Q: Why does the Sun have a Corona? A Wind?

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Review & Activities based on original talk

B large enough to restrict plasma motion: only along field lines



Od picture: balance between heat & radiation @ fixed pressure

> Radiative losses per volume: Vol. I: Eq. (8.6) Principia (9.1)

 $\underbrace{n_e n_H}_{\Lambda} \Lambda(T) = p^2 \frac{\Lambda(T)}{k_{\star}^2 T^2}$

radiation heat in

Activity 122 (p. 243): Eq. (9.1) contains a product of electron and hydrogen densities, but hydrogen is fully ionized at coronal temperatures and thus has no spectral lines that can be excited through collisions with electrons. Why is it acceptable to express it this way?



radiation



10-2

104

105

heat in

Od picture: balance between heat & radiation @ fixed pressure

> Radiative losses per volume: Vol. I: Eq. (8.6) Principia (9.1)

> > 10⁶

Т [К]

107

Activity 121 (p. 243): The processes of electromagnetic radiation from a plasma involve three fundamentally distinct processes: bound-bound, free-bound (radiative recombination), and free-free (Bremsstrahlung) emission. The Sun's coronal emission, caused by collisions of ions with thermal electrons, is dominated the first, except for flares when the last is also important; why?

→ Which ions are typically strong contributors to the coronal X-ray and EUV emission from an active region at ~ 3MK? Hint: combine elemental abundances with ionization energies (such as given by *). For this rough estimate, ignore oscillator strengths for the transitions involved. For the solar corona under most conditions, the dominant radiative losses are from C, N, O (below about 0.5 MK), and Fe (above about 0.5 MK).

https://en.wikipedia.org/wiki/lonization_energies_of_the_elements_(data_page)











Od picture: balance between heat & radiation @ fixed pressure

> Radiative losses per volume: Vol. I: Eq. (8.6) Principia (9.1)





 $n_e n_I$



Activity 123 (p. 245): Use Eq. (9.4) to estimate typical volumetric heating rates (i.e. ε_{heat}) for ... an active region (with coronal field strengths of order 200 G, loop-top temperatures of ~ 3 MK, and loop half lengths L $\simeq 15 \times 10^9$ cm). Compare [this] to the thermal energies also estimated from Eq. (9.4) and also compare plasma to field pressures (i.e., compute values of plasma- β).



$$T_{\rm a,6} \approx 2.8 (n_{\rm a,10} L_9)^{1/2} ; T_{\rm a,6} \approx 7.3 (\epsilon_{\rm heat} L_9^2)^{2/7},$$
 (9.4)

Extra for later today: what are $T_{a,6}$ and $n_{a,10}$ when the heating rate ε_{heat} in the active region loop increases by $\times 10^4$? On which does this have a larger effect?

Activity 123 (p. 245): Use Eq. (9.4) to estimate typical volumetric heating rates (i.e. ε_{heat}) for ... an active region (with coronal field strengths of order 200 G, loop-top temperatures of ~ 3 MK, and loop half lengths L ~ 15 × 10⁹ cm). Compare [this] to the thermal energies also estimated from Eq. (9.4) and also compare plasma to field pressures (i.e., compute values of plasma- β).

$$T_{a,6} \approx 2.8(n_{a,10}L_9)^{1/2} ; T_{a,6} \approx 7.3(\epsilon_{heat}L_9^2)^{2/7}, \qquad (9.4)$$

$$\epsilon = L_9^{-2} (T_6/7.3)^{7/2} = (15)^{-2} 2^{-7/2} = 4 \times 10^{-4} \text{ erg cm}^{-3} \text{ s}^{-1}$$

$$n_{10} = L_9^{-1} (T_6/2.8)^2 = (15)^{-1} 1^2 = 0.067$$

$$\implies n_e = 7 \times 10^8 \text{ cm}^{-3}$$

$$e = 3 n_e k_b T = 3 (7 \times 10^8) (4 \times 10^{-10}) = 0.9 \text{ erg cm}^{-3}$$

$$e/\epsilon = 0.9 / (4 \times 10^{-4}) = 2.2 \times 10^3 \text{ s} = 36 \text{ min}$$

 $F = L_9 \epsilon = L_9^{-1} (T_6/7.3)^{7/2} = 6 \times 10^6 \text{ erg cm}^{-2} \text{ s}^{-1}$



outflow

heat in



specific enthalpy



Advective energy oss -

>> radiative loss

$$\frac{1}{v}\frac{dv}{dr}\left\{v^{2}-\frac{2kT}{m_{p}}\right\} = \left\{\frac{4kT}{m_{p}r} - \frac{GM_{\odot}}{r^{2}}\right\}$$
(2.10)

$$\frac{d}{dr}\left\{\frac{v^{2}}{2} - \frac{2k_{b}T}{m_{p}}\ln(v)\right\} = \frac{d}{dr}\left\{\frac{2k_{b}T}{m_{p}}\ln(r^{2}) + \frac{GM_{\odot}}{r}\right\}$$
because

$$\frac{d}{dr}\left\{\frac{v^{2}}{2} - \frac{2k_{b}T}{m_{p}}\ln(vr^{2}) - \frac{GM_{\odot}}{r}\right\} = 0 = \frac{d}{dr}\left\{\frac{v^{2}}{2} + \frac{2k_{b}T}{m_{p}}\ln(\rho) - \frac{GM_{\odot}}{r}\right\}$$
potential
bernoulli's law:
specific enthalpy

$$k = \int_{r}^{p}\frac{dp'}{\rho(p')} = \frac{2k_{b}T}{m_{p}}\int_{r}^{\rho}\frac{d\rho'}{\rho'} = \frac{2k_{b}T}{m_{p}}\ln(\rho)$$

$$\frac{1}{v}\frac{\mathrm{d}v}{\mathrm{d}r}\left\{v^2 - \frac{2kT}{m_{\rm p}}\right\} = \left\{\frac{4kT}{m_{\rm p}r} - \frac{GM_{\odot}}{r^2}\right\}$$
(2.10)
$$\frac{d}{dr}\left\{\frac{v^2}{2} - \frac{2k_bT}{m_p}\ln(v)\right\} = \frac{d}{dr}\left\{\frac{2k_bT}{m_p}\ln(r^2) + \frac{GM_{\odot}}{r}\right\} \qquad \text{because} \\ \mathbf{f}(\mathbf{v}) = \mathbf{v}^2/2 - \mathbf{c_s}^2\ln(\mathbf{v}) \qquad -\mathbf{g}(\mathbf{r}) = \mathbf{c_s}^2\ln(\mathbf{A}) - \Psi(\mathbf{r})$$





Bernoulli's law: $v^2/2 + w + \Psi(r) = constant$ specific enthalpy ~ c_s^2 ~ kinetic energy of particles Q: how does the wind escape? How does it end up going faster? c_s ~ 150 km/s $v \sim 0$ $\Psi(R) = -v_{esc}^{2}/2$; $v_{esc} \sim 600 \text{ km/s}$

$$\frac{1}{v}\frac{\mathrm{d}v}{\mathrm{d}r}\left\{v^2 - \frac{2kT}{m_{\rm p}}\right\} = \left\{\frac{4kT}{m_{\rm p}r} - \frac{GM_{\odot}}{r^2}\right\}$$
(2.10)
$$\frac{d}{dr}\left(\frac{v^2}{2}\right) - \frac{2k_bT}{m_p}\frac{d}{dr}\ln(v) = \frac{2k_bT}{m_p}\frac{d}{dr}\ln(r^2) + \frac{d}{dr}\left(\frac{GM_{\odot}}{r}\right)$$

$$\frac{1}{v}\frac{\mathrm{d}v}{\mathrm{d}r}\left\{v^2 - \frac{2kT}{m_{\rm p}}\right\} = \left\{\frac{4kT}{m_{\rm p}r} - \frac{GM_{\odot}}{r^2}\right\}$$
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$$\frac{d}{\mathrm{d}r}\left\{\frac{v^2}{2} - \frac{GM_{\odot}}{r}\right\} = \frac{2k_bT}{m_p}\frac{d}{\mathrm{d}r}\ln(vr^2) = p\frac{d}{\mathrm{d}r}\left(\frac{1}{\rho}\right)$$

kinetic potential -work = p dV/dr = -de/dr + dQ/dr

$$\frac{d}{dr}\left\{\frac{v^2}{2} + e - \frac{GM_{\odot}}{r}\right\} = \frac{dQ}{dr} = T\frac{ds}{dr} \quad \text{heating} \quad \text{NB: de/dr} = 0$$

$$\frac{1}{v}\frac{\mathrm{d}v}{\mathrm{d}r}\left\{v^2 - \frac{2kT}{m_{\rm p}}\right\} = \left\{\frac{4kT}{m_{\rm p}r} - \frac{GM_{\odot}}{r^2}\right\}$$
(2.10)
$$\frac{d}{dr}\left\{\frac{v^2}{2} - \frac{2k_bT}{m_p}\ln(v)\right\} = \frac{d}{dr}\left\{\frac{2k_bT}{m_p}\ln(r^2) + \frac{GM_{\odot}}{r}\right\}$$
because
$$\frac{d}{dr}\left\{\frac{v^2}{2} + e - \frac{GM_{\odot}}{r}\right\} = \frac{dQ}{dr} = T\frac{ds}{dr}$$
heating

Q: how can I easily see that heat (i.e. entropy) must be added to the wind to keep T constant?

A: ds/sr = 0 \rightarrow T ~ $\rho^{\gamma-1} = \rho^{2/3}$ will decrease moving outward









Activity 37 (p. 71): Make comparisons of energy densities for the solar wind as in Sec. 3.5.2 at other bodies in the Solar System (using Table 5.2). Why comparisons of energy densities in planetary magnetic fields (Table 5.2) and in the surrounding solar wind are informative is discussed in Ch. 5. Why would you expect the ow energy density and the magnetic field energy density to be comparable at only a few solar radii from the Sun?

Planet	Distance $d_{\rm p}$ (AU) ^a	Solar wind density (cm^{-3})	$B_{\rm IMF} \ (\mu { m G})^{\ c}$	$\approx \beta$	$\approx v_{\rm A}$ (km/s)
Mercury	0.39	53	410	2	120
Venus	0.72	14	140	4	80
Earth	1	7^b	80	6	70
Mars	1.52	3	50	6	60
Jupiter	5.2	0.2	10	10	50
Saturn	9.5	0.07	6	10	50
Uranus	19	0.02	3	10	50
Neptune	30	0.006	2	10	50

Plasma β values assume a solar-wind temperature of 1.5 MK.

Table 5.2. Properties of the solar wind near the planets [after Table H-I:13.2].

^{*a*} 1 AU = $1.5 \, 10^8$ km; ^{*b*}tThe density of the solar wind fluctuates by about a factor of 5 about typical values of $\rho_{\rm sw} \sim (7 \, {\rm cm}^{-3})/d_{\rm p}^2$; ^{*c*} mean values. [...]

Activity 37 (p. 71): Make comparisons of energy densities for the solar wind as in Sec. 3.5.2 at other bodies in the Solar System (using Table 5.2). Why comparisons of energy densities in planetary magnetic fields (Table 5.2) and in the surrounding solar wind are informative is discussed in Ch. 5. Why would you expect the flow energy density and the magnetic field energy density to be comparable at only a few solar radii from the Sun?



Activity 133 (p. 263): With average values for solar wind density and velocity (assuming a radial outflow at constant velocity and with a density as specified in Table 2.4), at what distance from the Sun does the solar wind dynamic pressure equal the interstellar total pressure for estimated values of $B_{LISM} \approx 3$ G, $T_{LISM} \approx 6500$ K, and $n_{p;LISM} \approx 0.06$ cm⁻³ and $n_{H;LISM} \approx 0.18$ cm⁻³ (see, e.g., Sect. H-IV:3.2)?



B large enough to restrict plasma motion: only along field lines



Different coronae from different magnetic topology: open vs. closed



Why are some field lines open & others closed?

Magnetic field dominates:

nothing capable of countering its force so...

$$(\nabla \times \mathbf{B}) \times \mathbf{B} = 0$$
$$\Rightarrow \nabla \times \mathbf{B} = \alpha \mathbf{B} \quad (ie.\|\mathbf{B})$$

simplest version: $\alpha = 0$ (by fiat)

$$\Rightarrow \nabla \times \mathbf{B} = 0 \quad \Rightarrow \left[\mathbf{B} = -\nabla \chi \right] \quad \mathsf{p}_{(c)}$$

potential field (cf. electrostatics)

$$\nabla \cdot \mathbf{B} = 0 \quad \Longrightarrow \quad \nabla^2 \chi = 0$$

harmonic potential (cf. electrostatics in vacuum)

 $\mathbf{B} = -\nabla \chi \quad \& \quad \nabla^2 \chi = 0$

potential field outside sphere r=R_o



$$\mathbf{B} = -\nabla \chi \quad \& \quad \nabla^2 \chi = 0 \quad \begin{array}{c} \text{potential field outside} \\ \text{sphere } \mathbf{r} = \mathbf{R}_o \end{array}$$

Field: purely radial @ r=R_s (by fiat)

$$(B_{\theta}, B_{\varphi}) = 0 \implies \left(\frac{\partial \chi}{\partial \theta}, \frac{\partial \chi}{\partial \varphi}\right) = 0$$

$$\Rightarrow \chi(R_{s}, \theta, \varphi) = 0 \quad \text{Dirichlet}$$

$$\chi(r, \theta, \varphi) = \sum_{\ell,m} A_{\ell,m} \left[\left(\frac{R_{s}}{r}\right)^{\ell+1} - \left(\frac{r}{R_{s}}\right)^{\ell}\right] Y_{\ell,m}(\theta, \varphi)$$

$$B_{r}(R_{o}, \theta, \varphi) = -\frac{\partial \chi}{\partial r}\Big|_{r=R_{o}} \quad \text{Observed (Neumann)}$$

$$\theta_{r}(R_{o}, \theta, \varphi) = \sum_{\ell,m} \frac{A_{\ell,m}}{R_{s}} \left[(\ell+1)\left(\frac{R_{s}}{R_{o}}\right)^{\ell+2} + \ell\left(\frac{R_{o}}{R_{s}}\right)^{\ell-1}\right] Y_{\ell,m}(\theta, \varphi)$$

$$\theta_{r}(R_{o}, \theta, \varphi) = \sum_{\ell,m} \frac{A_{\ell,m}}{R_{s}} \left[(\ell+1)\left(\frac{R_{s}}{R_{o}}\right)^{\ell+2} + \ell\left(\frac{R_{o}}{R_{s}}\right)^{\ell-1}\right] Y_{\ell,m}(\theta, \varphi)$$

$$\theta_{r}(R_{o}, \theta, \varphi) = \sum_{\ell,m} \frac{A_{\ell,m}}{R_{s}} \left[(\ell+1)\left(\frac{R_{s}}{R_{o}}\right)^{\ell+2} + \ell\left(\frac{R_{o}}{R_{s}}\right)^{\ell-1}\right] Y_{\ell,m}(\theta, \varphi)$$

Activity 62 (p. 124): The solar wind stretches the high-coronal magnetic field into the heliosphere into a roughly radial field below the Alfven radius. This enables an analogy with electrostatics: the field of electric charges placed above a perfect conductor can be computed by placing mirror charges opposite to the conducting surface, which then naturally has the electric field perfectly normal to the conducting surface. Analogously, in a magneto-static consideration above the spherical Sun, the magnetic field can be approximated by placing mirror 'charges' on a sphere at distance d_{ss}^2/R_{\odot} which then has the field perfectly radial at d_{ss} . This is called the 'source surface model' ... For illustration, simplify the source-surface model by a 2-d sketch involving a line of charges and another of mirror charges. Sketch the equivalent of the foundation of the heliospheric current sheet and examples of 'closed' field lines (the equivalent of coronal loops closing back onto the solar surface) and 'open' field lines (the equivalent of field stretched out into the heliosphere), at the base of which we find dark 'coronal holes' in X-ray images of the Sun.







Solar wind flows from open field crossing r=R_s ... the `source' of the wind → the `source surface' $B_r(\theta,\phi)$ ``measured'' over entire sphere

- accumulate strips over 27-day rotation
- hope that not much changes
- fill in poles (somehow)
- decompose w/ spherical harmonics
- coeffs. $\rightarrow A_{l,m}$

Assumptions of the PFSS

• No currents in coronal field (simplest equilibrium)

 $\nabla \times \mathbf{B} = 0 \qquad R_o < r < R_s$

- Field becomes open (radial) @ fixed radius r=R_s
- Not much change during 27-day accumulation



- Model distinguishing open/closed coronal field
- ➔ Field actually open will be source of solar wind, less dense & dark in EUX & SXR



for large
$$r: v_{\phi} \approx \frac{\Omega r_{\rm A}^2}{r} \to 0; B_{\phi} \approx -\frac{B_r \Omega r}{v_r},$$
 (5.20)

Activity 61 (p. 122): At what distance from the Sun does the above solar-wind model have $|B_r| = |B_{\phi}|$ for typical values of the slow and fast solar wind?

 $\Omega \approx 2\pi / (30 \text{ d}) = 2.5 \times 10^{-6} \text{ rad/s}$ $v_r^{(s)} \approx 400 \text{ km/s} = 4 \times 10^7 \text{ cm/s}$ $v_r^{(s)} / \Omega \approx 1.6 \times 10^{13} \text{ cm} = 1 \text{ AU}$ $v_r^{(f)} = 2 v_r^{(s)}$

 $v_r^{(f)}/\Omega = 2 AU$



Historical interlude

Lord Kelvin once argued that it was impossible for magnetic distrurbances on the Sun to be responsible for geomagnetic activity on Earth (i.e. space weather should not occur). He did so using reasoning we continue to use all the time:

Magnetic field far away from currents will be dominated by the leading-order multipole – the dipole – which decreases with distance as B \sim r $^{-3}$. At this rate the field will be negligible at 1 AU.

We have concluded above that $B_r \sim r^{-2}$ and $B_{\phi} \sim r^{-1}$ in clear contradiction of Kelvin's reasoning. What aspect of his argument is incorrect? What was he unaware of?





WSO - Source Surface Field



0, <u>+</u>1, 2, 5, 10, 20 MicroTesla



Effect of a ``warped" HCS



Vol. III fig. 8.6

Vol. III fig. 8.7







Why does the ``reverse shock'' propagate forward (i.e. outward)?

Ignore spherical geometry: 1d picture of fast behind slow:



Why does the ``reverse shock'' propagate forward (i.e. outward)?





Summary

- Corona: because there is heating reaches high T because radiation cannot balance heating so conduction is needed
- More heat → higher density
- Wind: because there is heating advective energy flux balances heating
- Creates heliosphere