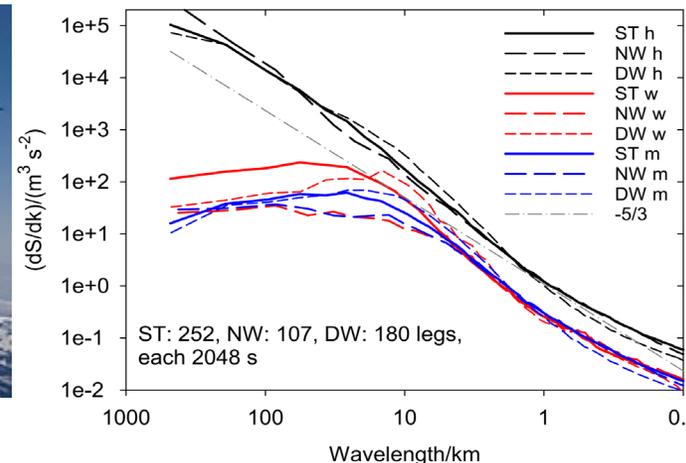




DLR + partners HALO

NSF-NCAR Gulfstream V



3 campaigns

h: horizontal

w: vertical

m: model

b: body motions

spectra +  
dissipation rates

# Measurements of High-Altitude Turbulence from Research Aircraft: Energy spectra and dissipation rates from synoptic to dissipation scales

Ulrich Schumann<sup>1)</sup>, Andreas Dörnbrack<sup>1)</sup>,  
Andreas Giez<sup>2)</sup>, Markus Rapp<sup>1)</sup>,  
Peter Bechtold<sup>3)</sup>, and Axel Seifert<sup>4)</sup>

<sup>1)</sup>Institute of Atmospheric Physics; <sup>2)</sup>Flight Experiments;  
German Aerospace Center –  
Deutsches Zentrum für Luft und Raumfahrt, DLR,  
Oberpfaffenhofen,

<sup>3)</sup> ECMWF,

<sup>4)</sup> DWD (German Weather Service)



- DW: Deep Propagating Gravity Wave Experiment (DEEPWAVE) in 2014 (Fritts et al., 2016),
- NW: North Atlantic Waveguide and Downstream Impact Experiment (NAWDEX) in 2016 (Schäfler et al., 2018)
- ST: Southern Hemisphere Transport, Dynamics, and Chemistry-Gravity Waves (SOUTHTRAC-GW) mission in 2019 (Rapp et al., 2021).



HALO (DLR)



NSF-NCAR Gulfstream V

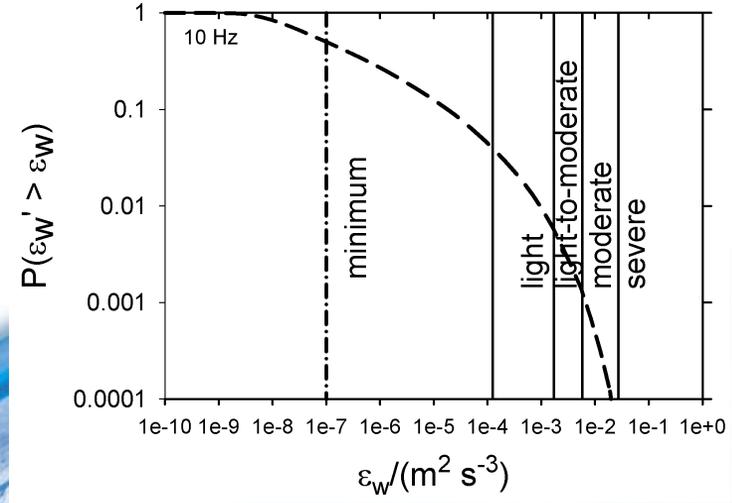
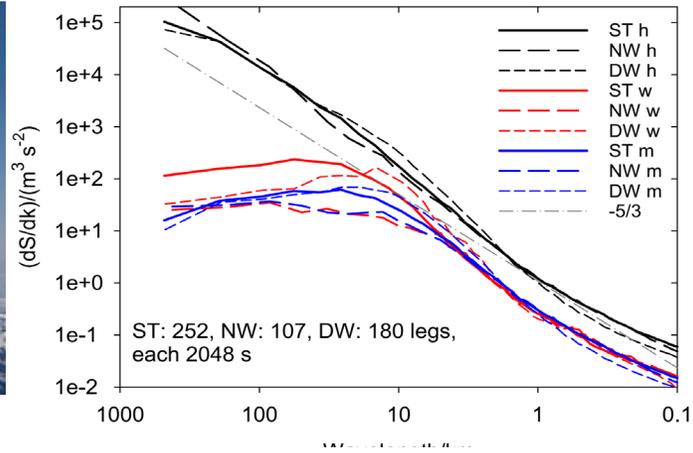
## Measurements of High-Altitude Turbulence from Research Aircraft

Ulrich Schumann<sup>1)</sup>, Andreas Dörnbrack<sup>1)</sup>,  
 Andreas Giez<sup>2)</sup>, Markus Rapp<sup>1)</sup>,  
 Peter Bechtold<sup>3)</sup>, and Axel Seifert<sup>4)</sup>

<sup>1)</sup>Institute of Atmospheric Physics; <sup>2)</sup>Flight Experiments;  
 German Aerospace Center –  
 Deutsches Zentrum für Luft und Raumfahrt, DLR,  
 Oberpfaffenhofen,

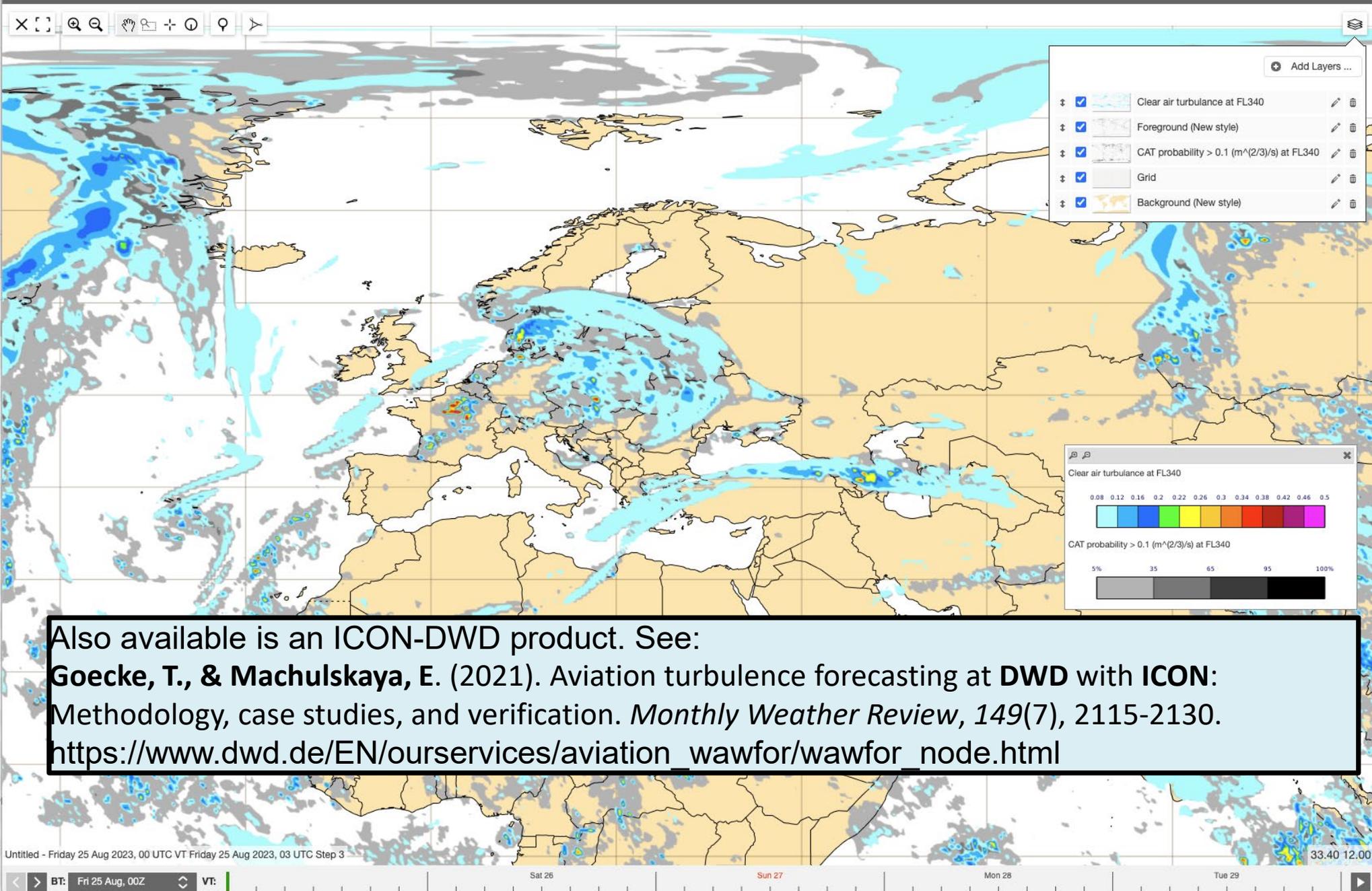
<sup>3)</sup> ECMWF,

<sup>4)</sup> DWD (German Weather Service)



Strong turbulence  
 very rare  
 Mostly wavy  
 motions  
 Anisotropic  
 Inertial subrange for  
 $L_0/\eta > 10$  requires  $\epsilon$   
 $> \epsilon_{MIN}$   
 Non-Gaussian  
 $\epsilon_w$  most accurate

Knowledge for Tomorrow



CAT at FL 340 from (brand-)new ECMWF Forecast product

provided by Peter Bechtold

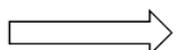
New web product of Cihan Sahin, ECMWF

colors: CAT (EDR) from HRES

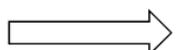
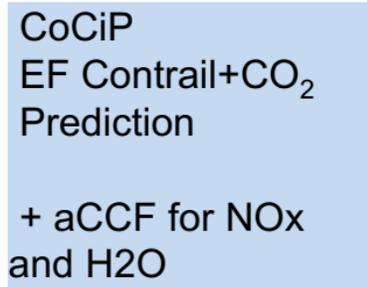
grey: Probability of CAT > 0.1 m<sup>2/3</sup> s<sup>-1</sup> in 50 member ensemble

Also available is an ICON-DWD product. See:  
**Goecke, T., & Machulskaya, E. (2021).** Aviation turbulence forecasting at **DWD** with **ICON**: Methodology, case studies, and verification. *Monthly Weather Review*, 149(7), 2115-2130.  
[https://www.dwd.de/EN/ourservices/aviation\\_wawfor/wawfor\\_node.html](https://www.dwd.de/EN/ourservices/aviation_wawfor/wawfor_node.html)

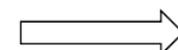
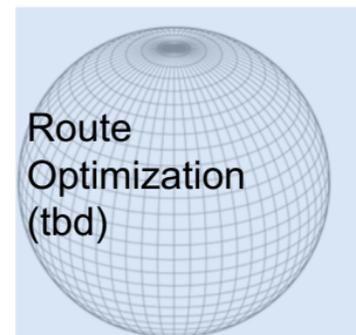
# Aviation Climate Impact Metric prediction



T, q, p  
u, v, w  
IWC,  
geopot, PV  
irradiances



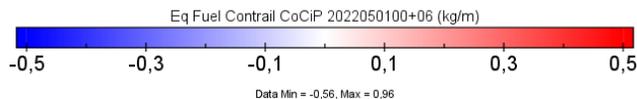
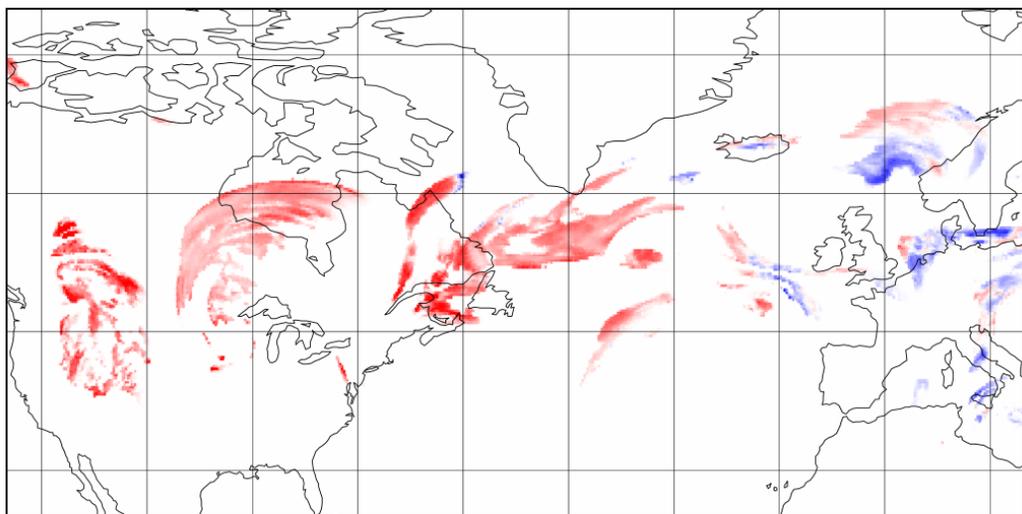
EF<sub>Contrail</sub>  
1 scalar  
field per  
aircraft type



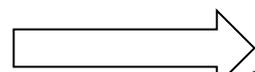
Route  
optimized for  
CO<sub>2</sub>, Contrails,  
NO<sub>x</sub>, costs,  
flight time, etc.

↓ Aircraft type (e.g., B77L), BADA3 or PS model

Eq Fuel Contrail CoCiP 2022050100+06



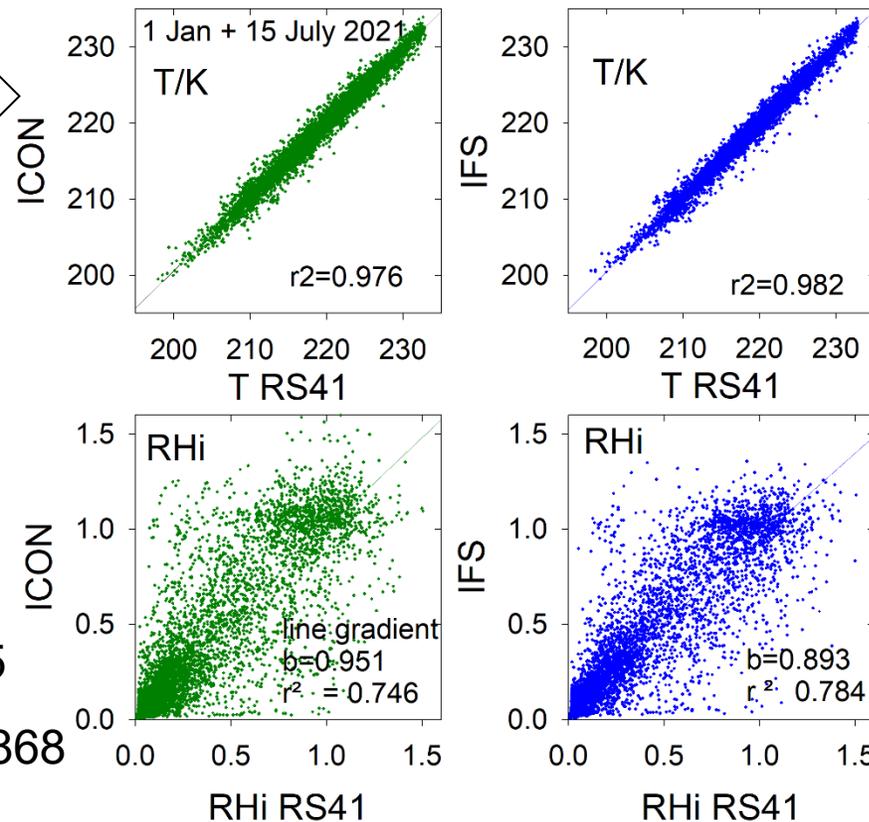
red: warming, blue: cooling contrails at FL 340



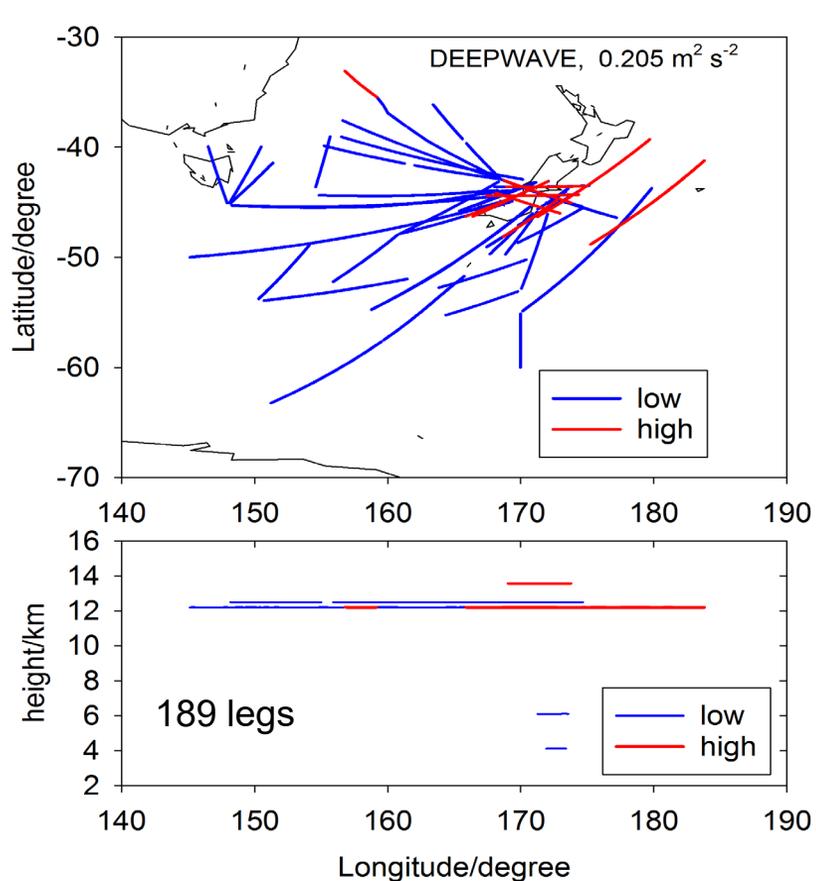
First trials of comparing IFS and new ICON (2-mom ice scheme) of Axel Seifert, DWD, to BUFR RS41 T and RHi data

T: ICON-IFS: r2=0.985

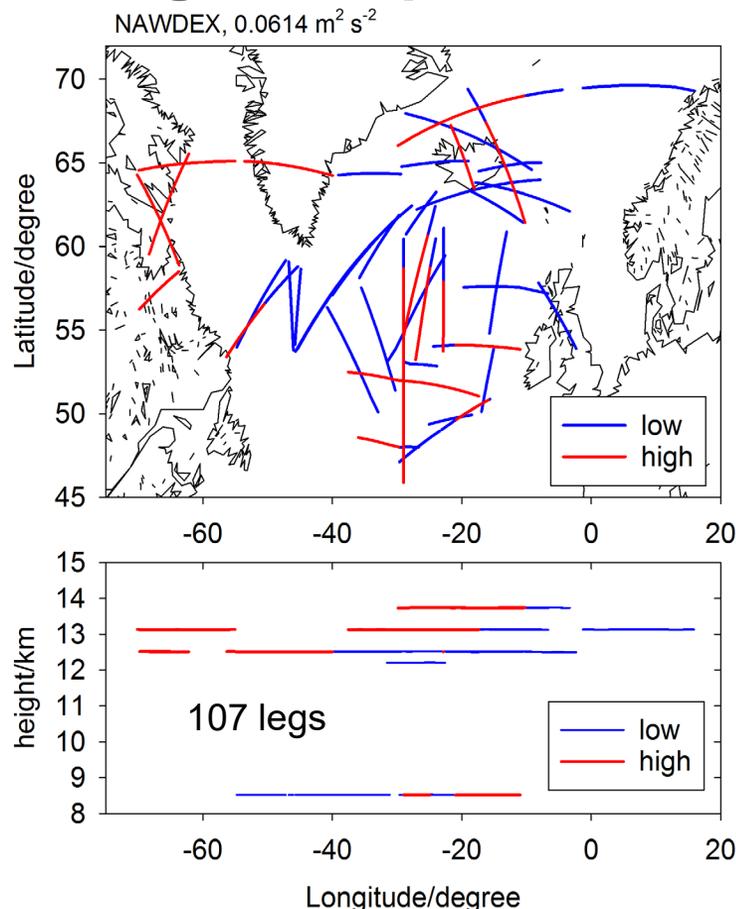
RHi: ICON-IFS, r2=0.868



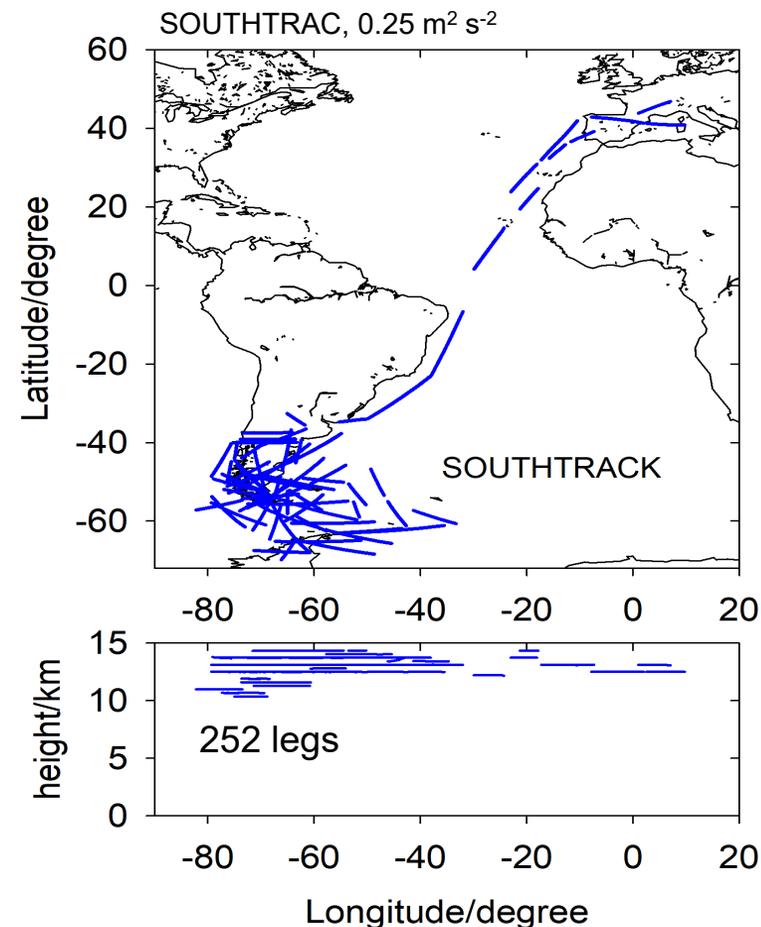
# DEEPWAVE (DW, 2014), NAWDEX (NW, 2016), SOUTHTRAC (ST, 2019) for low/high dissipation rates



Deep Propagating Gravity Wave Experiment  
Fritts et al. (BAMS, 2016)  
Data from NSF-GV (HIAPER) NCAR EOL



North Atlantic Waveguide and Downstream  
Impact Experiment  
Schäfler et al. (BAMS, 2018)  
Data from HALO, DLR-FX



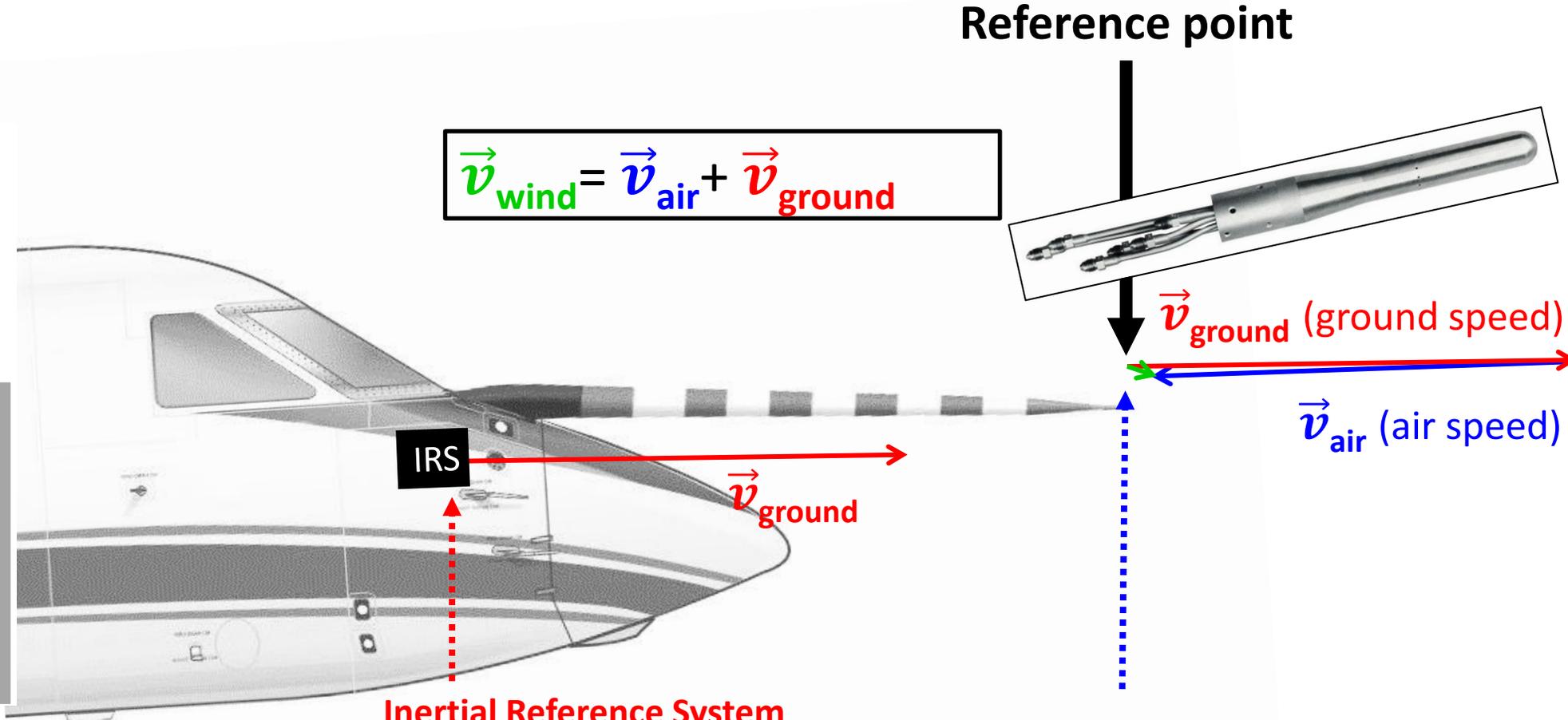
Southern Hemisphere Transport, Dynamics,  
and Chemistry-Gravity Waves  
Rapp et al. (BAMS, 2020)  
Data from HALO, DLR-FX



# Determination of the **Wind Vector** = air speed - ground speed on HALO with the BAHAMAS system (DLR-FX)



Static pressure and temperature



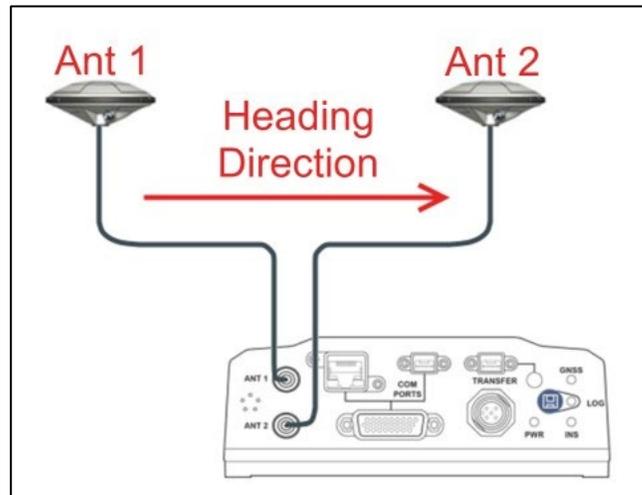
Inertial Reference System for Inertial and GNSS Navigation

Air Flow Sensor

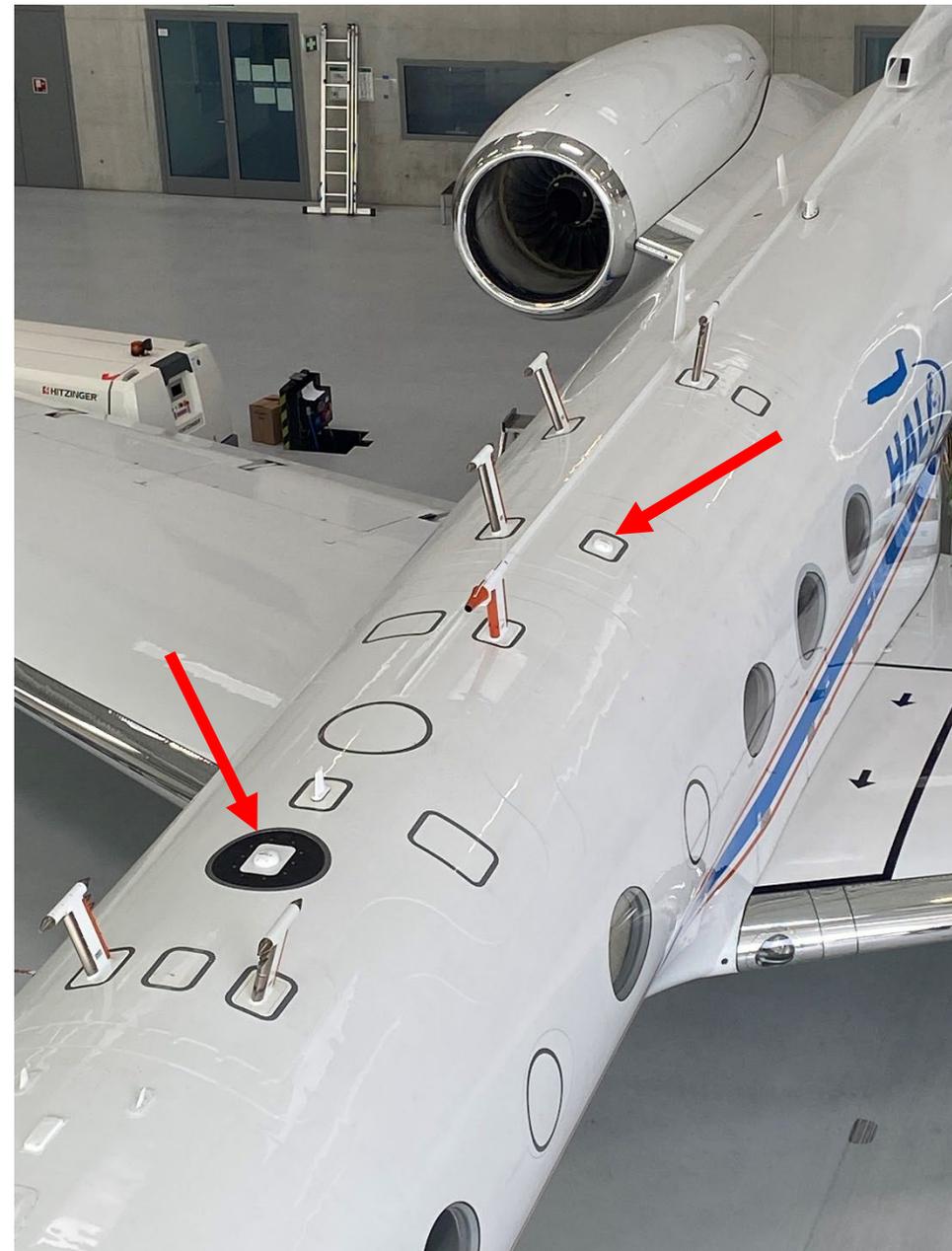
similar to Lenschow and Spyer-Duran, (1989)

## New since 2022: Dual Antenna Configuration

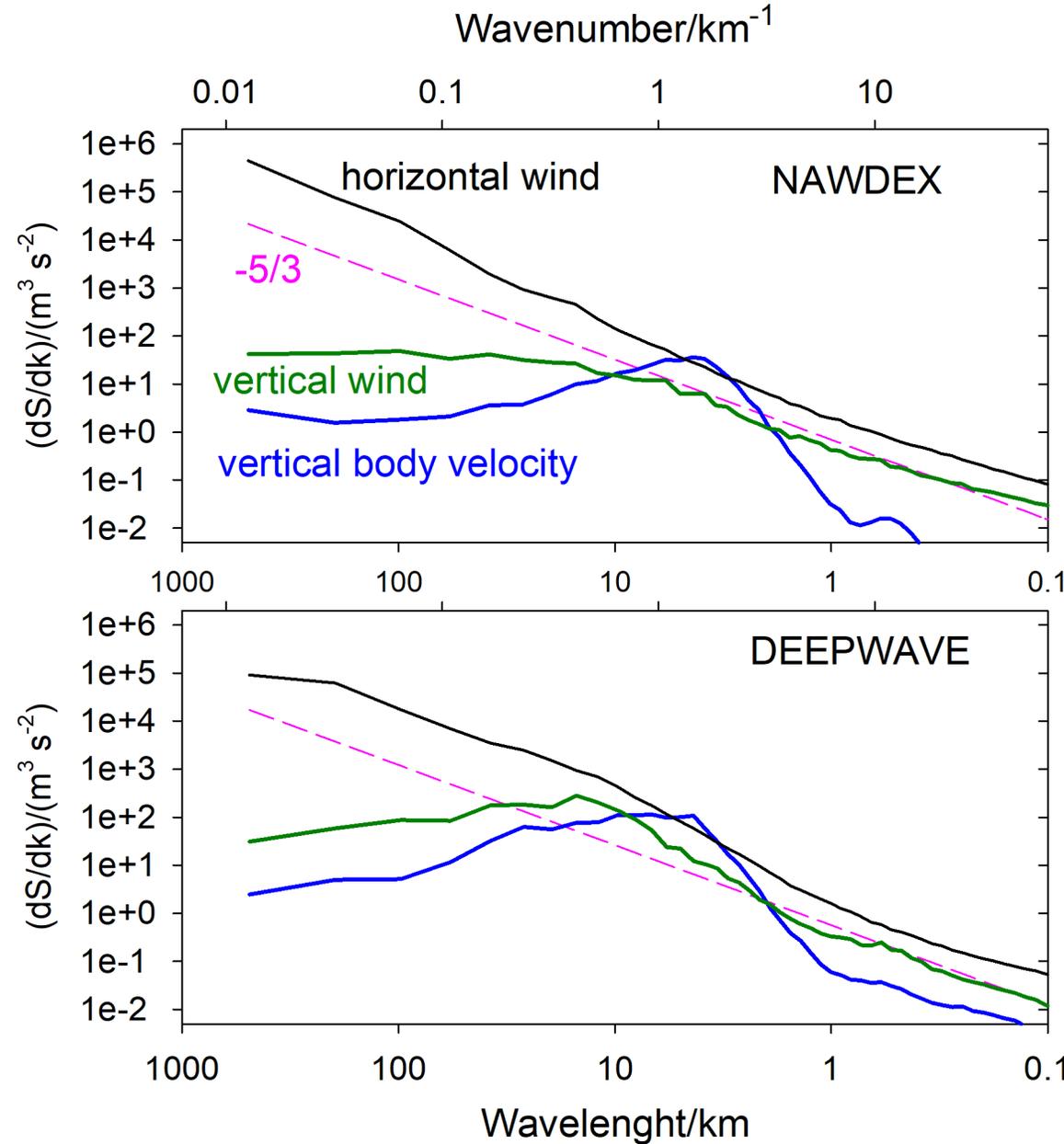
Inertial and GPS Navigation System  
with a dual antenna GNSS system  
for determination of low frequency  
heading and pitch by using two GPS anti



A.Giez, FX, 28.06.2023



# Measured velocity spectra, mean over all straight 2048-s DW- and NW-legs



How to explain the *w* spectra?

Impact of vertical body motions (phugoid oscillation) on *w* measurement?



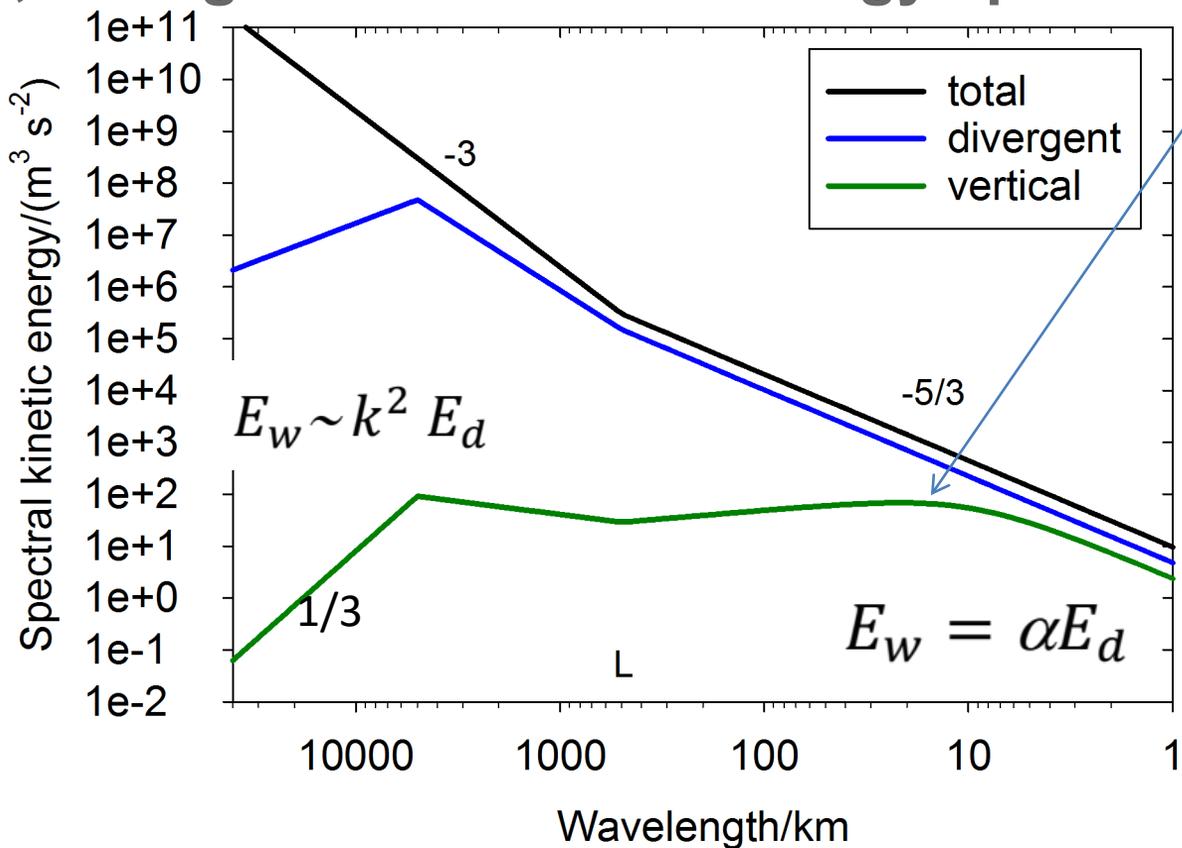
# Schematic sketch of total, divergent and vertical energy spectra

## Hypothesis:

The spectrum of vertical velocities  $E_w$ , as a function of wavenumber  $k$  and height  $h$ , is related to the spectrum of horizontal velocities  $E_h$

1) at large scales: to  $E_d$  by continuity,

2) at small scales: to  $E_h$  by dynamics towards local isotropy



A mesoscale maximum in the  $w$ -spectrum occurs if the divergent horizontal velocity spectrum  $E_d$  has a slope flatter than -2

$$E_w(k, h) = \frac{\alpha (h_{\text{eff}} k)^2}{\alpha + (h_{\text{eff}} k)^2} E_d(k, h), \quad h_{\text{eff}} = \beta h$$

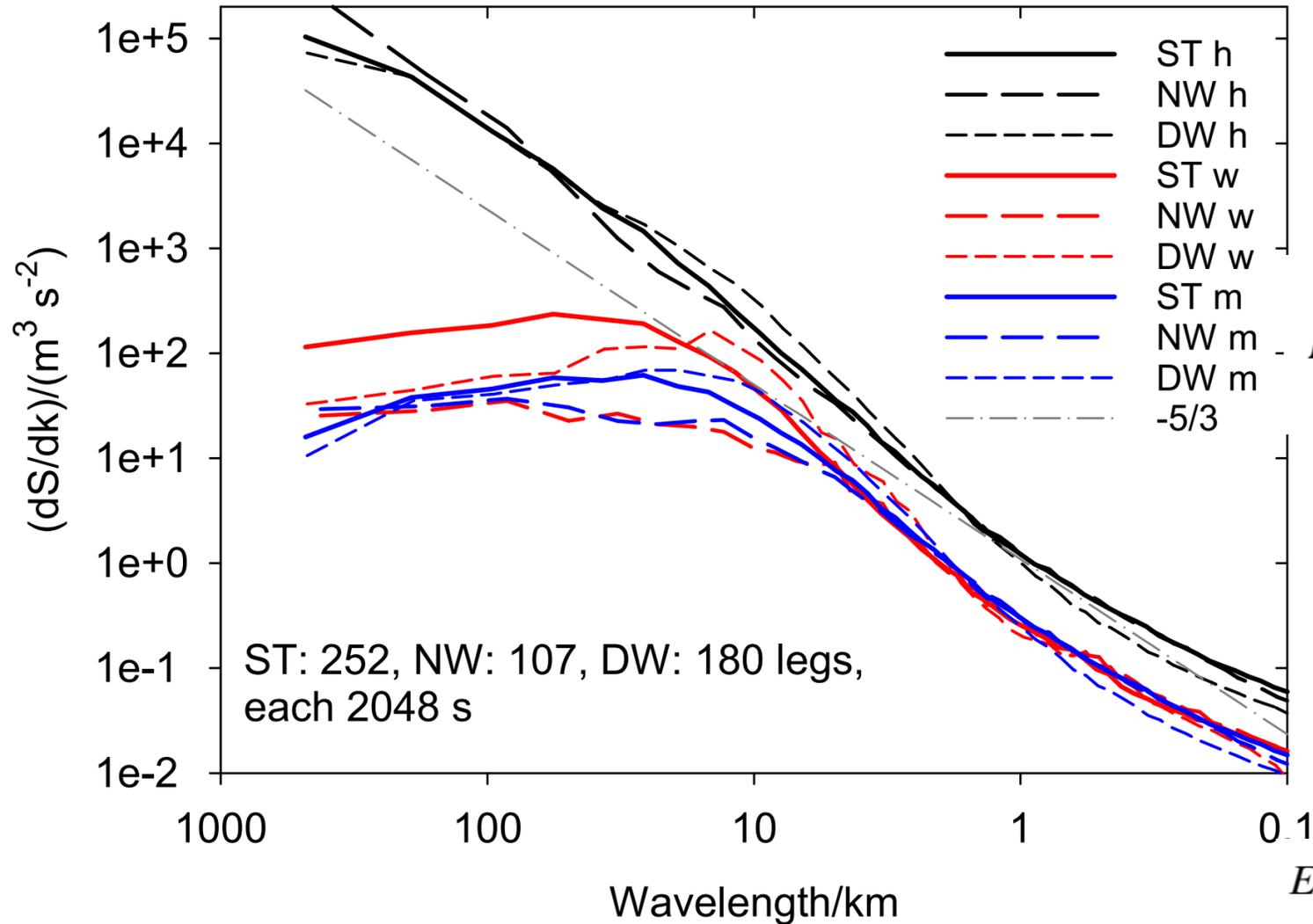
$$E_w(k, h) = (h_{\text{eff}} k)^2 E_d(k, h), \quad hk \ll 1$$

$$E_w(k, h) = \alpha E_d(k, h) = \alpha d E_h(k, h); \quad hk \gg 1$$

$$h=10 \text{ km}, \alpha = 1/2, \beta = 0.11, d=1/2$$



# Mean spectra of kinetic energy from 3 campaigns



"h" horizontal energy

"w" vertical energy spectra

"m" model, (Schumann, JAS, 2019)

$$E_w(k, h) = \frac{\alpha (h_{\text{eff}} k)^2}{\alpha + (h_{\text{eff}} k)^2} d E_h(k, h)$$

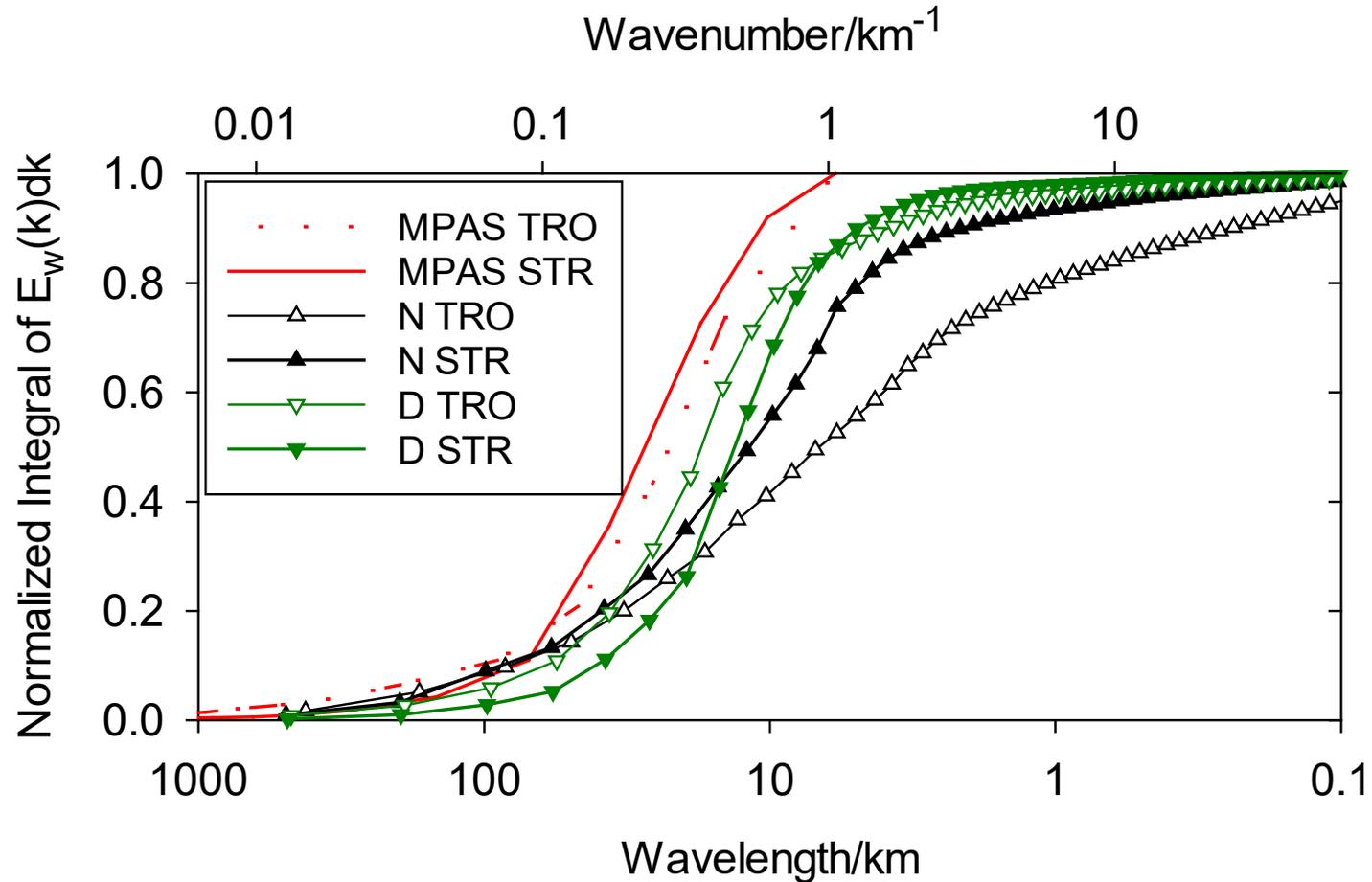
$$h_{\text{eff}} = \beta h$$

$$E_w(k, h) = (h_{\text{eff}} k)^2 E_d(k, h), \quad hk \ll 1$$

$$E_w(k, h) = \alpha E_d(k, h) = \alpha d E_h(k, h); \quad hk \gg 1$$



# Which scales contribute most to w-variance?



> 0.5 km: 90 %

> 7 km: 50 %



## Dissipation rates $\varepsilon$ from SOUTHTRAC 10 and 100 Hz data, FFT

- Dissipation rate  $\varepsilon$  is computed every 5 s from 10 s-segments (100 or 1000 data points) for forward, sideward and upward velocity components  $\rightarrow \varepsilon_i = (\varepsilon_u, \varepsilon_v, \varepsilon_w)$  in  $\text{m}^2 \text{s}^{-3}$
- Variance spectra computed with Tukey filter to minimize influence of aperiodicity in the data.
- Between 0.4 and 4 Hz, the spectra are fitted by a -5/3-Kolmogorov spectrum to derive  $\varepsilon$

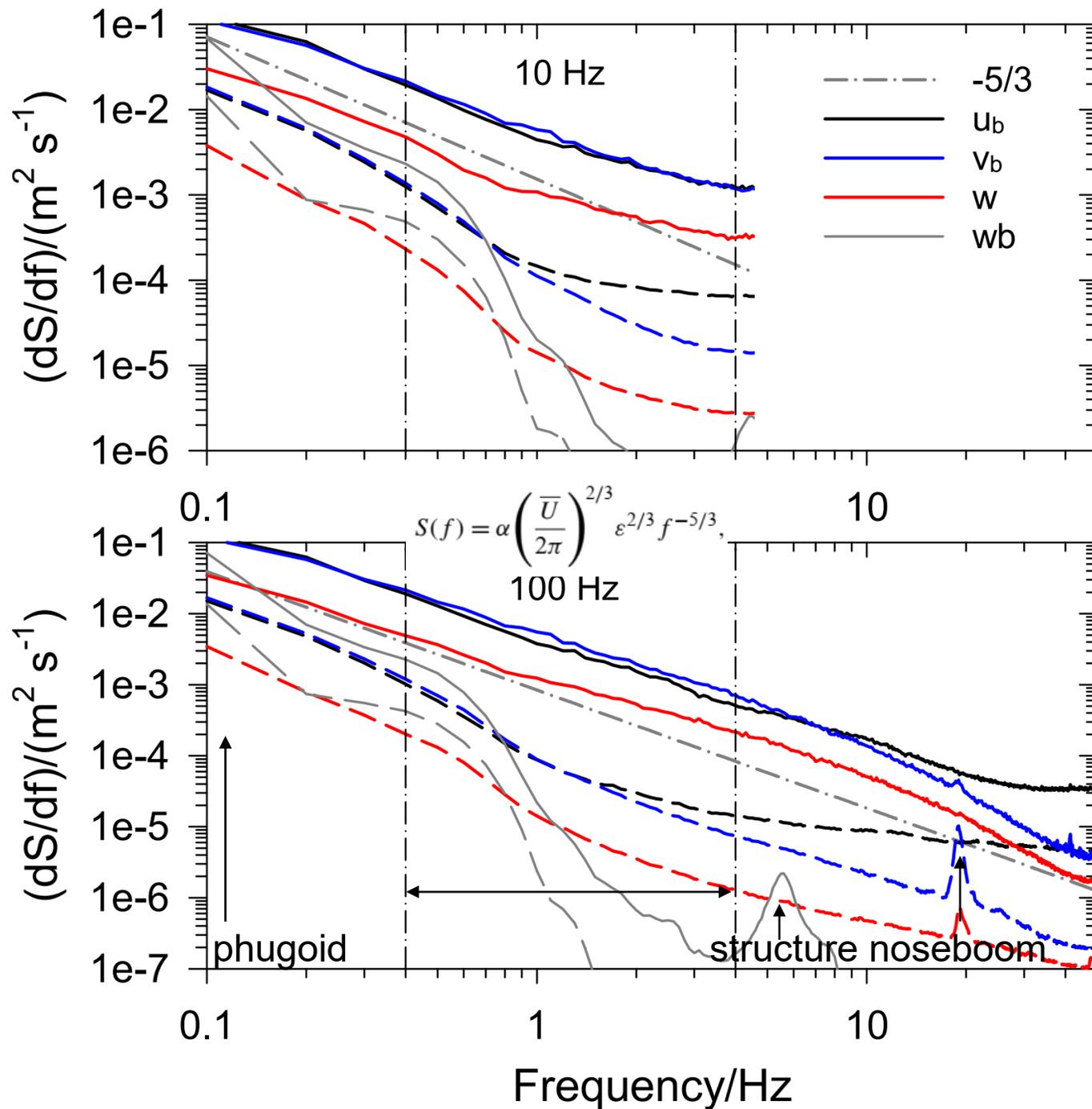
$$S_i(k) = \alpha_i \varepsilon_i^{2/3} k^{-5/3}, \quad \alpha_i = (0.53, 0.707, 0.707), \quad k = 2\pi f / \text{TAS}, \quad \int S_i(k) dk = (1/2) \langle u_i'^2 \rangle$$

- boundaries 0.4 Hz and 4 Hz are selected to avoid high-frequency noise (mainly from TAS for u, beta for v, alpha for w; besides noise in position and attitude data)
- Method basically as in Schumann et al. (1995), validated by comparisons to Bramberger et al. (JACM, 2020); also compared to Imazio et al. (2022, JGR)
- also computed: mean slopes of the log-log w-spectrums in the same frequency range; these slope values fluctuate between at least -4 and +1 around the -5/3 value



# 10 and 100 Hz Frequency Spectra

as used for dissipation rate analysis



$$S_i(k) = C_i \epsilon_i^{2/3} k^{-5/3}$$

$$k = 2\pi f / \text{TAS}$$

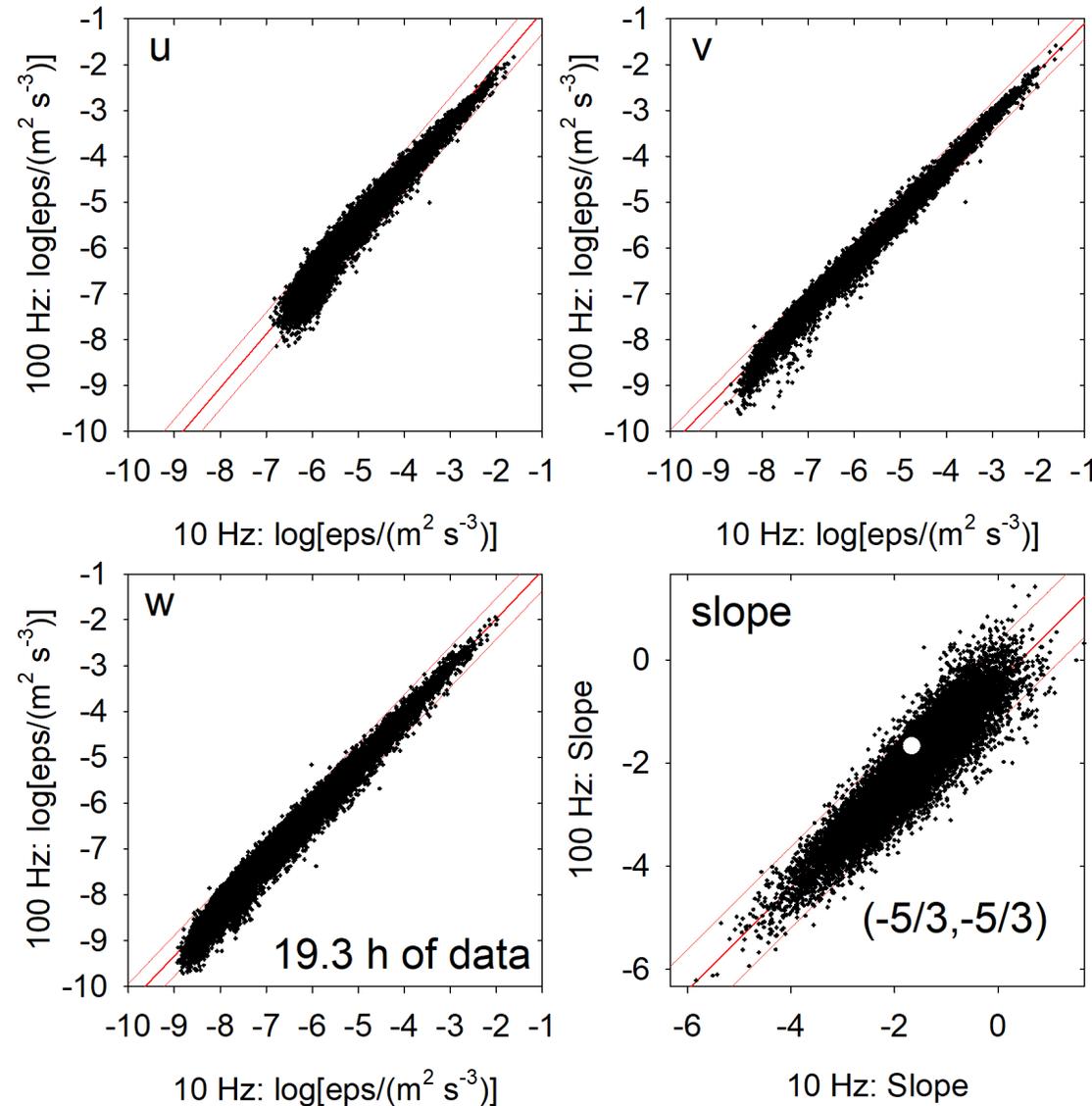
Mean over 6921 legs

Solid : high  $\epsilon$   
Dashed: low  $\epsilon$



# Comparison 10 Hz - 100 Hz: Correlations

Based on all coincident  
100 Hz and 10 Hz legs



**Dissipation rates:**  
 $\epsilon_u$  limited by TAS  
 $\epsilon_v$  limited by beta  
 $\epsilon_w$  limited by alpha

Best resolution for  
dissipation rate  $\epsilon$  from  $w$

$w$ -spectral slope often  
deviating from  
Kolmogorov's  $-5/3$ ,  
mainly because of local  
non-equilibrium



# Inertial range turbulence in stratified air exists only if buoyancy > inertial > viscous forces -> pdf is not log-normal (not log-Gaussian)

Stratification is characterized by the Brunt-Väisälä frequency

$$N = \sqrt{\frac{g}{\Theta} \frac{\partial \Theta}{\partial z}}$$

Characteristic scales are the

Ozmidov for similar inertial/buoyancy forces

$$L_O = \left(\frac{\epsilon}{N^3}\right)^{1/2}$$

and the

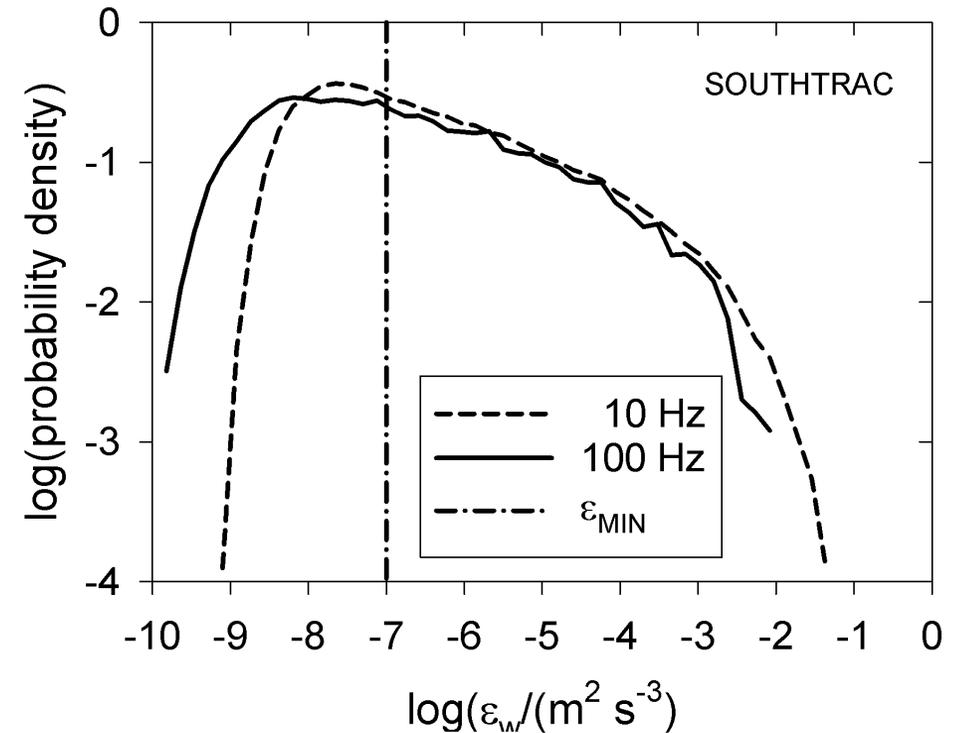
Kolmogorov scales for similar inertial/viscous forces

$$\eta = \left(\frac{\nu^3}{\epsilon}\right)^{1/4}$$

$L_O/\eta > 10$  requires  $\epsilon > \epsilon_{\text{MIN}}$ , with

$$\epsilon_{\text{MIN}} = \left(\frac{L_O}{\eta}\right)^{4/3} \nu N^2 \approx 21.5 \nu N^2$$

$$L_O/\eta = 10.$$



See also  
Lübken (1997),  
Rapp et al. (2004)



# Inertial range turbulence in stratified air exists only if buoyancy > inertial > viscous forces. Same in linear PDF scale

Stratification is characterized by the Brunt-Väisälä frequency

$$N = \sqrt{\frac{g}{\Theta} \frac{\partial \Theta}{\partial z}}$$

Characteristic scales are the

Ozmidov for similar inertial/buoyancy forces

$$L_O = \left( \frac{\epsilon}{N^3} \right)^{1/2}$$

and the

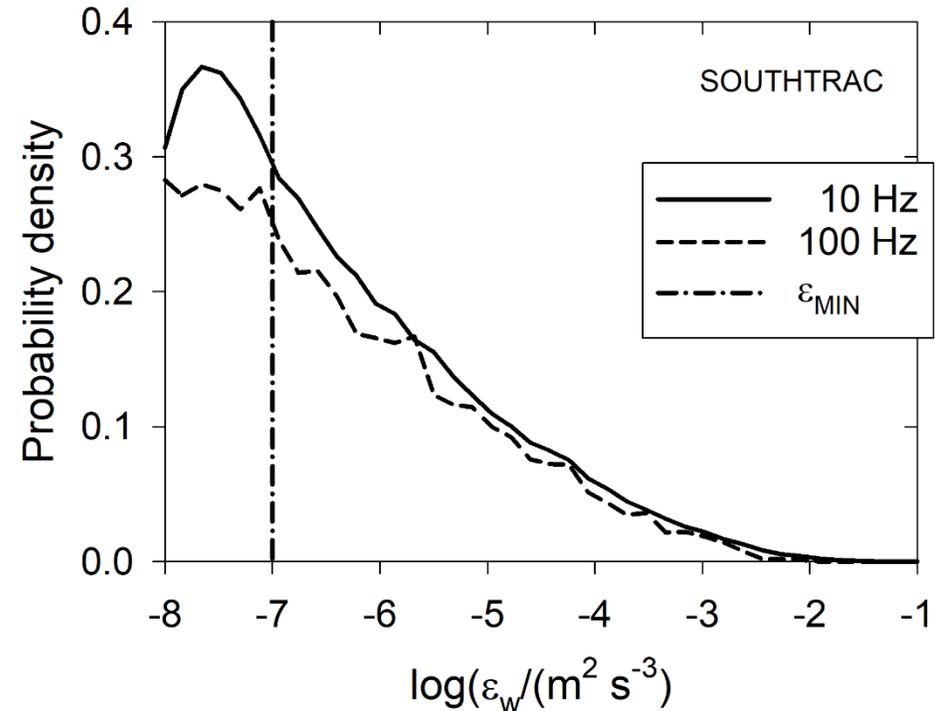
Kolmogorov scales for similar inertial/viscous forces

$$\eta = \left( \frac{\nu^3}{\epsilon} \right)^{1/4}$$

$L_O/\eta > 10$  requires  $\epsilon > \epsilon_{\text{MIN}}$ , with

$$\epsilon_{\text{MIN}} = \left( \frac{L_O}{\eta} \right)^{4/3} \nu N^2 \approx 21.5 \nu N^2$$

$$L_O/\eta = 10.$$



See also  
Lübken (1997),  
Rapp et al. (2004)



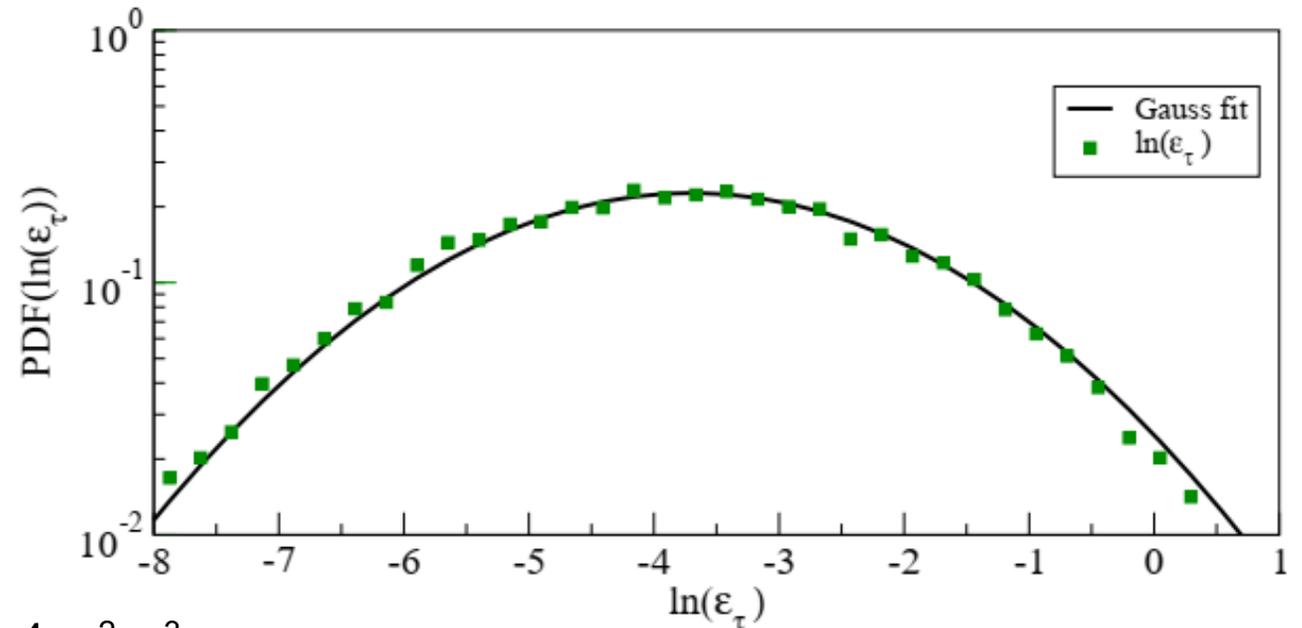
## Comparison to literature:

log-normal pdfs expected for intermittency [*Kolmogorov*, 1962; *Obukhov*, 1962; *Van Atta and Chen*, 1970; *Merceret*, 1976; *Nastrom and Gage*, 1985; *Mandelbrot*, 1991; *Frisch*, 1996; *Frehlich and Sharman*, 2004; *Frehlich et al.*, 2004]

-> log normal if stratification effects are small

## High-resolution measurement of ... turbulence at a mountain top station

by H. Siebert, R. A. Shaw, J. Ditas, T. Schmeissner, S. P. Malinowski, E. Bodenschatz, and H. Xu; AMT, 2015

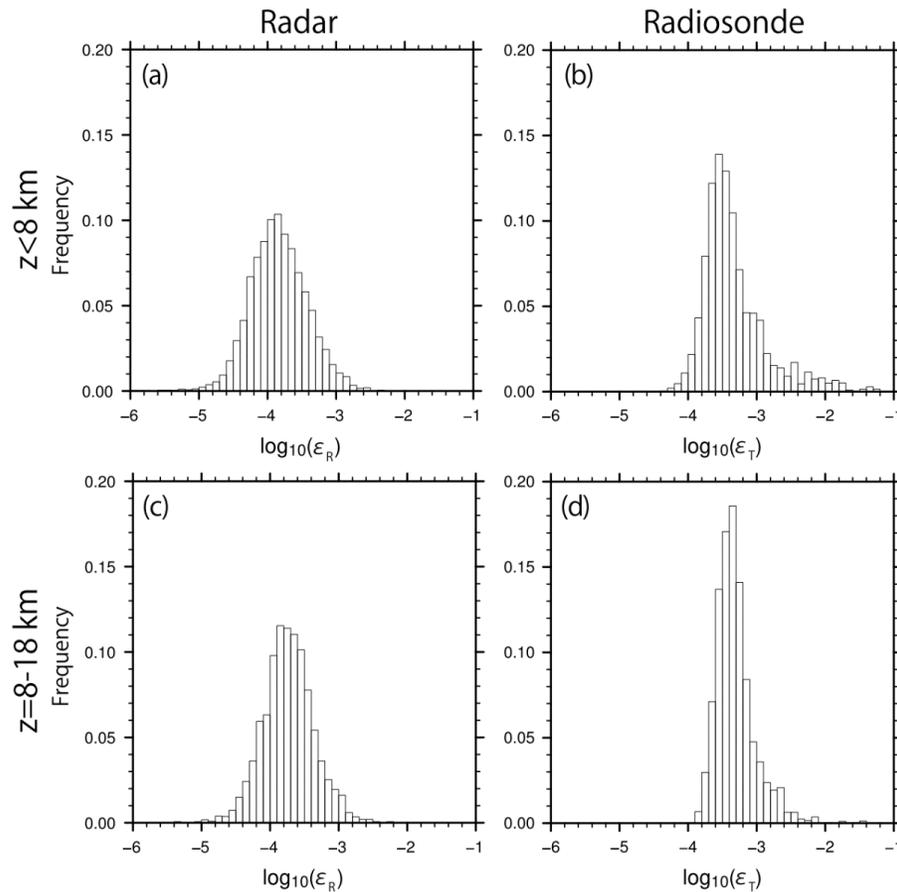


$\approx 3.E-4 \text{ m}^2 \text{ s}^{-3}$

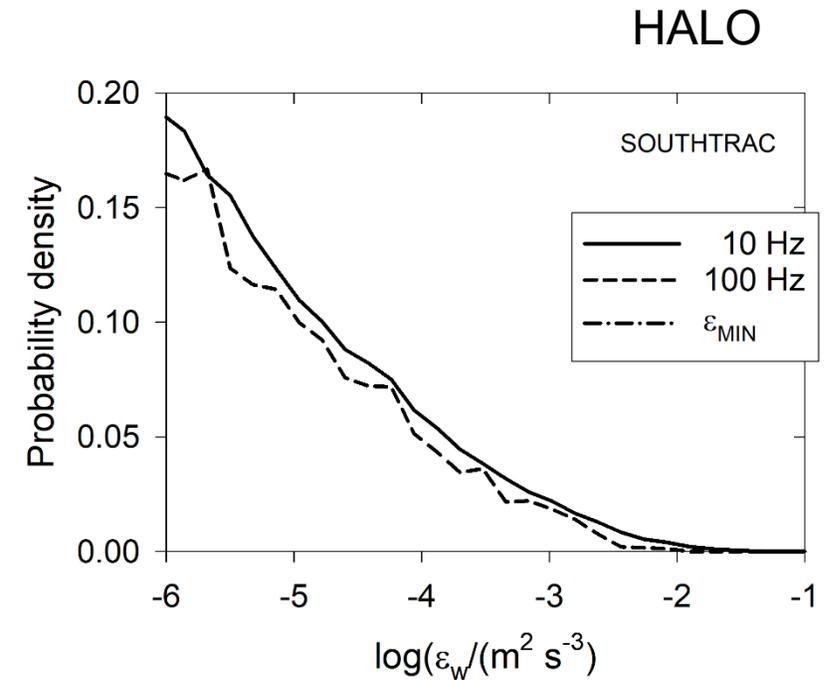
**Figure 7.** Probability density function (PDF) of  $\ln(\epsilon_\tau)$  with  $\tau = 0.1 \text{ s}$  estimated from the same data as in Fig. 4. A Gaussian distribution is plotted as a reference.

# Comparison to literature:

Estimate of Turbulent Energy Dissipation Rate From the VHF Radar and Radiosonde Observations in the Antarctic by Kohma, Sato, Tomikawa, Nishimura and Sato (JGR, 2018)



**Figure 4.** Normalized histograms of  $\epsilon$  estimated from (a) radar and (b) radiosondes in the altitude below 8 km. (c, d) The same as Figures 4a and 4b but for altitudes of 8 to 19 km.



-> strong differences



# Further Comparison to literature:

## Characterizations of tropospheric turbulence and stability layers from aircraft observations (JGR, 2003)

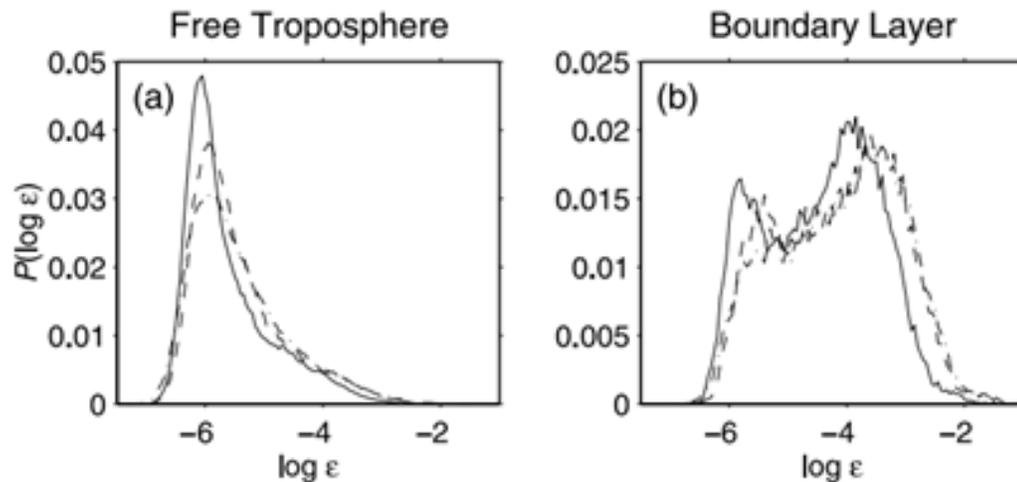
John Y. N. Cho<sup>1</sup> and Reginald E. Newell

Department of Earth, Atmospheric, and Planetary Sciences, Massachusetts Institute of Technology, Cambridge, Massachusetts, USA

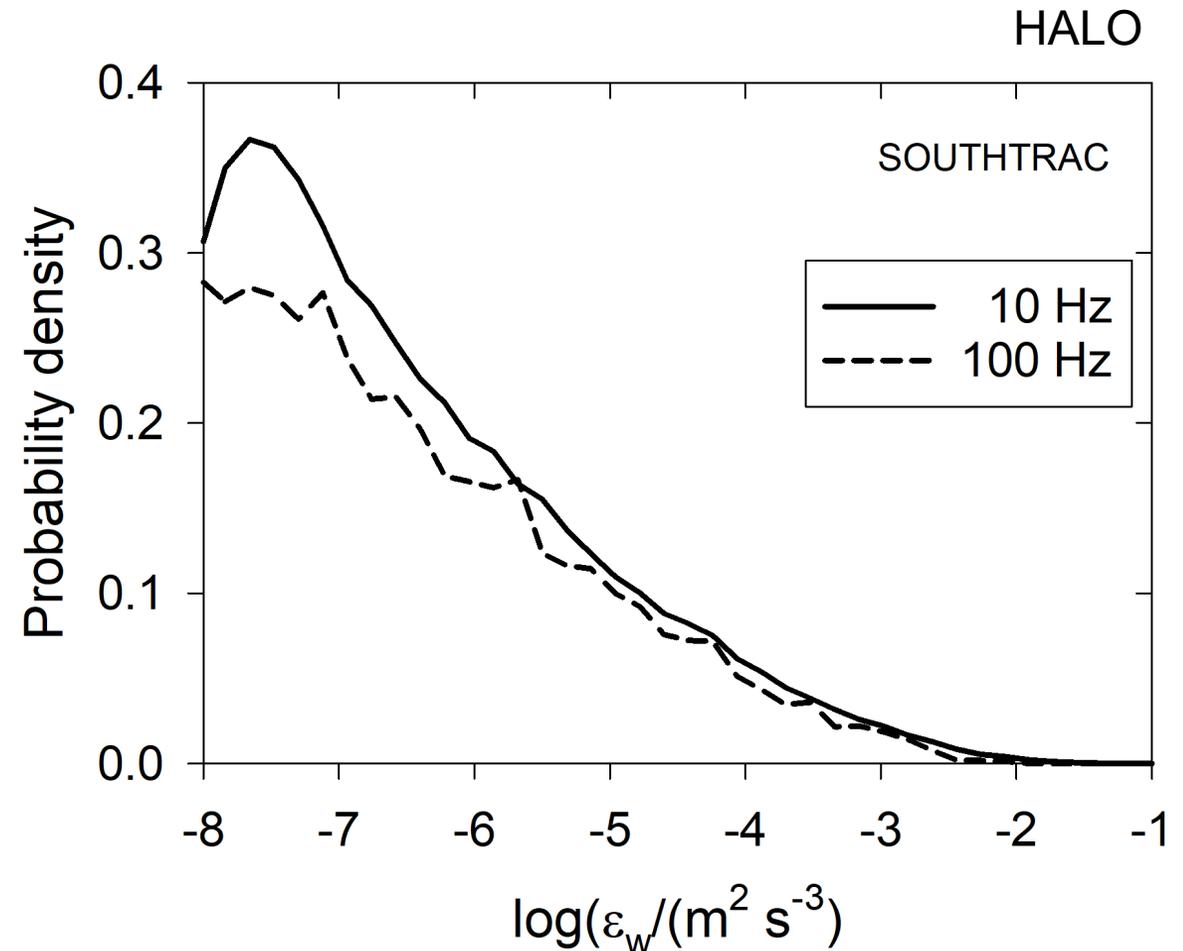
Bruce E. Anderson, John D. W. Barrick, and K. Lee Thornhill

NASA Langley Research Center, Hampton, Virginia, USA

Received 2 August 2002; revised 12 December 2002; accepted 23 December 2002; published 26 August 2003.



**Figure 4.** PDFs of  $\log \epsilon$  and  $\log I$  for  $\Delta t = 0.05$  s (solid), 0.25 s (dashed), and 0.5 s (dash-dotted).



AURÉLIEN PODGLAJEN,<sup>a</sup> T. PAUL BUI,<sup>b</sup> JONATHAN M. DEAN-DAY,<sup>b</sup> LEONHARD PFISTER,<sup>b</sup>  
 ERIC J. JENSEN,<sup>b</sup> M. JOAN ALEXANDER,<sup>c</sup> ALBERT HERTZOG,<sup>d</sup> BERND KÄRCHER,<sup>c</sup>  
 RIWAL PLOUGONVEN,<sup>f</sup> AND WILLIAM J. RANDEL<sup>g</sup>

## Further Comparison to literature:

NOVEMBER 2017

PODGLAJI

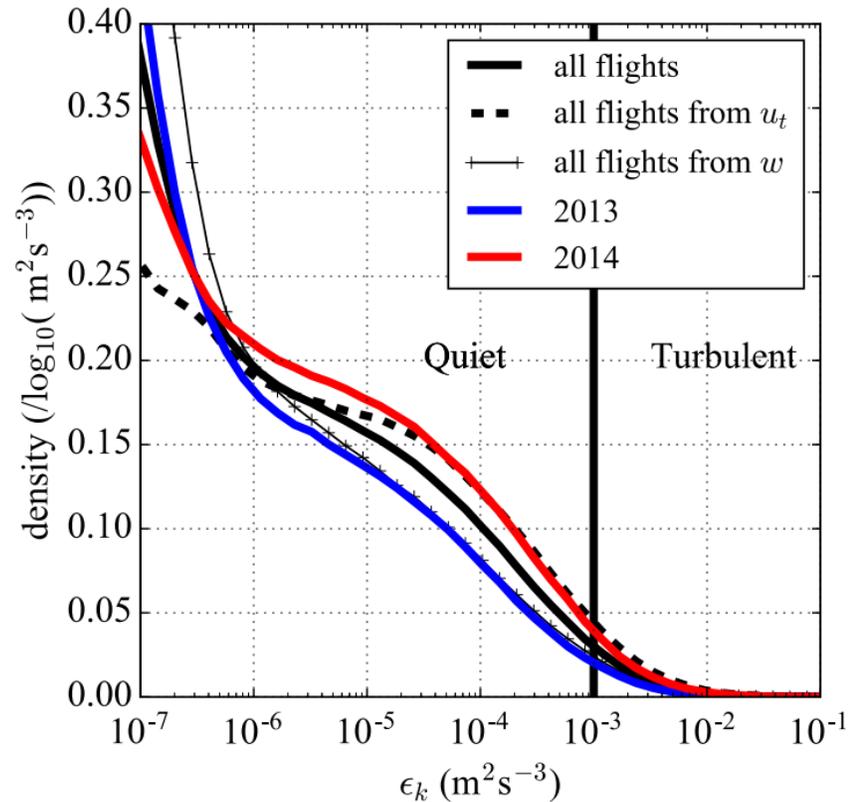
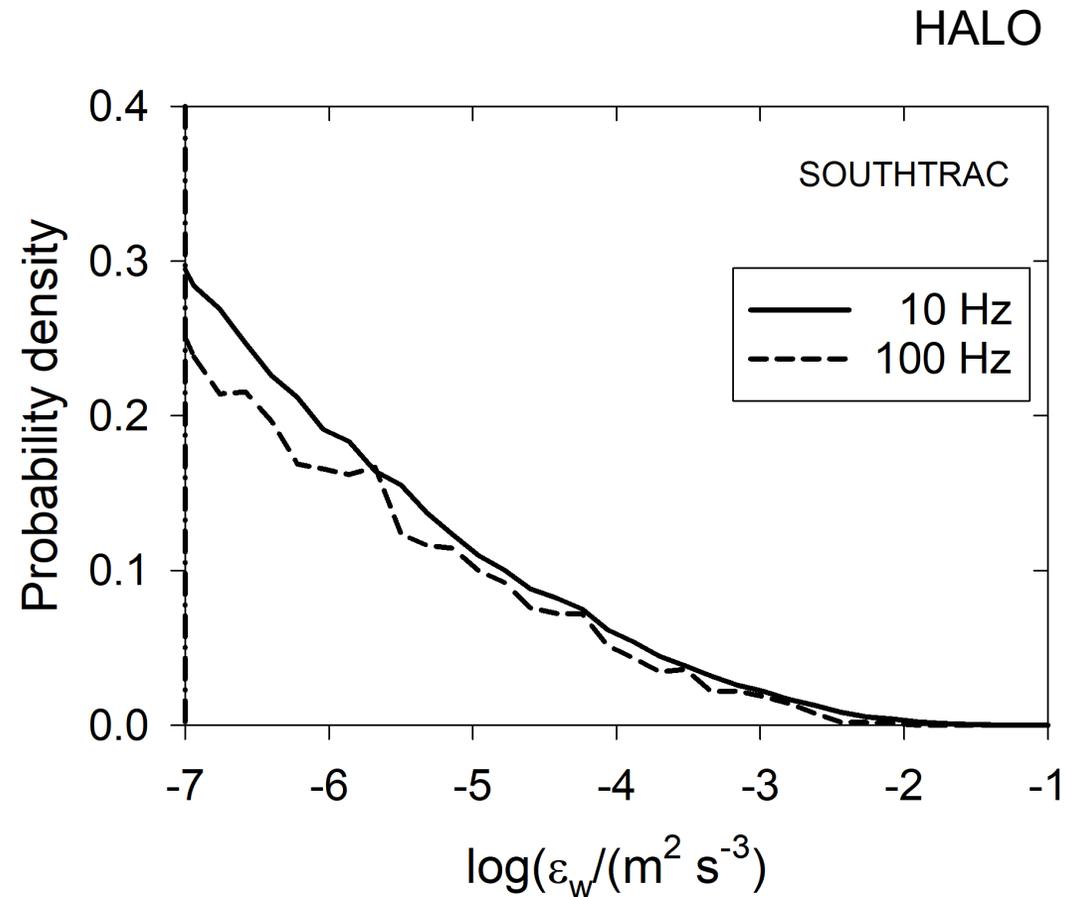


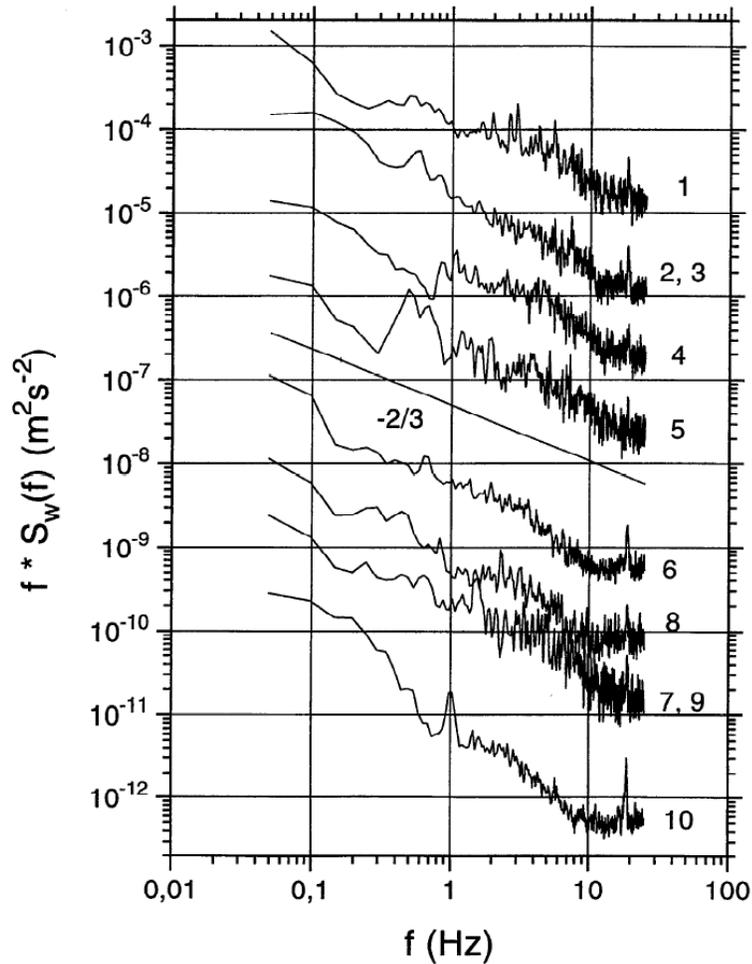
FIG. 6. PDF of  $\epsilon_k$  for all ATTREX flights estimated from  $u_t$  only (dashed black line) and from  $w$  only (crosses) or using Eq. (3) (continuous black line), 2013 eastern Pacific flights (blue line), and 2014 western Pacific flights (red line). The vertical black line shows the threshold chosen to select occurrence of active events. Only the values above the estimated noise level ( $\sim 1 \times 10^{-7} \text{ m}^2 \text{ s}^{-3}$ ) are shown.

JAS (2017)

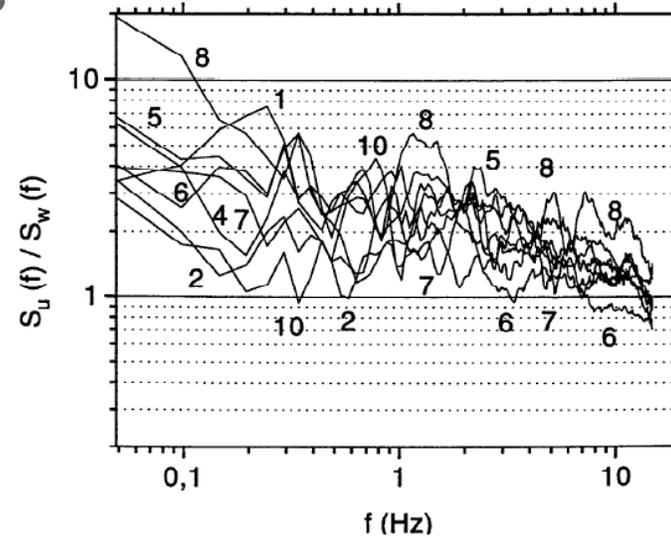
ATTREX,  
Global Hawk,  
20 Hz



# Comparison to Literature: Turbulence in the tropopause region: inertial range? Local isotropy?



**Figure 12.** Spectral density function  $M(f) = fS_w(f)$  (non-filtered) of vertical velocity fluctuations versus frequency  $f$ . The numbers refer to the peaks within the respective flight segments as in Figure 11. To separate the curves,  $M(f)$  has been reduced before plotting by a factor 1 (for 1), 10 (for 2, 3), 100 (for 4), etc.



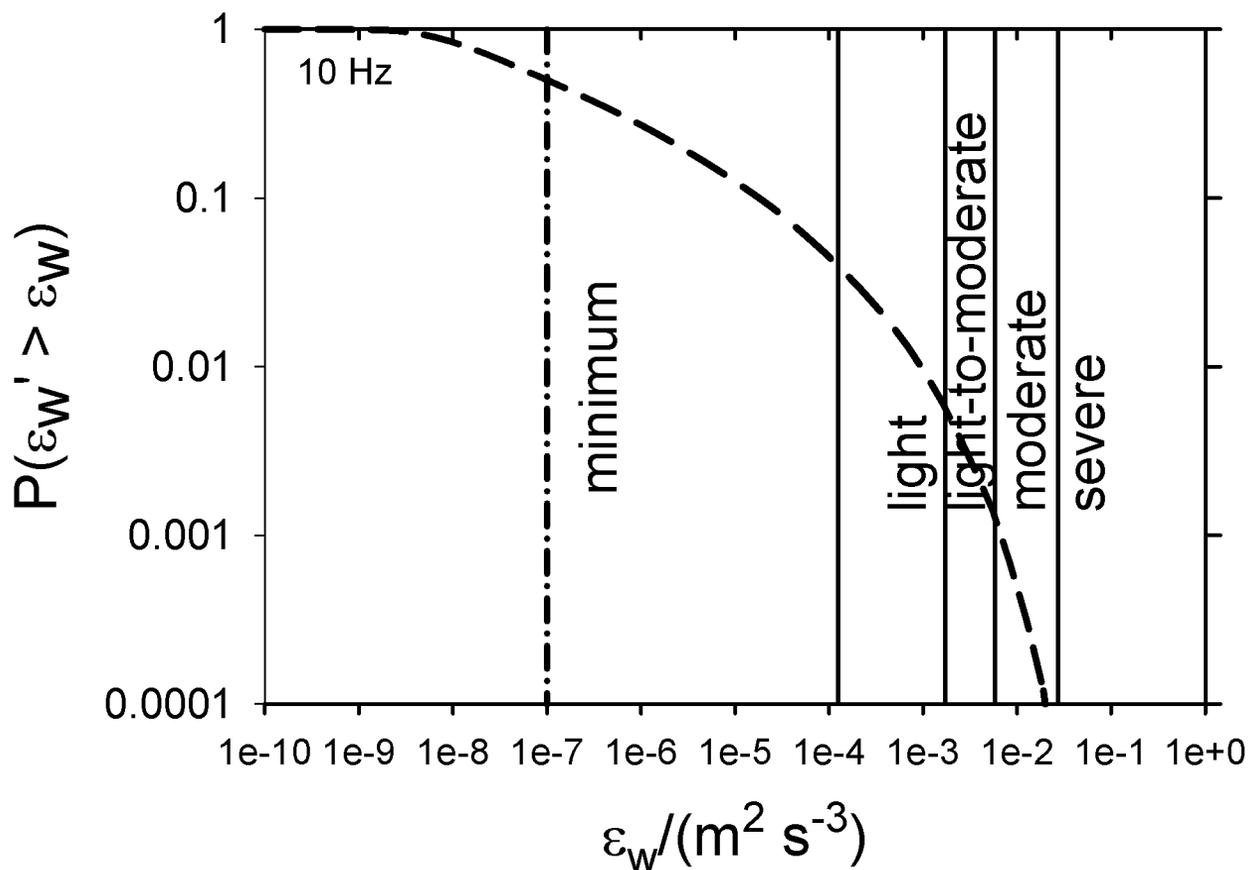
Number	$\epsilon$ , $10^{-8} \text{ m}^2 \text{ s}^{-3}$	$L_O$ , m	$\eta$ , m
1	$7.9 \pm 0.7$	0.12	0.02
2	$5.7 \pm 1.4$	0.10	0.03
3	$5.7 \pm 1.4$	0.10	0.03
4	$10 \pm 2.0$	0.12	0.03
5	$16 \pm 3.0$	0.15	0.02
6	$1.4 \pm 0.5$	0.06	0.04
7	$1.7 \pm 0.5$	0.06	0.04
8	$10 \pm 2.0$	0.14	0.03
9	$10 \pm 2.0$	0.14	0.03
10	$1.1 \pm 0.2$	0.04	0.05

**UTLS North Atlantic  
mid latitudes  
POLINAT, Falcon**  
Schumann, Konopka,  
Baumann et al. (JGR, 1995)

$$L_O = \left( \frac{\epsilon}{N^3} \right)^{1/2}$$

$$\eta = \left( \frac{\nu^3}{\epsilon} \right)^{1/4}$$

**Severe turbulence occurs very rarely.  
Even moderate turbulence occurred in only < 0.1 %  
of all 10-s SOUTHTRAC flight legs**



	$\varepsilon$	EDR = $\varepsilon^{1/3}$
unit:	$\text{m}^2 \text{s}^{-3}$	$\text{m}^{2/3} \text{s}^{-1}$
minimum	< 1.e-7	0.005
light	> 0.000125	0.05
light-to-moderate	> 0.001728	0.12
moderate	> 0.005832	0.18
moderate-to-severe	> 0.027	0.3

higher limit values used elsewhere (Sharman et al., 2014, pers. comm. 2023):

EDR=0.10, 0.3, 0.5  $\text{m}^{2/3}\text{s}^{-1}$  (ICAO, 2001)

EDR=0.15, 0.22, 0.34  $\text{m}^{2/3}\text{s}^{-1}$  (Sharman, 2023)

for “light”, “moderate”, “severe”, resp.



For more details see:

DECEMBER 2019

SCHUMANN

3847

## The Horizontal Spectrum of Vertical Velocities near the Tropopause from Global to Gravity Wave Scales

ULRICH SCHUMANN

*Deutsches Zentrum für Luft- und Raumfahrt, Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany*

## JGR Atmospheres

RESEARCH ARTICLE

10.1029/2022JD036654

### Special Section:

SOUTHTRAC-GW: An airborne field campaign to explore gravity wave dynamics at the world's strongest hotspot

## High-Resolution Aircraft Observations of Turbulence and Waves in the Free Atmosphere and Comparison With Global Model Predictions



Andreas Dörnbrack<sup>1</sup> , Peter Bechtold<sup>2</sup> , and Ulrich Schumann<sup>1</sup> 

<sup>1</sup>DLR Oberpfaffenhofen, Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany, <sup>2</sup>ECMWF, Reading, UK, Bologna, Italy, Bonn, Germany



# Conclusions

- The BAHAMAS system on HALO provides reliable energy spectra and dissipation estimates
- The vertical wind ( $w$ ) spectra are related to kinetic energy of divergent motions ( $d$ ) at large scales by continuity and to total horizontal energy ( $h$ ) at small scales
- In the stably stratified atmosphere near the tropopause, dissipation is anisotropic and not log-normal distributed.
- The Kolmogorov model provides reliable dissipation rate for  $\varepsilon > \varepsilon_{\text{MIN}} \sim 1 \cdot 10^{-7} \text{ m}^2 \text{ s}^{-3}$  only
- **Strong turbulence occurs very rarely.** Even moderate turbulence occurred in only 0.1% of all SOUTHTRAC 10-s flight legs
- Instead we have **mainly anisotropic wavy motions without inertial-range turbulence**
- Comparison to literature shows reasonable agreement with previous research aircraft results
- The set of derived  $\varepsilon_w$  values is available and is a valid measure for “clear air turbulence”
- Next: relate ice supersaturation ( $R_{\text{hi}} > 1$ ) to turbulence, stratification shear etc. using high resolution radiosonde data (BUFR) data. Mainly RS41?



# Reserve slides



# Dissipation rates $\epsilon$ from spectra or structure function

- Both spectra and structure functions useful to identify scaling laws
- Spectra provide more accurate results than structure functions, at least for turbulence in stratified air masses



# Dissipation rates $\varepsilon$ from SOUTHTRAC 10 Hz data

## - Structure Function

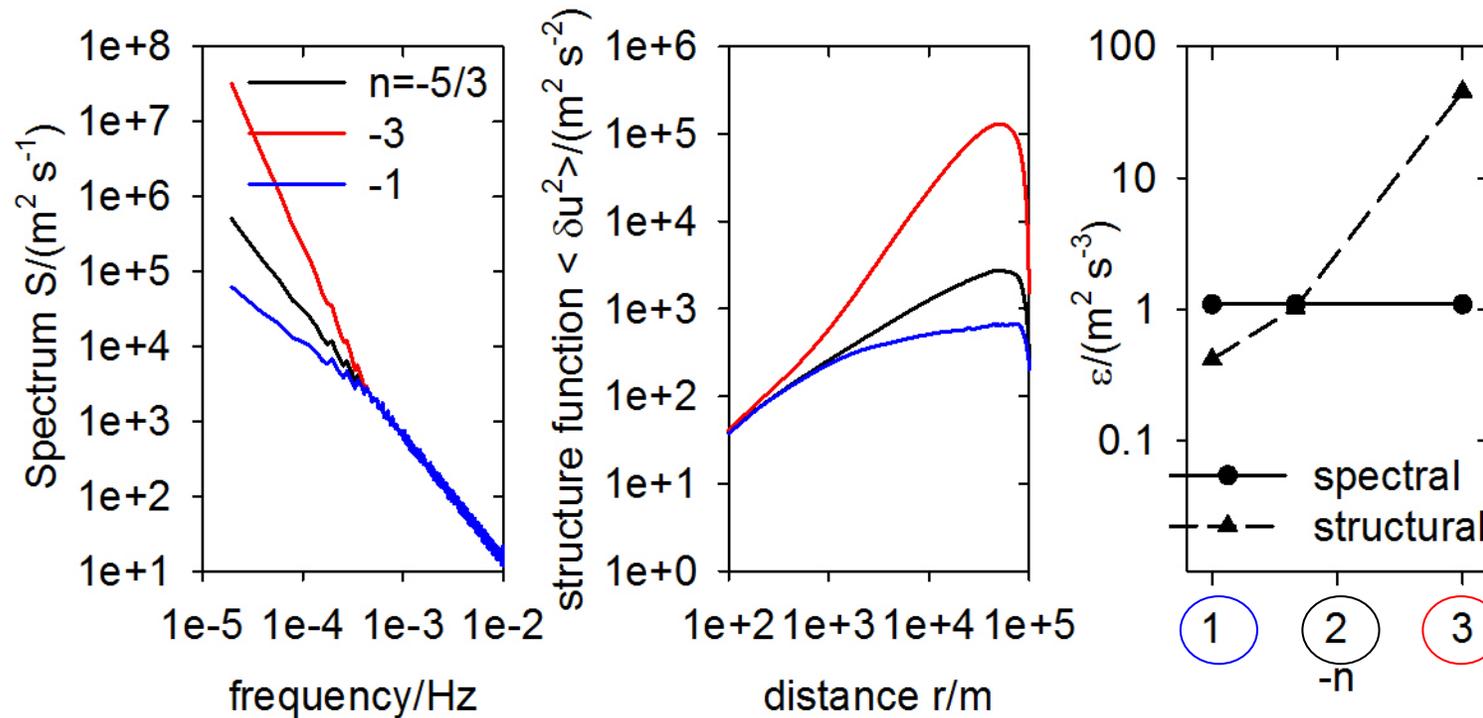
- See Frehlich and Sharman (MWR, 2004)
- dissipation rate  $\varepsilon$  is computed every 5 s from 10 s-segments (100 data points) for forward, sideward and upward velocity components  $\rightarrow (\varepsilon_u, \varepsilon_v, \varepsilon_w)$  in  $\text{m}^2 \text{s}^{-3}$
- Structure function computed from the definition

$$D_u(s) = \langle (u'(x+s)u'(x)) \rangle = C_K \varepsilon^{2/3} s^{2/3}, \quad C_K = (2, 8/3, 8/3) \text{ for } u, v, w$$

- Which requires a double loop (s, and time) and hence more computer time than computing spectra
- and approximated by the Kolmogorov law:
  
- Evaluated for smallest distance  $s = \text{TAS}^* \Delta t$



# Dissipation rates from turbulence structure-functions and (1-d) variance spectra with spectral slopes between -1 and -3.



Results from analytical integrals and numerical simulations agree

Kolmogorov(1941):

$$E(k) = \alpha \epsilon^{2/3} k^{-5/3}$$

$$S(r) = c \epsilon^{2/3} r^{2/3}$$

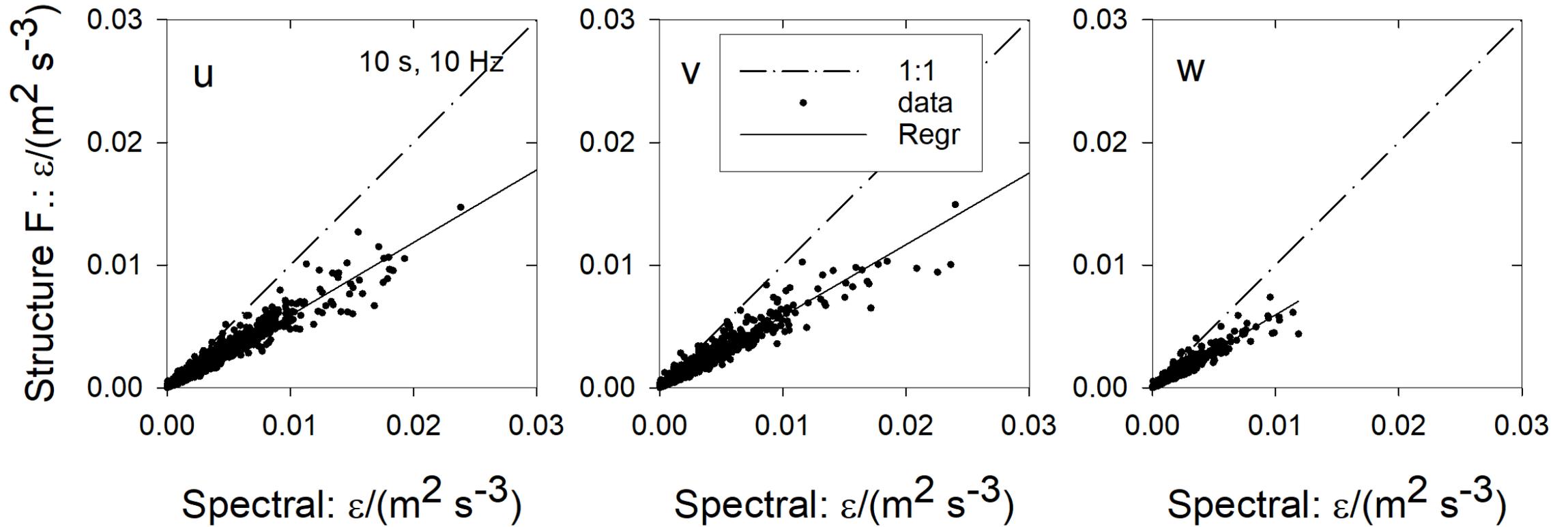
$$c = (3/2)\Gamma(1/3)\alpha$$

-> Spectra are better suited for dissipation analysis



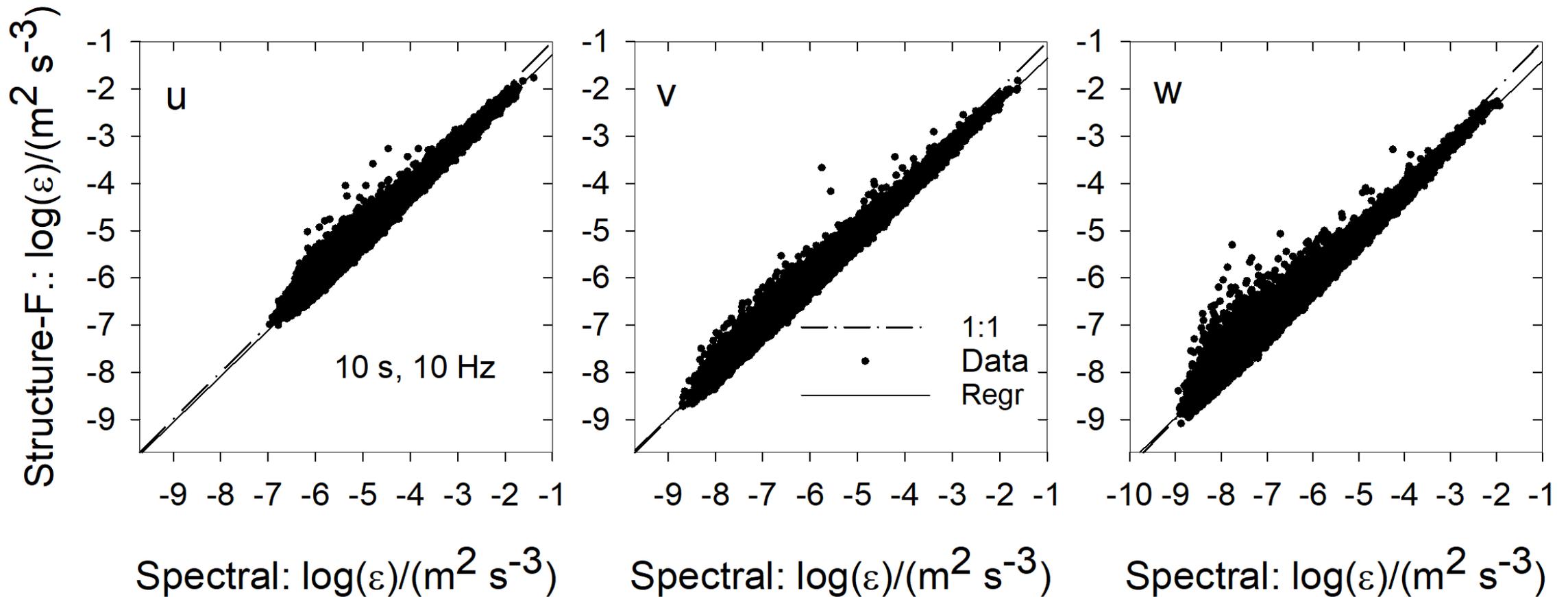
# SOUTHTRACK: Dissipation rates from spectral and structure function analysis

10-s segments - Linear scales:



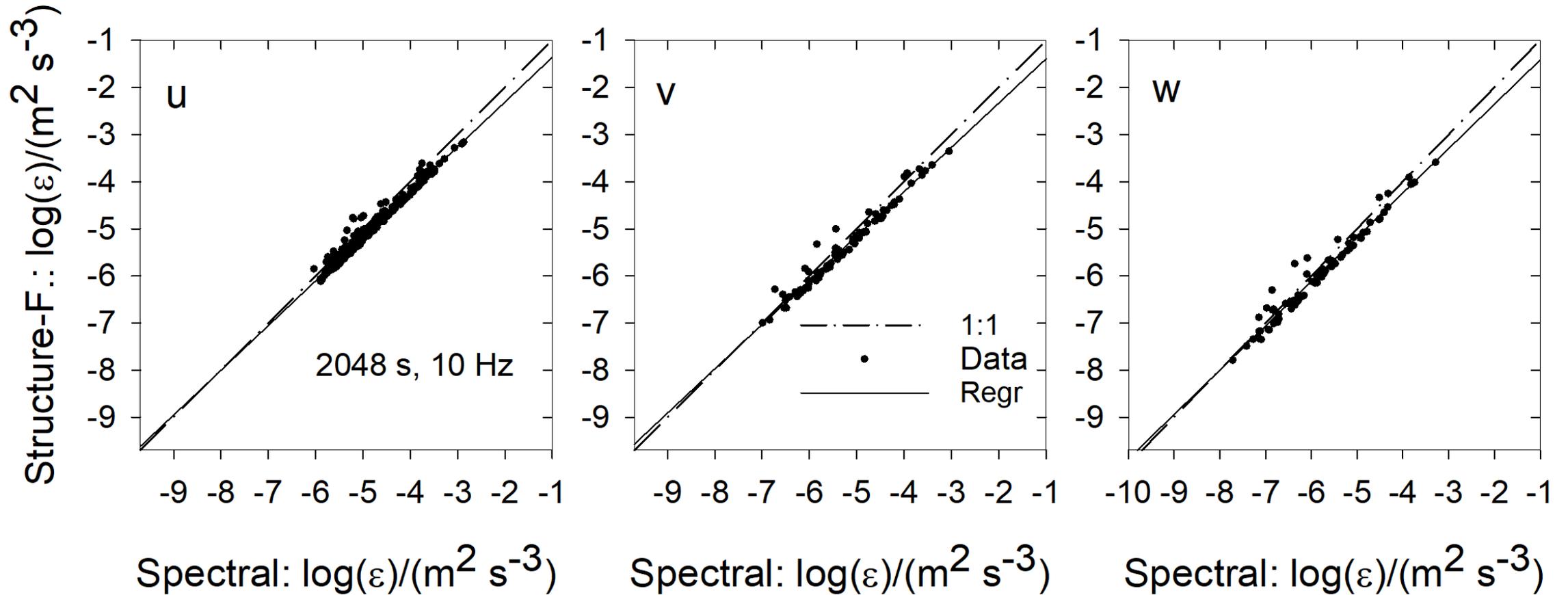
# SOUTHTRACK: Dissipation rates from spectral and structure function analysis

10-s segments - Logarithmic scales:

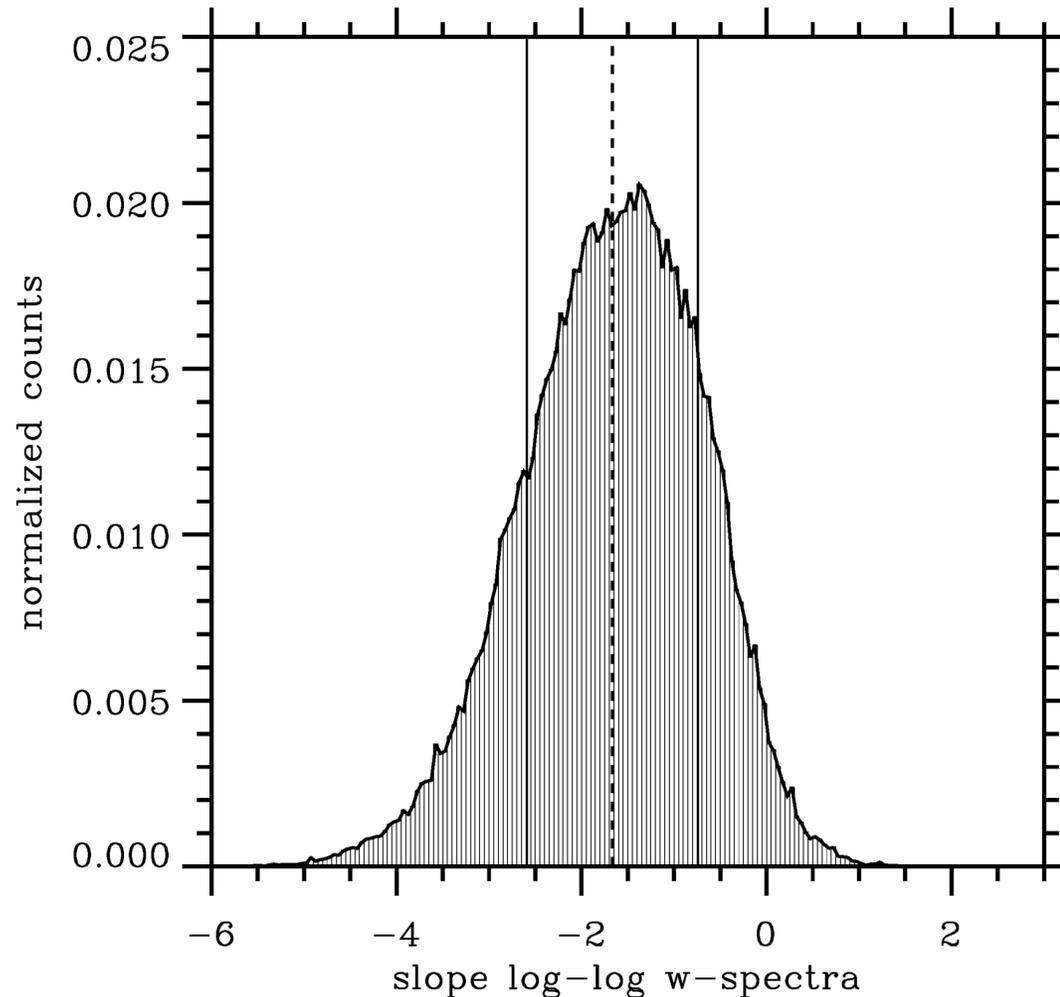


# SOUTHTRACK: Dissipation rates from spectral and structure function analysis

2048-s segments - logarithmic scales:



## Spectra of 10-s flight segments reflect a steady inertial subrange in the mean only: bursts and decaying turbulence instead



mean slope =  $-\frac{5}{3} \pm 0.92$   
 derived turbulence is nonsteady and highly anisotropic;  
 i.e. assumption of locally isotropic inertial-range turbulence is a hardly satisfied, rough approximation and valid in large-ensemble averages only.

There are atmospheric regions where turbulence is in its stationary state and regions where turbulence decays in time or, on the contrary, becomes stronger (WACŁAWCZYK et al., JAS 2019).

