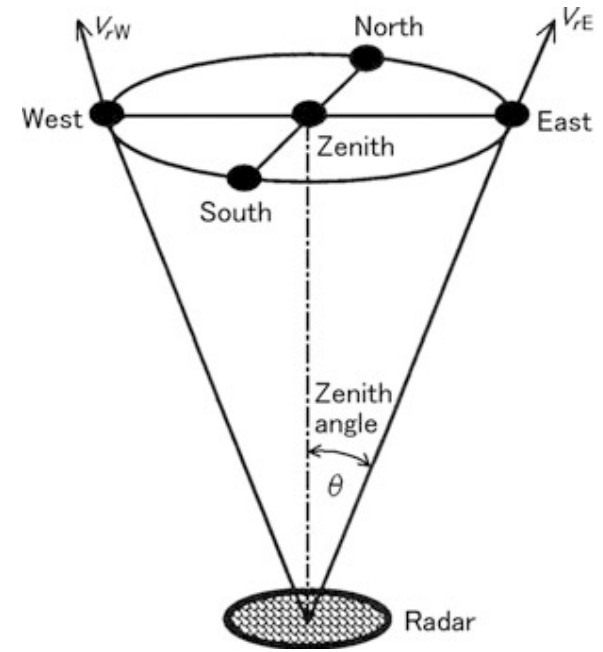
- Applicability to other sites (i.e., mid latitudes & tropics)
- Effect of processes related to latent heat release

# Data: Radiosondes

## Operational radiosonde observations at Syowa Station

- Meisei RS-06G/RS-11G, twice a day (00UT, 12UT)
- Processed data (NOT Raw data)
- $u$ ,  $v$ , &  $\theta$ 
  - Relative humidity (RH) is not used in the following results.
- From Oct. 2015 to Dec. 2022
- Interpolated at a constant vertical interval of 5 m from data with  $\Delta t = 1$  sec.
- Restricted observations where horizontal distance between the radar and radiosondes  $< 25$  km

# Data: PANSY radar



Time interval: ~200 s  
Range resolution: 150 m

4 oblique beams with a zenith angle of  $10^\circ$   
are used to avoid the effect of specular reflection.

## Estimation of $\varepsilon$ from radar spectral width

- $\sigma_{\text{obs}}^2 = \sigma_{\text{T}}^2 + \sigma_{\text{B}}^2 + \sigma_{\text{S}}^2 + \sigma_{\text{W}}^2$  ( $\sigma_{\text{T}}^2$ : Turbulence;  $\sigma_{\text{B}}^2$ : Beam broadening;  $\sigma_{\text{S}}^2$ : Shear broadening;  $\sigma_{\text{W}}^2$ : Time broadening)  
Beam broadening  $\sigma_{\text{B}}^2$  is removed using an algorithm developed by Nishimura et al. (2020)

- $\varepsilon = 0.46 N w_{\text{std}}^2$  ( $w_{\text{std}}^2 = \frac{\sigma_{\text{T}}^2}{2 \ln 2}$ ) (Sato & Woodman 1982; Hocking, 1983)

In the following,  $w_{\text{std}}$  averaged over 4 oblique beams are shown.

$w_{\text{std}}$  (standard deviation of vertical wind fluctuations due to turbulence) is used for the ML-based approach



# Training dataset: $\{\widehat{w}_{\text{std}}(z_i)\}, \left\{ [\hat{u}(z), \hat{v}(z), \theta'(z)]_{z_i-1.5\text{km}}^{z_i+1.5\text{km}} \right\}$

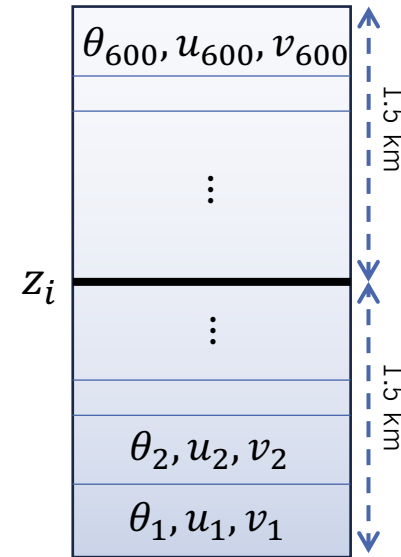
## Radar: $w_{\text{std}}(z_i)$

- Temporal average: until 1 h after radiosonde launch
- Yeo-Johnson transformation

$$\widehat{w}_{\text{std}} = \begin{cases} ((w_{\text{std}} + 1)^\lambda - 1) / \lambda & \text{if } \lambda \neq 0, w_{\text{std}} \geq 0 \\ \ln(w_{\text{std}} + 1) & \text{if } \lambda = 0, w_{\text{std}} \geq 0 \\ -((-w_{\text{std}} + 1)^{2-\lambda} - 1) / (2 - \lambda) & \text{if } \lambda \neq 0, w_{\text{std}} < 0 \\ -\ln(-w_{\text{std}} + 1) & \text{if } \lambda = 0, w_{\text{std}} < 0 \end{cases}$$

For making the  $w_{\text{std}}$  distribution approximate normal distribution

## Radiosondes: $u, v, \theta$ ( $z = [z_i - 1.5\text{km}, z_i + 1.5\text{km}]$ )



- Data dimension: 3 km [600 x ( $u, v, \theta$ )]
- $\theta' = \theta - \bar{\theta}$   
( $\bar{\theta}$ : Vertical average over 3 km)
- $(\hat{u}, \hat{v})^T = \mathbf{R}(u, v)^T$   

$$\mathbf{R} = \begin{pmatrix} \cos \varphi & -\sin \varphi \\ \sin \varphi & \cos \varphi \end{pmatrix} \quad (0 < \varphi < 2\pi)$$

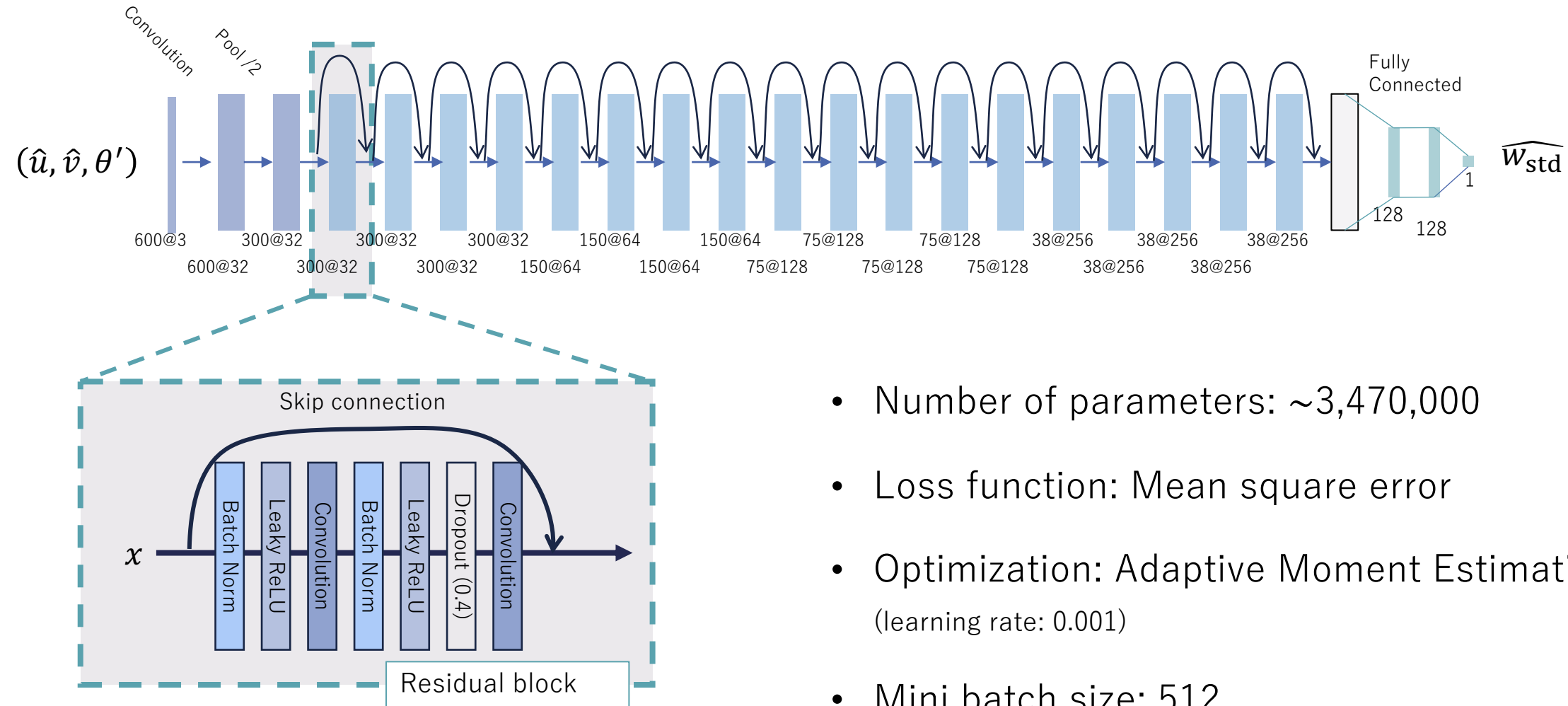
Rotation angle  $\varphi$  is given randomly for each profile
- ✓ Data augmentation technique for improving the ML model's generalization ability

**Training data:** October 2015 - December 2021

**Validation data:** January - December 2022

Validation data is NOT used during the training process but is utilized for the validation purposes.

# Machine Learning (ML) model

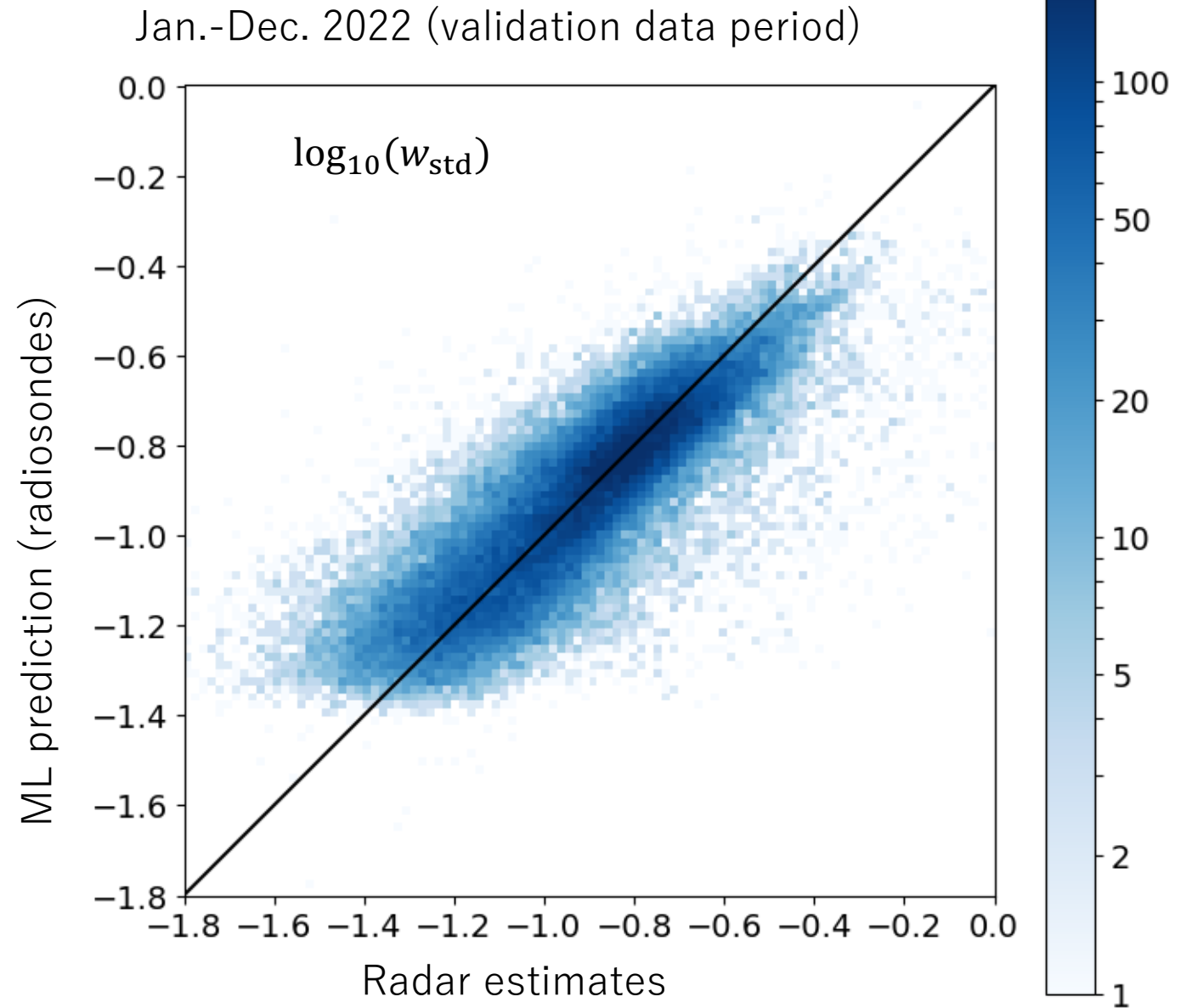


- Number of parameters:  $\sim 3,470,000$
- Loss function: Mean square error
- Optimization: Adaptive Moment Estimation (learning rate: 0.001)
- Mini batch size: 512

cf. Residual Neural Network (ResNet; He et al., 2015)

ResNet enables the model with hundreds of layers to train easily and approach better accuracy when the model is going deeper

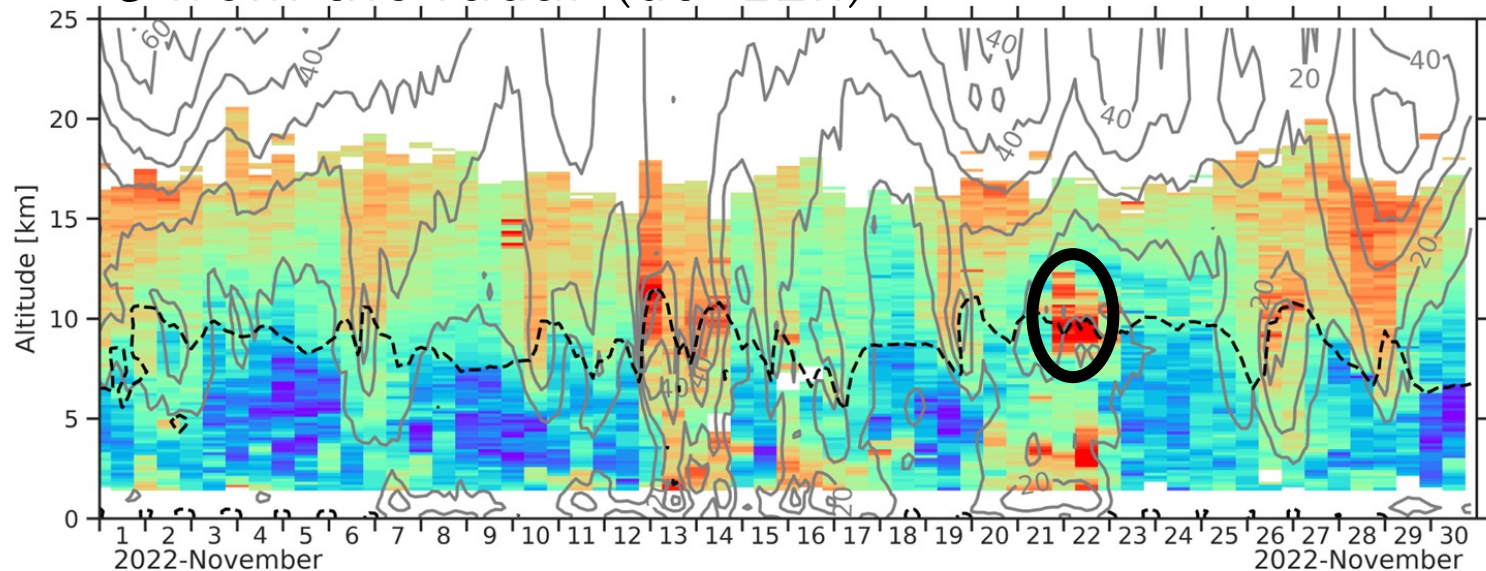
# Results: Radar observation vs. ML prediction



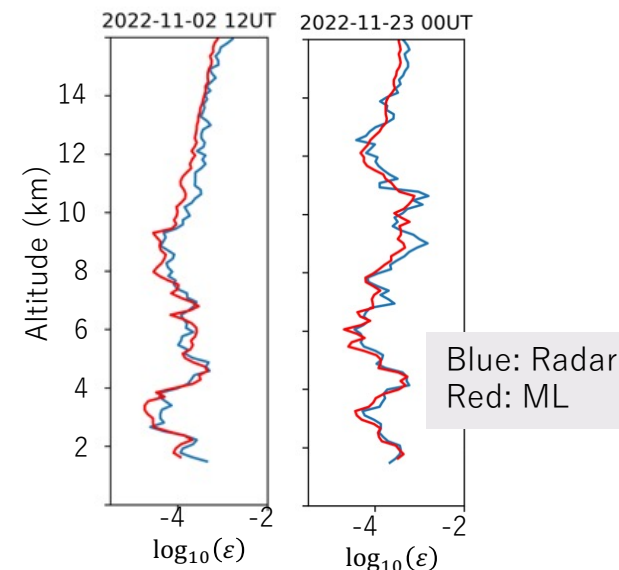
NOTE: Observations in 2022 are not used in the training process

# Results: Time-height section of $\varepsilon$ in November 2022

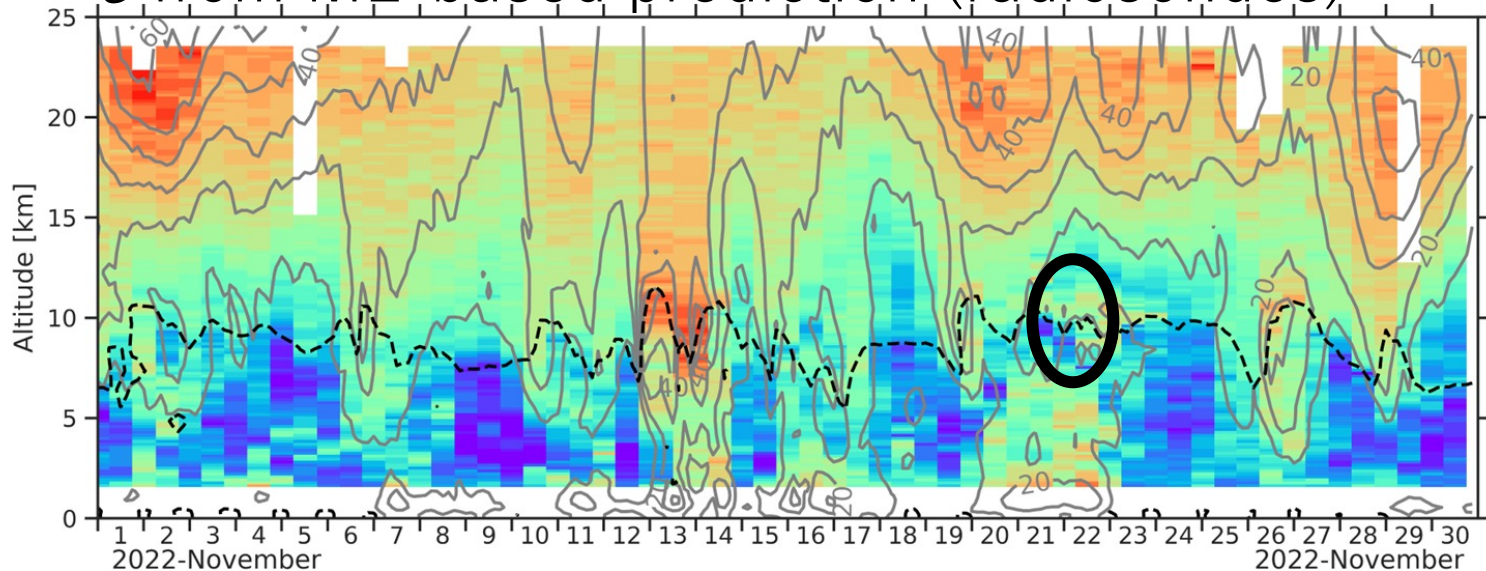
$\varepsilon$  from the radar (dt=12h)



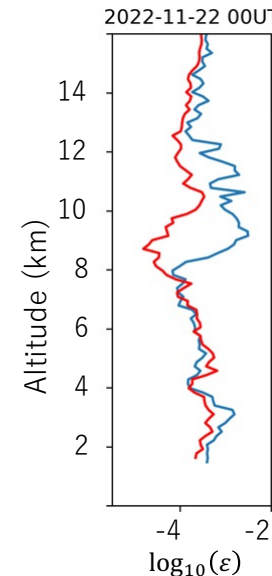
Successful case s



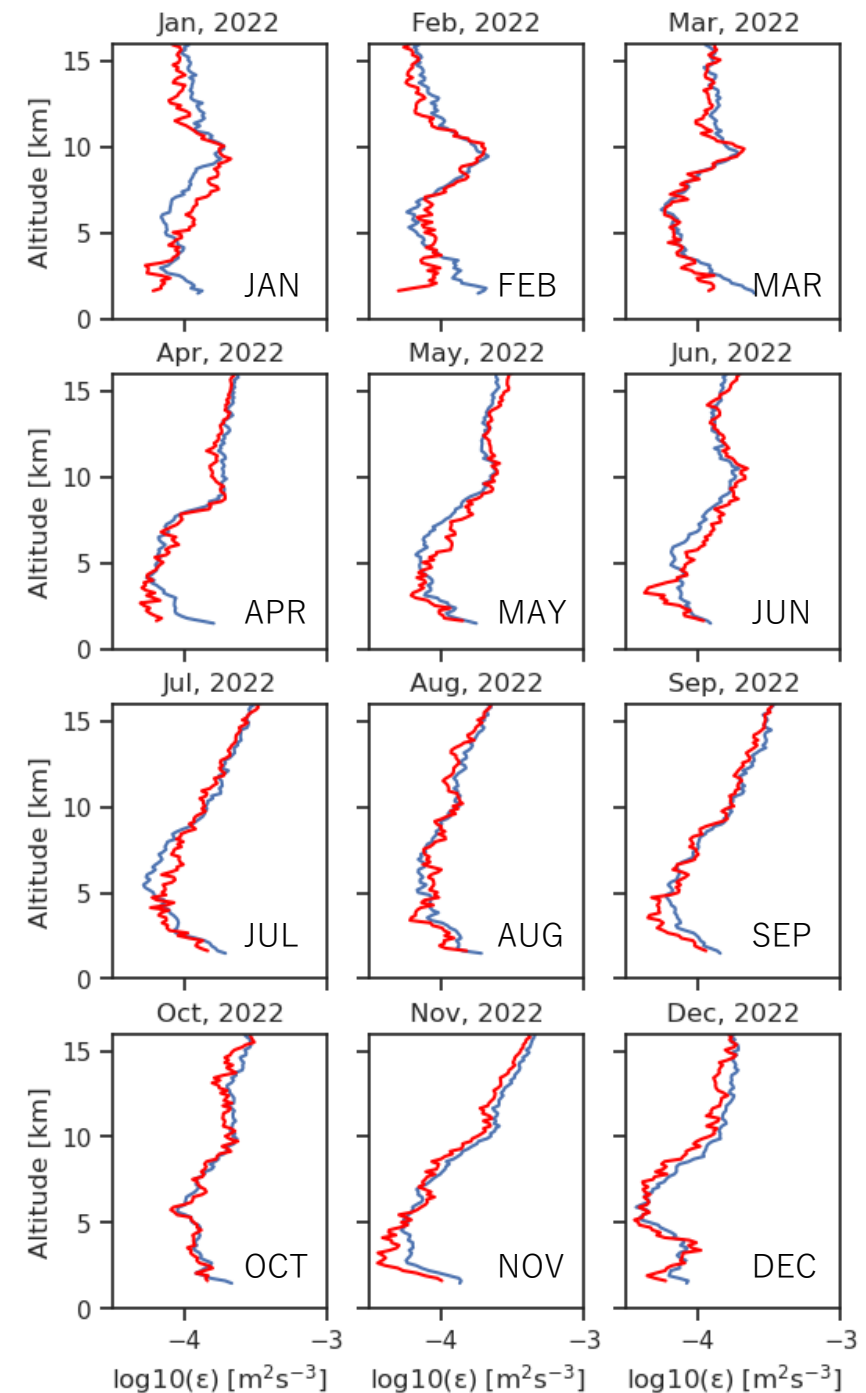
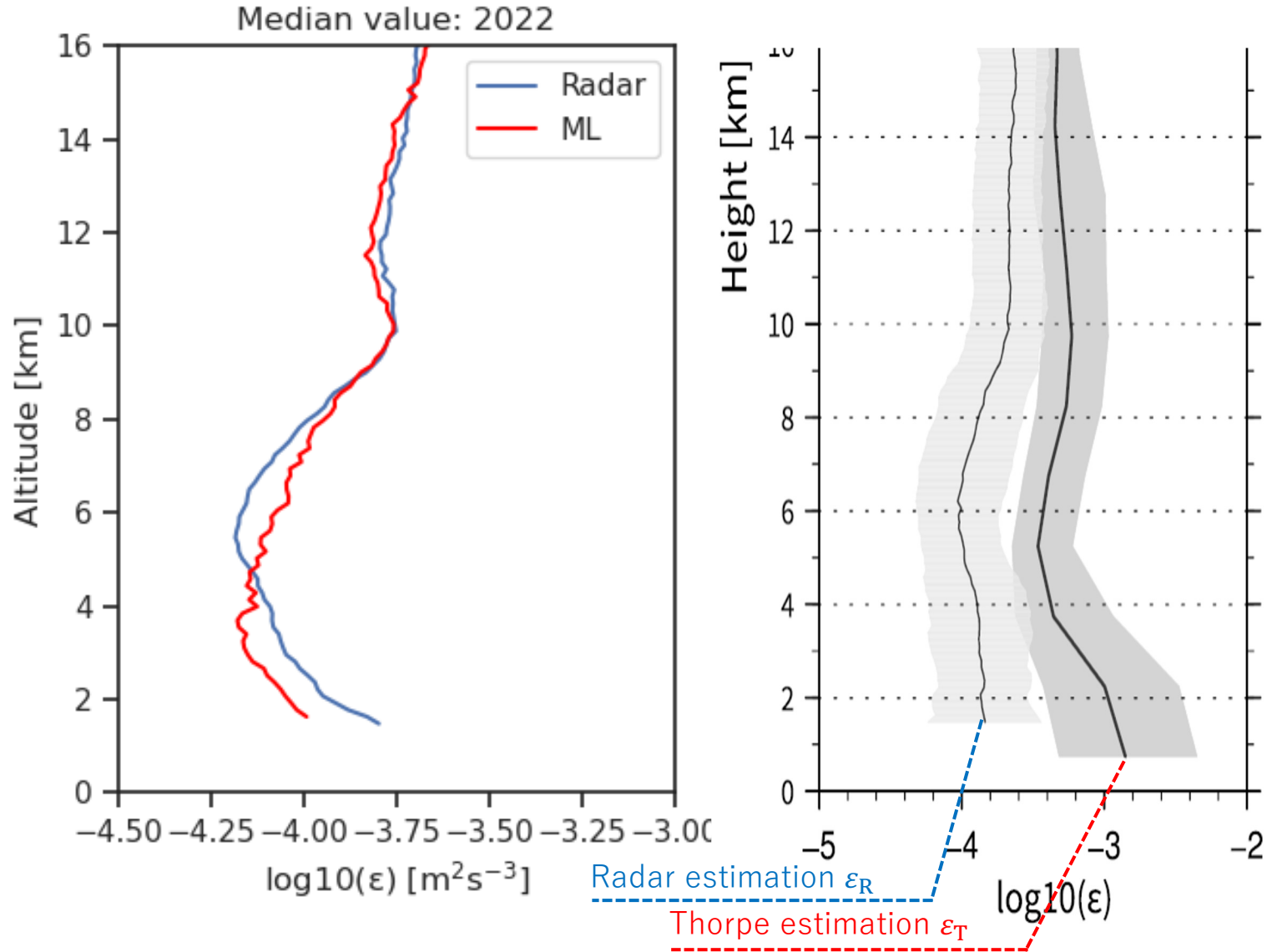
$\varepsilon$  from ML-based prediction (radiosondes)



Missing large  $\varepsilon$



# Results: Annual mean & monthly mean $\epsilon$ in 2022





# Summary

## 1. Turbulent Energy Dissipation Rates ( $\varepsilon$ ) Comparison:

- Used VHF radar data at Syowa Station, Antarctic
- Compared with radiosonde-based estimation via Thorpe method

The ratio of radar-based  $\varepsilon$  to Thorpe-based  $\varepsilon$  is significantly small in the altitude range of 1.5–9 km compared to over 11 km.

## 2. Machine Learning (ML) Approach for Estimating $\varepsilon$

- Developed a ML-based algorithm to estimate  $\varepsilon$  from the radiosonde observations.

ML-based estimates closely resemble those obtained from radar observations

Limitation: The current algorithm fails to detect strong, sporadic turbulence events.

Applicability to other observation sites?



# Prospects

## Toward global mapping of turbulent energy dissipation rates

- Improvement the ML-based method
  - Detection of strong turbulence that appears sporadically
  - Validation of the ML-based method using other radars at different latitudes (e.g., MU radar @ Shigaraki, Japan [34.5°N])
    - Generalization ability
    - Assessment of influence of condensation process in the troposphere
- Investigation of which features the ML model is actually looking at to make predictions
- Comparison with other estimation based on observations from aircraft, UAV, special balloon, etc.



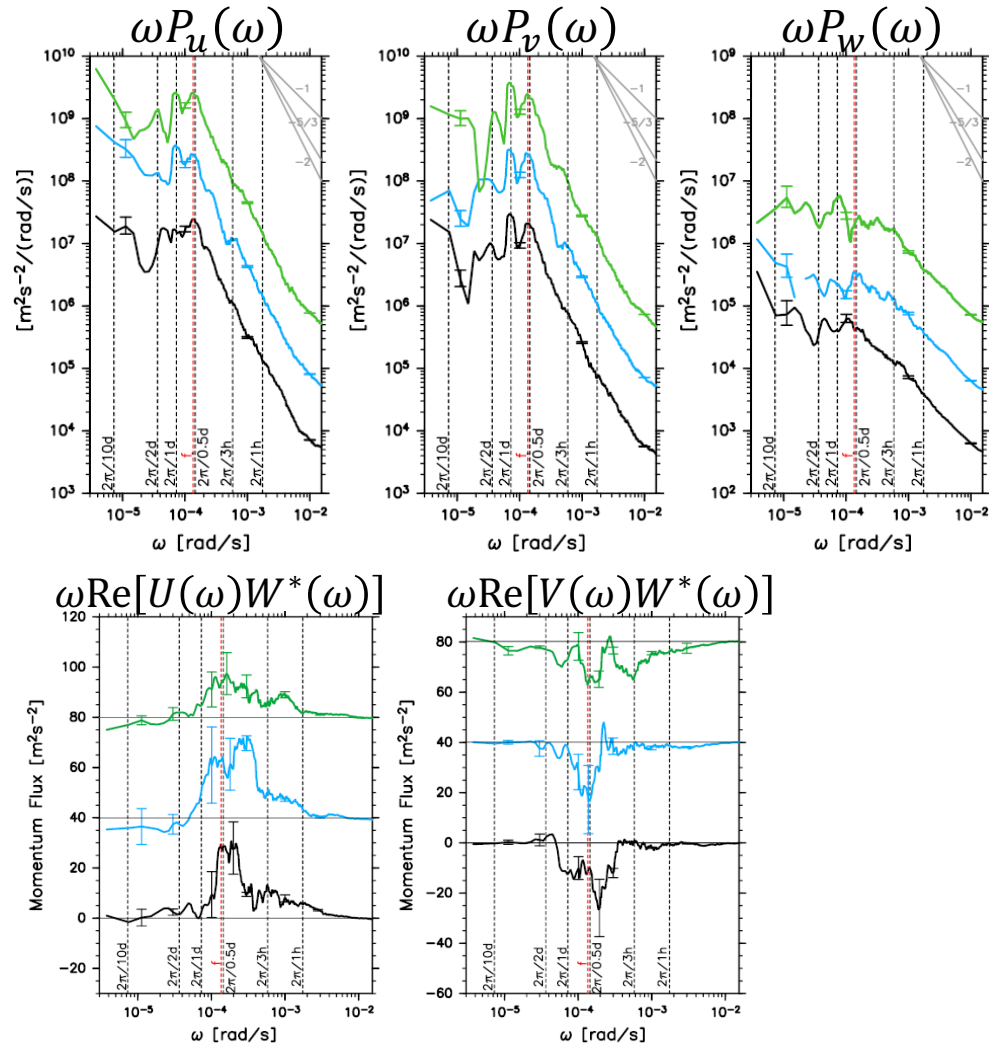
# Prospects

## Toward global mapping of turbulent energy dissipation rates

- Sensitivity test of training data
  - What kind of data (e.g., vertical resolution,  $\theta$  only, wind only, etc.) are necessary for estimation of  $\varepsilon$ ?
- Another estimation model of radar-based  $\varepsilon$  (e.g., Luce et al., 2023)
- Application to radiosonde network
  - GRUAN (Global Reference Upper-Air Network) data
    - Well-calibrated data, 30-40 sites
  - BUFR?
    - >1000 sites
    - Various sensors, software versions, vertical resolutions ...

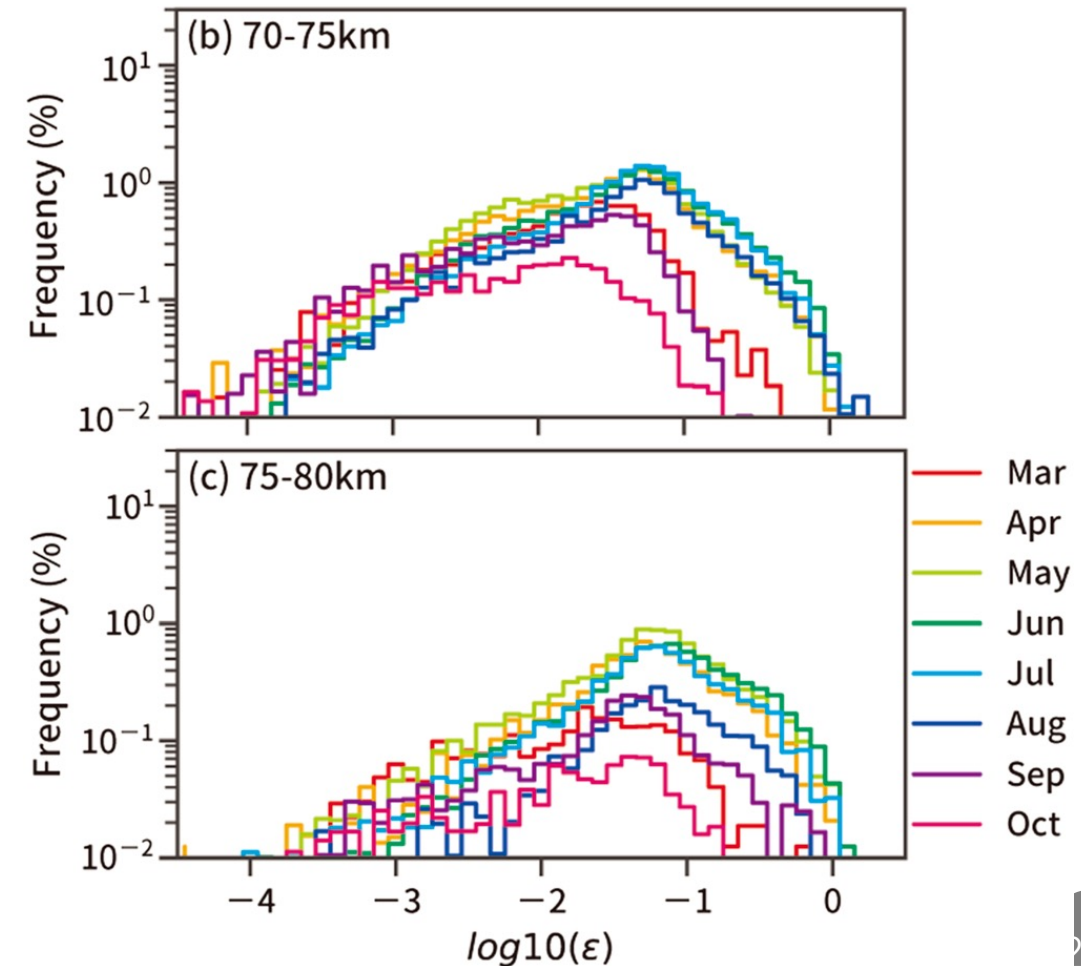
# GW and turbulence in the mesosphere by the PANSY radar

Sato et al. (2017) : Spectra of winds and momentum fluxes in the summer mesosphere



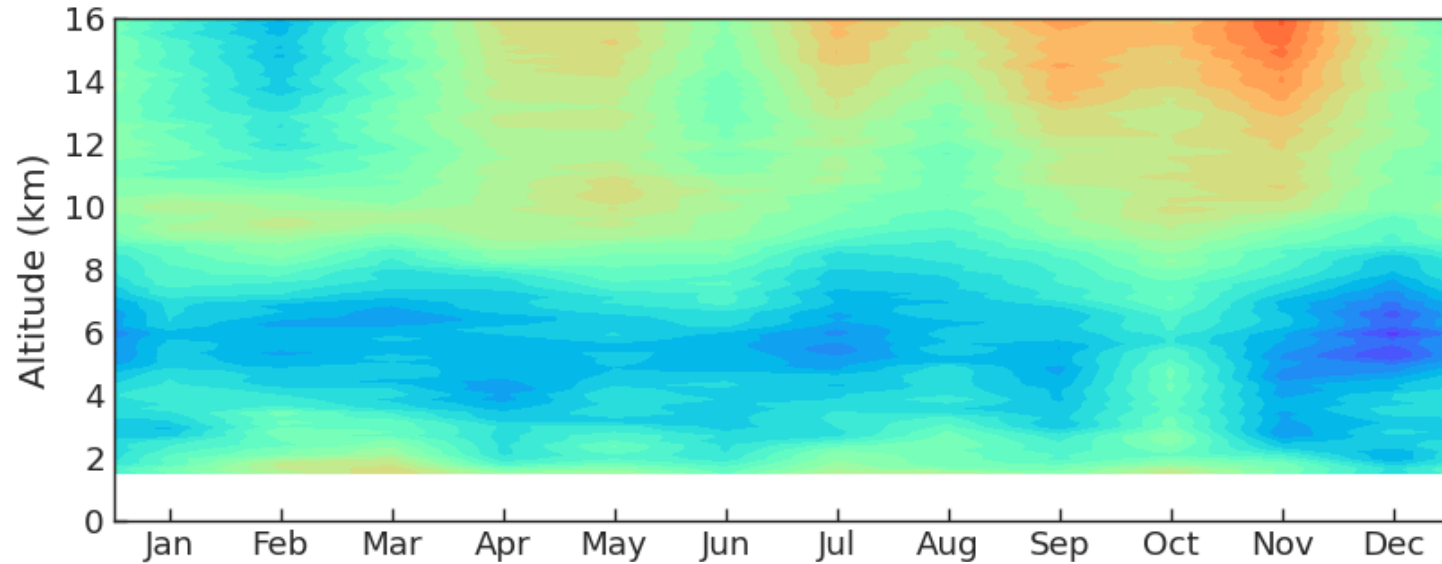
Kohma et al. (2020; 2021) :

Seasonal variation of mesospheric  $\varepsilon$

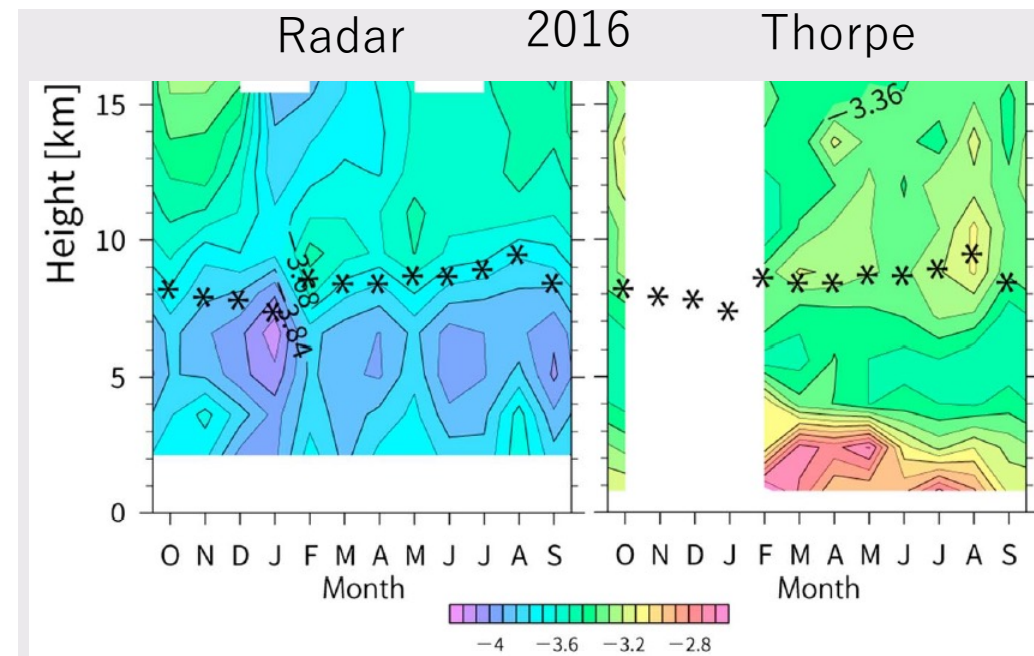
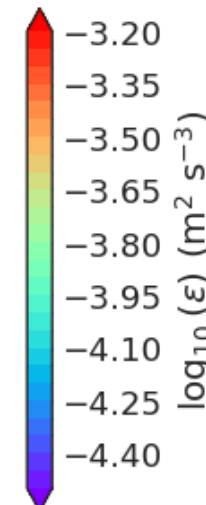
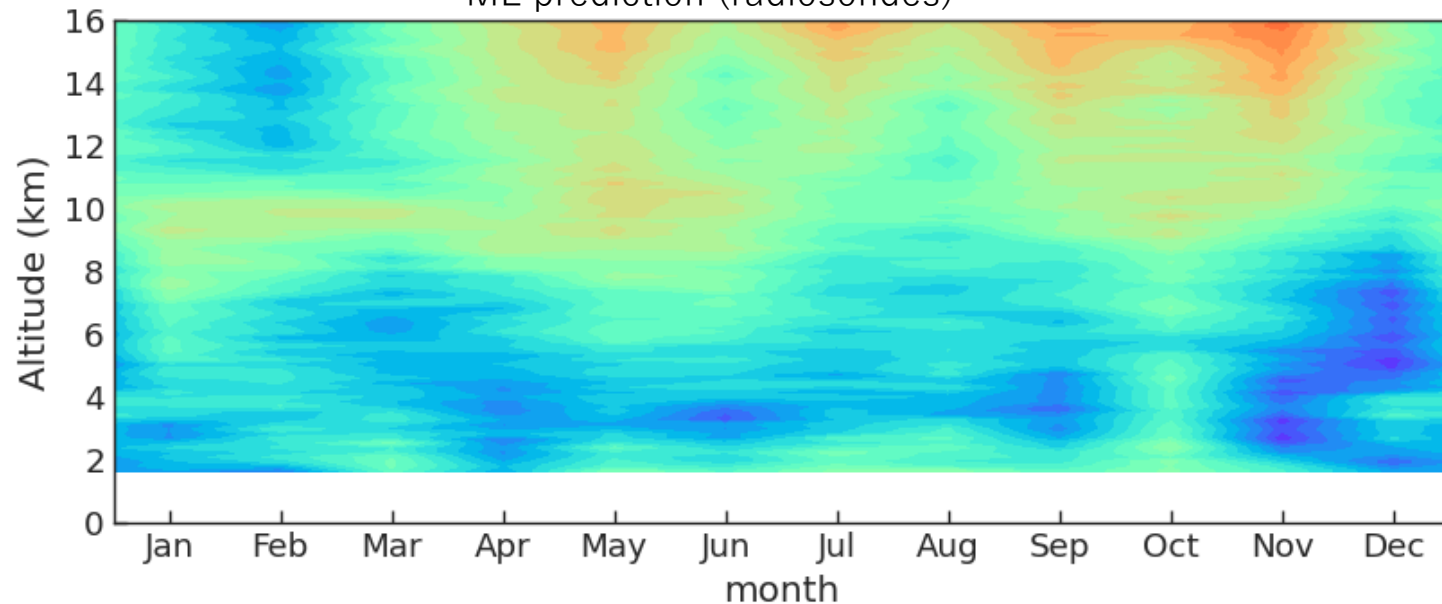


# Results: Seasonal variation of $\varepsilon$ in 2022

Radar  $\varepsilon$  (2022)

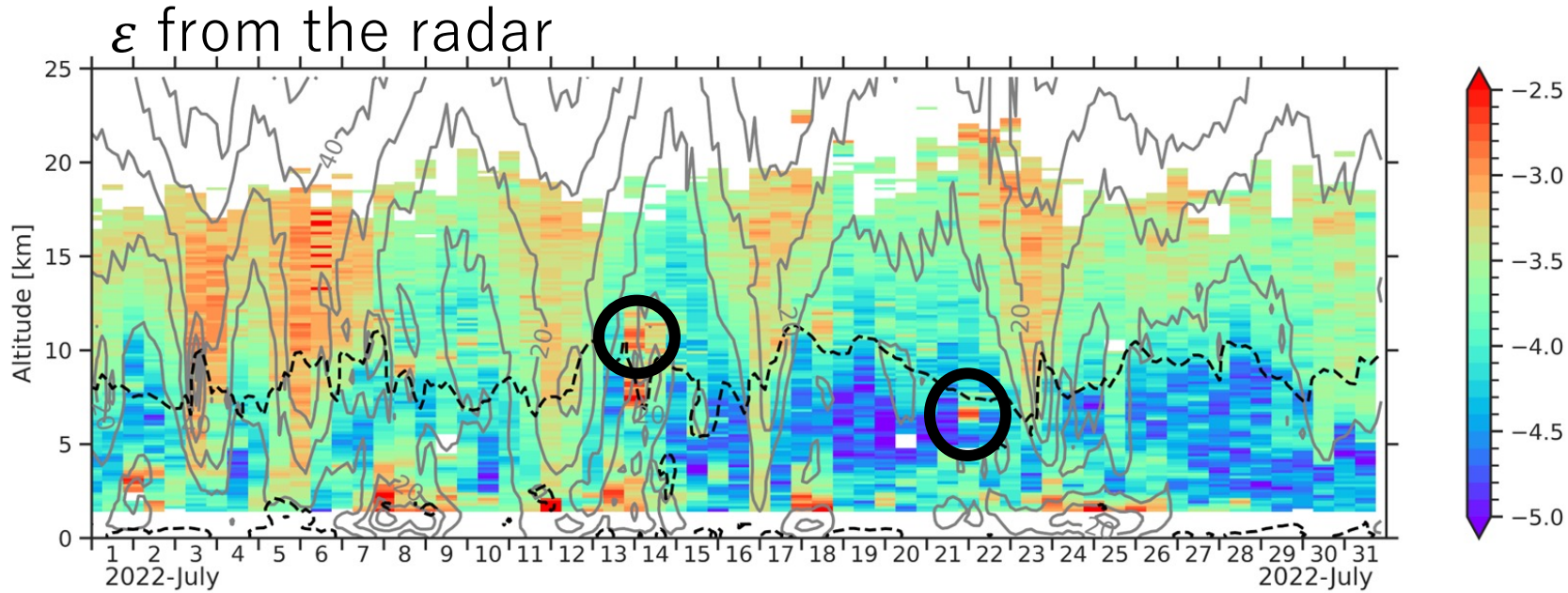


ML prediction (radiosondes)

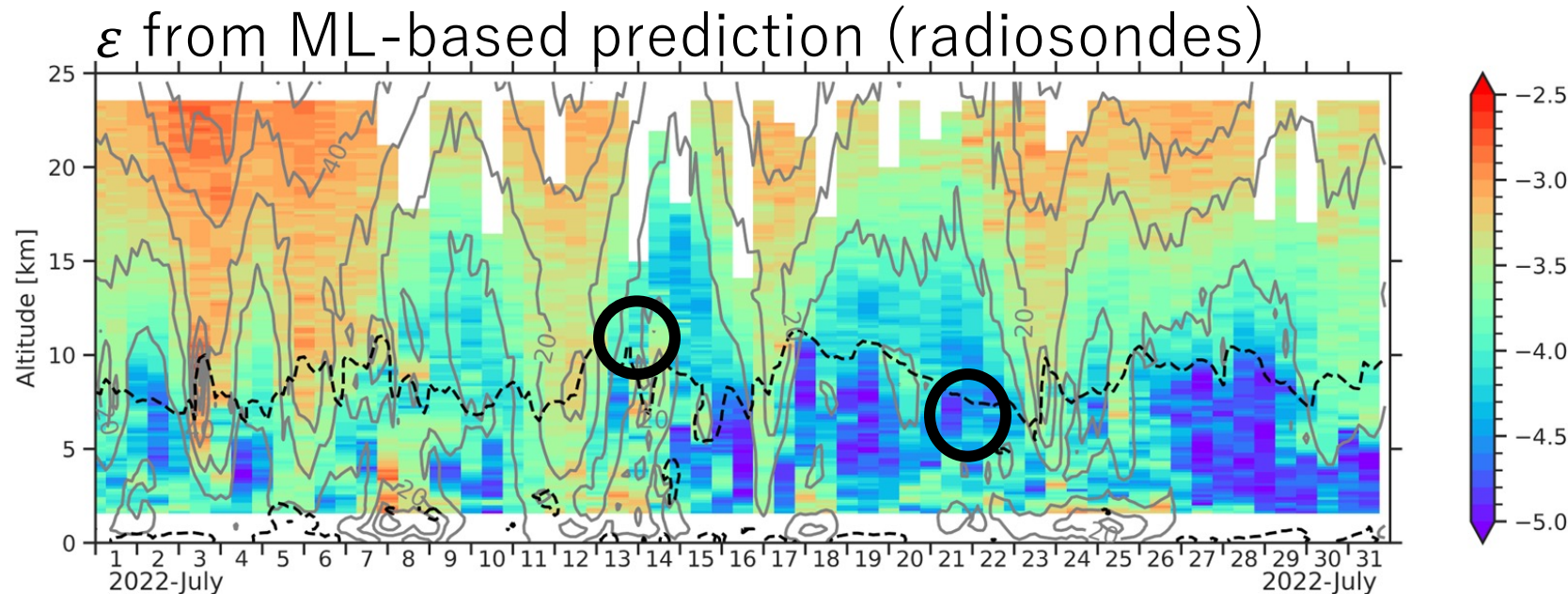
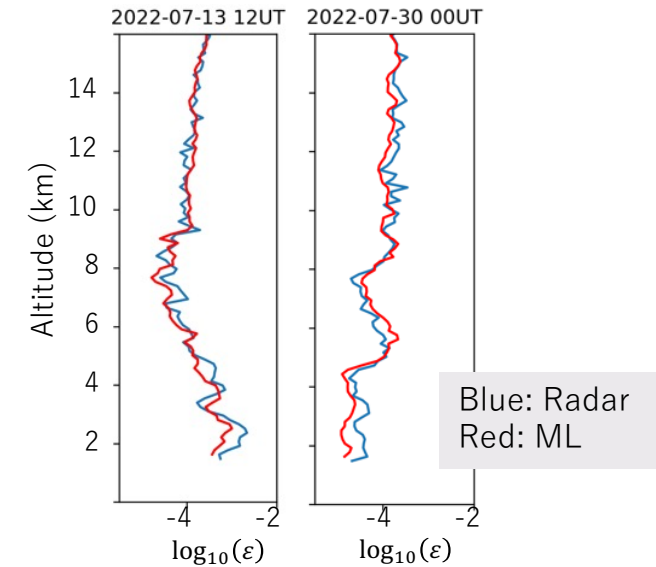




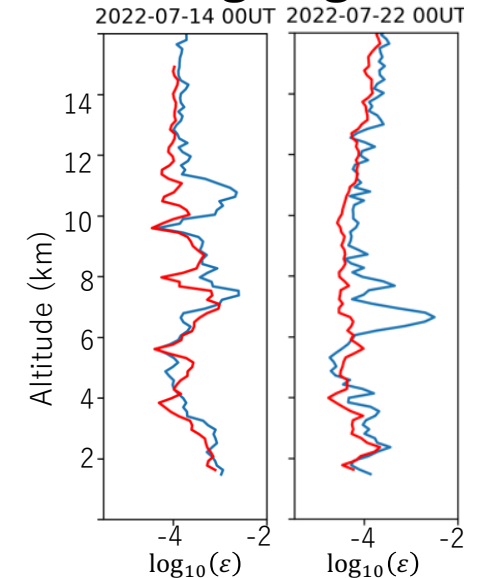
# Results: Time-height section of $\varepsilon$ in July 2022



## Successful case s

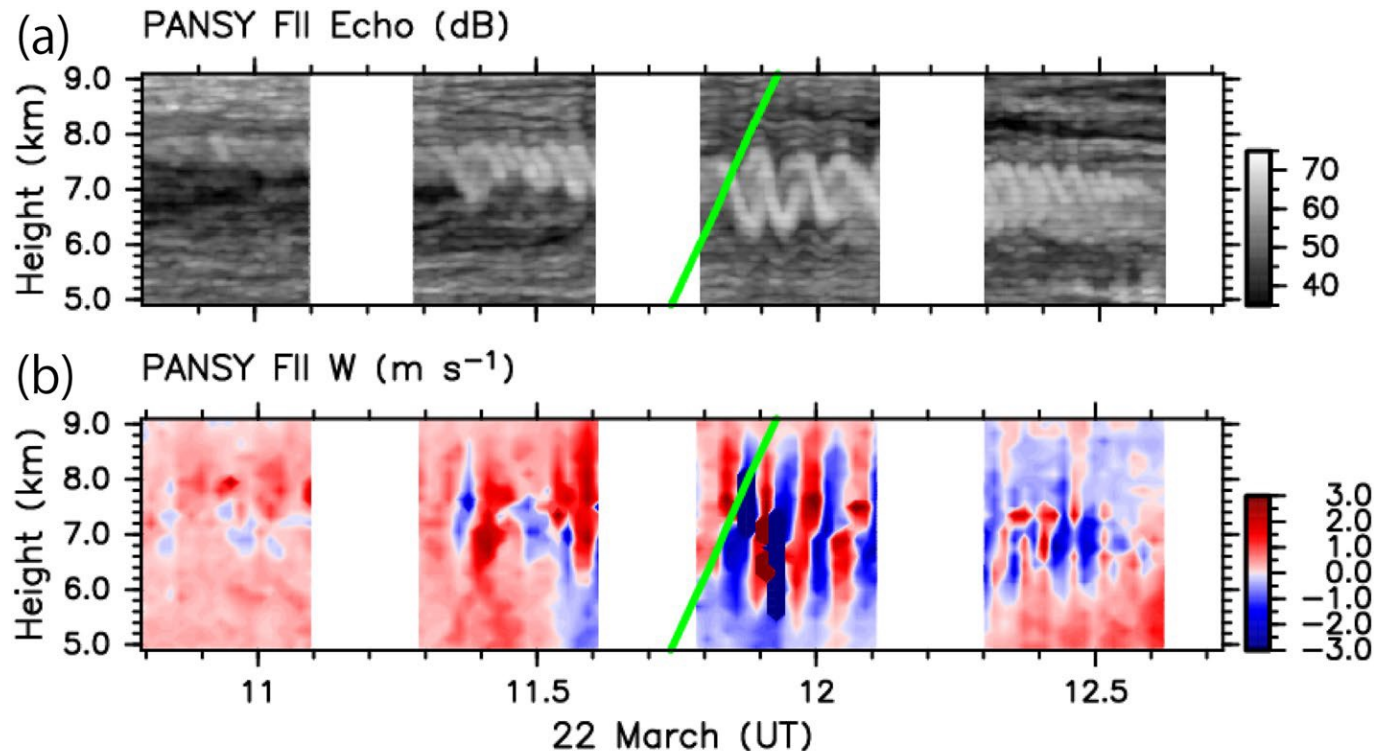


## Missing large $\varepsilon$



# K-H billows observed by PANSY radar

- Minamihara et al. (2023)
  - K-H billow observations using Frequency-domain Interferometric Imaging (FII) techniques
    - FII mode :  $dt \sim 13$  s,  $dz \sim 9.4$  m
    - Standard mode :  $dt \sim 90$  s,  $dz \sim 150$  m
  - From 10-day continuous observation, 73 K-H billows are detected

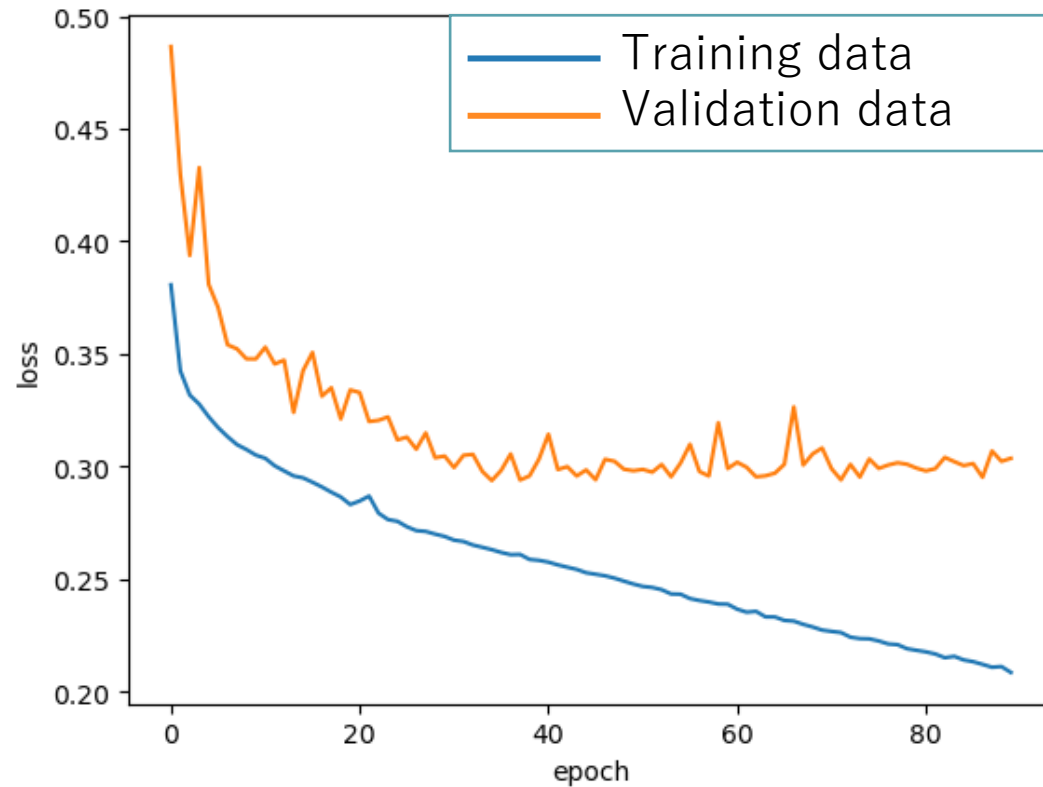


Characteristics of KH billows	PANSY		MU radar <sup>a</sup>	
	Mean	Median	Mean	Median
Depth [m]	559	500	620	550
Wave period [s]	177.6	162.9	90	78
Horizontal wavelength [m]	2,019	1,837	2,600	2,700
Aspect ratio	0.342	0.271	0.22	–
$\log_{10} \epsilon_{\max}$ [ $\text{m W kg}^{-1}$ ]	-0.19	-0.22	-0.28	-0.17
Vertical shear [ $\text{m s}^{-1} \text{ km}^{-1}$ ]	13.1	12.3	21.4	23.4
Number of samples	73		217	

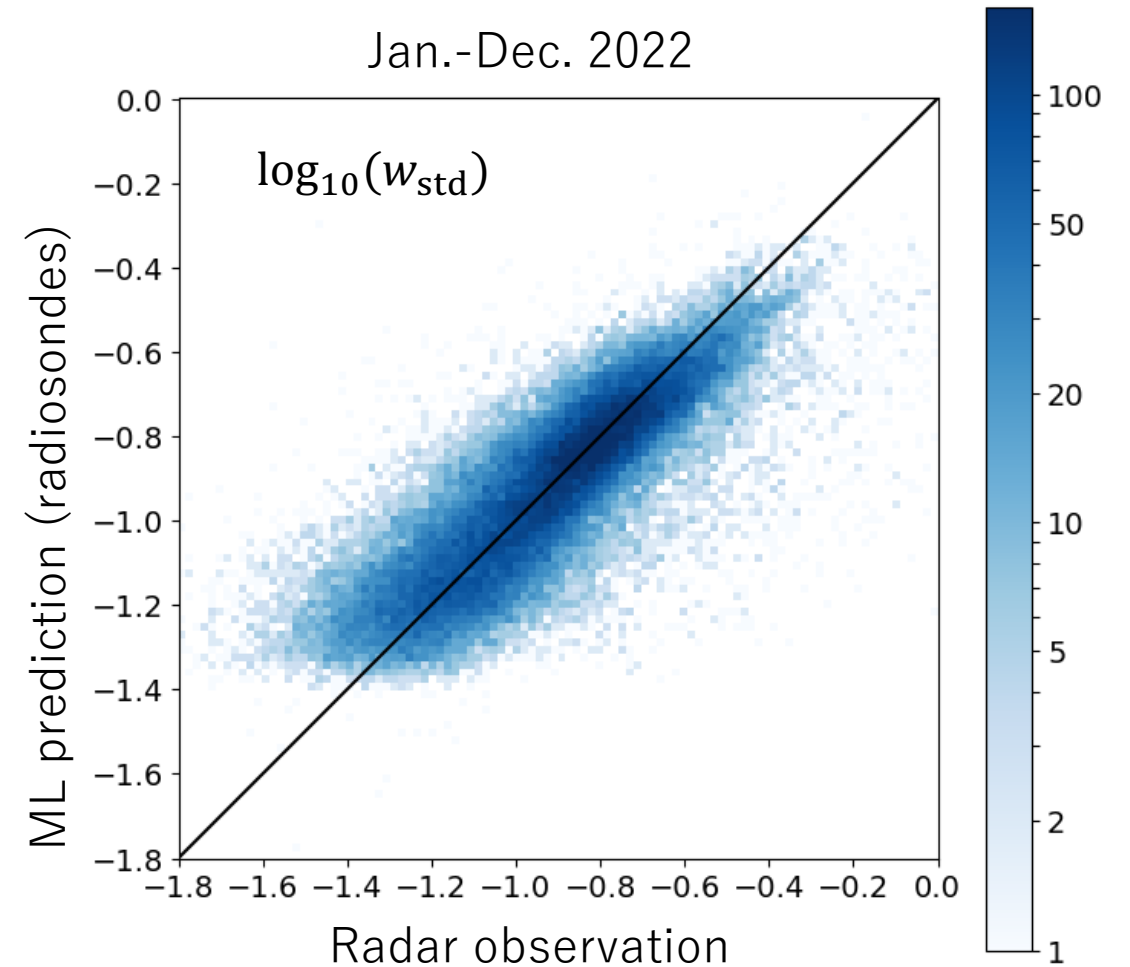
<sup>a</sup>Fukao et al. (2011).

# Results: ML training process and Validation

Loss function (Mean square error)



Radar observation vs. ML prediction



NOTE: Observations in 2022 are not used in the training process

# Estimation of the energy dissipation rate using spectral width of backscatter echo of atmospheric radar observations

(Sato and Woodman, 1982; Hocking 1983)

Observed Doppler spectral width ( $\sigma_{\text{obs}}$ ) of the echo is written as

$$\sigma_{\text{obs}}^2 = \sigma_T^2 + \sigma_B^2 + \sigma_S^2 + \sigma_W^2$$

$\sigma_T^2$ : Turbulence;  $\sigma_B^2$ : Beam broadening;  $\sigma_S^2$ : Shear broadening;  $\sigma_W^2$ : Time broadening

The turbulent velocity variance ( $w_{\text{rms}}^2$ ) is

$$w_{\text{rms}}^2 = \sigma_T^2 / (2 \ln 2)$$

Using Kolmogorov spectrum  $E(k) = C \varepsilon^{2/3} k^{-5/3}$

$$\frac{3}{2} w_{\text{rms}}^2 = \int_{k_B}^{k_b} C \varepsilon^{2/3} k^{-5/3} dk$$

and assuming  $k_B \ll k_b$

$$\varepsilon = C^{-3/2} w_{\text{rms}}^3 k_B$$

Using  $k_B = N / \sqrt{w_{\text{rms}}^2}$ ,  $C^{-3/2} \approx 0.5$ , and obs. correction

$$\varepsilon = 0.46 N w_{\text{rms}}^2$$

Note:  $k_B$  is valid for stably stratified atmosphere



# Data: Radiosondes

- Operational radiosonde observations at Syowa Station
  - Meisei RS-06G (**Raw-PTU**), on 00UT and 12UT
  - From Oct. 1, 2015 to Sep. 30, 2016
  - Nighttime data only
  - Interpolated at a constant vertical interval of 12 m from data with 1 second time resolution
  - Potential temperature profiles were reconstructed by replacing the potential temperature with the moist-conservative potential temperature in the cloudy sections (Wilson et al., 2013)
  - Procedure of selection for overturning layers (Wilson et al., 2010; 2011)
- Assuming that  $L_T = L_O$  (i.e.,  $c = 1$ ),  $\varepsilon_T = L_T^2 N^{*3}$ ,

where  $N^* \equiv \left(\frac{g}{\theta} \frac{\theta_{rms}}{L_T}\right)^{1/2}$  (Bulk buoyancy frequency; Smyth et al., 2001)

